# **Manual for**

# **BLUPF90 family of programs**

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## Introduction

BLUPF90 is a family of programs for mixed-model computations focusing on animal breeding applications. The programs can do data conditioning, estimate variances using several methods, calculate BLUP for very large data sets, calculate approximate reliabilities, and use SNP information for improved accuracy of breeding values and genome-wide association studies (GWAS).

The programs have been designed with 3 goals in mind:

- 1. Flexibility to support a large set of models found in animal breeding applications.
- 2. Simplicity of software to minimize errors and facilitate modifications.
- 3. Efficiency at the algorithmic level.

Aside from being used in hundreds of studies, the programs are utilized for commercial genetic evaluation in dairy, beef, pigs, chicken, fish, plants, and beyond by major companies/institutions/associations in the US and worldwide.

The programs are written in Fortran 90/95 and originated as exercises for a class taught by Ignacy Misztal at the University of Georgia. Over time, they have been upgraded and enhanced by many contributors. Details on programming and computing algorithms are available in an Interbull <u>paper</u> (Misztal, 1999) and as course notes. Old versions of source codes for nearly all programs are available **here**.

Additional information about the programs is available at http://nce.ads.uga.edu/wiki/doku.php as wiki pages. There is a BLUPF90 discussion group at groups.io.

## List of programs from Wiki page

The latest binaries are available here.

All binaries for Linux, Mac OSX, and Windows are updated frequently. Always check for the most updated versions.

The programs support mixed models with multiple-correlated effects, multiple animal models and dominance.

- a combined program of blupf90, remlf90, and airemlf90 BLUPF90+ GIBBSF90+ - a combined program of gibbs2f90, gibbs3f90, thrgibbs1f90, and thrgibbs3f90 BLUPF90 – BLUP in memory REMLF90 - accelerated EM REML AIREMLF90 - Average Information REML with several options including EM-REML and heterogeneous residual variances (S. Tsuruta) CBLUP90 - solutions for bivariate linear-threshold models CBLUP90THR - as above but with thresholds computed and many linear traits (B. Auvray) CBLUP90REML - as above but with guasