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Creating genomic relationship matrices with preGSf90

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preGSf90

- Performs Quality Control of SNP information
- Creates the genomic relationship matrix (**G**)
 - and relationships based on pedigree (**A**₂₂)
 - Inverse of relationship matrices



BLUP-based models

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{A}^{-1} \frac{\sigma_e^2}{\sigma_a^2} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{W}'\mathbf{y} \end{bmatrix}$$

BLUP

Henderson, 1963

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{G}^{-1} \frac{\sigma_e^2}{\sigma_a^2} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{W}'\mathbf{y} \end{bmatrix}$$

GBLUP

Nejati-Javaremi et al., 1997
Fernando, 1998
VanRaden, 2008

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{H}^{-1} \frac{\sigma_e^2}{\sigma_a^2} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{W}'\mathbf{y} \end{bmatrix}$$

ssGBLUP

Misztal et al. (2009)
Legarra et al. (2009)
Aguilar et al. (2010)
Christensen & Lund
(2010)

$$\mathbf{H}^{-1} = \begin{bmatrix} \mathbf{A}^{11} & \mathbf{A}^{12} \\ \mathbf{A}^{21} & \mathbf{A}^{22} \end{bmatrix} + \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{G}^{-1} - \mathbf{A}_{22}^{-1} \end{bmatrix}$$

$$\mathbf{H}^{-1} = \mathbf{A}^{-1} + \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{G}^{-1} - \mathbf{A}_{22}^{-1} \end{bmatrix}$$

PreGSf90

- Created to construct the matrices using in ssGBLUP

$$\mathbf{H}^{-1} = \mathbf{A}^{-1} + \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{G}^{-1} - \mathbf{A}_{22}^{-1} \end{bmatrix}$$

$$\mathbf{G} \qquad \mathbf{G}^{-1}$$

$$\mathbf{A}_{22} \qquad \mathbf{A}_{22}^{-1}$$

$$\mathbf{G}^{-1} - \mathbf{A}_{22}^{-1}$$

Genomic Relationship Matrix - **G**

- $$\mathbf{G} = \frac{\mathbf{Z}\mathbf{Z}'}{2 \sum p_i(1-p_i)} \quad (\text{VanRaden, 2008})$$

- Z = matrix for SNP marker

- Dimension of $Z = n * i$

- n animals

- i markers

Genotype Codes


0 – Homozygous

1 – Heterozygous

2 – Homozygous

5 – No Call (Missing)

SNP file



```
80 21101011002012011011010110111111211111210100
8014 21110101511101120221110111511112101112210100
516 21100101202252021120210121102111202212111101
181 21110111112201120550200020101022212211111100
```

HOW TO: Creation of Genomic Matrix

- Read SNP marker information => **M**
$$\begin{bmatrix} 2 & 1 & 2 & \dots \\ 0 & 1 & 0 & \dots \\ \dots & \dots & \dots & \dots \end{bmatrix}$$
- Get 'means' to center
 - Calculate allele frequency from observed genotypes (p_i)
 - $p_i = \text{sum}(\text{SNPcode}_i) / 2n$
- Centered matrix **Z** = **M** – 2**P**
- **G** =
$$\frac{\mathbf{ZZ}'}{2 \sum p_i(1-p_i)}$$
 (VanRaden, 2008)

Creation of Genomic matrix

- Issues
 - Large number of genotyped individuals
 - Large number of SNP markers
 - Matrix multiplication $\sim \text{cost } n^2 * i$
- Large amounts of data put in (cache) memory to do matrix multiplication for each pair of animals and indirect memory access (center)

PreGSf90

- Efficient methods
 - create the genomic relationship matrix and the relationship matrix based on pedigree
 - Invert the relationship matrices
- Computes statistics for the matrices
 - Means, Var, Min, Max
 - Correlations between diagonals
 - Correlations for off-diagonals
 - Correlations for the full matrices
 - Regression coefficients

OPTIONS – preGS90 parameter file

- PreGSF90

- controled by adding OPTION commands to the parameter file

```
OPTION SNP_file marker.geno.clean
```

- Reads:

- `marker.geno.clean`
 - `marker.geno.clean.XrefID` (created by renumf90)
 - Pedigree file
 - Map file (optional)

Genomic Matrix default options

- $\mathbf{G}_0 = \frac{\mathbf{Z}\mathbf{Z}'}{2 \sum p_j(1-p_j)}$ (VanRaden, 2008)
- With:
 - \mathbf{Z} centered using current allele frequencies
 - Current genotyped animals

Genomic Matrix Options

- OPTION whichfreq *x*
 - 0: read from file *freqdata* or other specified name (needs OPTION FreqFile)
 - 1: 0.5
 - 2: current calculated from genotypes (default)
- OPTION FreqFile *file*
 - Reads allele frequencies from a file

Genomic Matrix default options

- **Blending** - to avoid singulativity problems

$$\mathbf{G} = 0.95 * \mathbf{G}_0 + 0.05 * \mathbf{A}_{22}$$

– OPTION AlphaBeta 0.95 0.05 #(default)

– Beta may vary from 0.2 to 0.01

Genomic Matrix default options

- **Tuning**

- Adjust \mathbf{G} to have mean of diagonals and off-diagonals equal to \mathbf{A}_{22}
- OPTION tunedG 2 #(default) Chen et al. (2011)

- Base of GBLUP is *genotyped* animals
- Base of pedigree is *founders of the pedigree*
- For SSGBLUP modelled as a mean for genotyped animals
 - $p(\mathbf{u}_2) = N(\mathbf{1}\mu, \mathbf{G})$
 - Integrate $\mu : \mathbf{G}^* = \mathbf{1}\mathbf{1}'\lambda + (1 - \lambda/2)\mathbf{G}$
 - $\mu = (\text{Genomic base}) - (\text{Pedigree base})$
 - Vitezica et al. 2011

Options for matching \mathbf{G} to \mathbf{A}_{22}

- OPTION tunedG x
 - 0: no adjustment
 - 1: $\text{mean}(\text{diag}(\mathbf{G}))=1$, $\text{mean}(\text{offdiag}(\mathbf{G}))=0$
 - 2: $\text{mean}(\text{diag}(\mathbf{G}))=\text{mean}(\text{diag}(\mathbf{A}_{22}))$,
 $\text{mean}(\text{offdiag}(\mathbf{G}))=\text{mean}(\text{offdiag}(\mathbf{A}_{22}))$ (default)
 - 3: $\text{mean}(\mathbf{G})=\text{mean}(\mathbf{A}_{22})$
 - 4: Use Fst adjustment. Powell et al. (2010) & Vitezica et al. (2011)

$$\lambda = \frac{1}{n^2} \left(\sum_i \sum_j \mathbf{A}_{22ij} - \sum_i \sum_j \mathbf{G}_{ij} \right) \quad \mathbf{G}^* = \mathbf{1}\mathbf{1}'\lambda + (1 - \lambda/2)\mathbf{G}$$

Storing and Reading Matrices

- preGSf90 saves $\mathbf{G}^{-1} - \mathbf{A}_{22}^{-1}$ by default (file: GimA22i)

To save 'raw' genomic matrix:

- OPTION saveG [all]
 - If the optional *all* is present all intermediate \mathbf{G} matrices will be saved!!!

To save \mathbf{G}^{-1}

- OPTION saveGInverse
 - Only the final \mathbf{G} , after blending, scaling, etc. is inverted !!!

To save \mathbf{A}_{22} and inverse

- OPTION saveA22 and OPTION saveA22Inverse

Storing and Reading Matrices

- `OPTION saveG [all] , OPTION saveGInverse, ...`
 - Saves in binary format
 - “Dumped” format to save space and time
 - To save as row, column, value:
 - `OPTION no_full_binary`
 - Still binary, but can be easily read and converted to text

Storing with Original IDs

- Some matrices could be stored in text files with the original IDs extracted from *renaddxx.ped* created by the RENUMF90 program (col #10)
- For example:
 - OPTION saveGOrig
 - OPTION saveDiagGOrig
 - OPTION saveHinvOrig
- Values
 - origID_i, origID_j, val

Genomic Matrix - Population structure

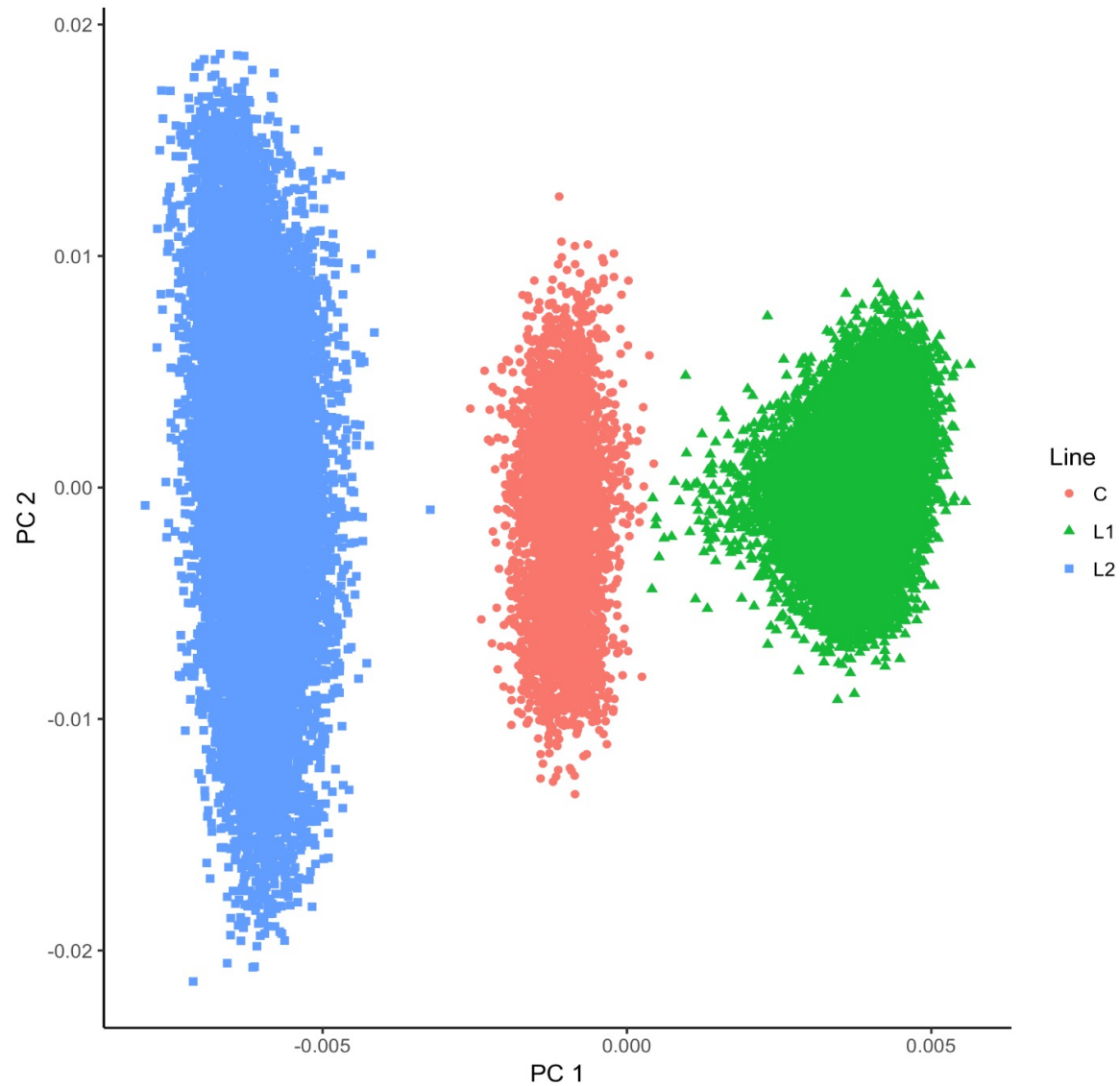
```
OPTION plotpca
```

Plot first two principal components to look for stratification in the population.

```
OPTION extra_info_pca file col
```

Reads from *file* the column *col* to plot with different colors for different classes.

Genomic Matrix - Population structure



Tricks to setup **G** for GBLUP

- Tricks are needed because preGSf90 is set up for ssGBLUP

1) Use a dummy pedigree

1 0 0

2 0 0

...

2) Use PED_DEPTH 1 in renumf90

3) Change blending parameters

– OPTION AlphaBeta 1.00 0.00 → $G = 1.00 * \mathbf{G} + 0.00 * \mathbf{I}$

– OPTION AlphaBeta 0.99 0.01 → $G = 0.99 * \mathbf{G} + 0.01 * \mathbf{I}$

4) No adjustment for compatibility with \mathbf{A}_{22}

– OPTION tunedG 0

PreGSf90 inside BLUPF90 ??

- Almost all programs from BLUPF90 support the creation of genomic relationship matrices
- `OPTION SNP_file xxxx`
- Why preGSF90 ?
 - Same genomic relationship matrix for several models, traits, etc.
 - Just do it once and store GimA22i

Use in application programs

- Use renumf90 for renumbering and creation of XrefID and files
SNP_FILE
marker.geno
- Run preGSf90 with quality control, saving clean files
- Option 1:
run blupf90 with clean files
- Option 2:
run preGSf90 with clean files (program saves **GimA22i**)
run blupf90 with option to read **GimA22i** from the file

Reading external matrices

- BLUPF90 programs accept external matrices created outside
- http://nce.ads.uga.edu/wiki/doku.php?id=user_defined_files_for_covariances_of_random_effects
- File should be row, column, value in plain text format (lower OR upper triangular)

renf90.par

```
RANDOM_GROUP
# genomic
2
RANDOM_TYPE
user_file
FILE
# matrix file
Gi
```

Valid format

```
1 1 1
1 2 0.5
2 2 1
```

Non-valid format

```
1 1 1
1 2 0.5
2 1 0.5
2 2 1
```

- user_file: if providing the inverse of the covariance structure
- user_file_inv: if the program has to invert the covariance structure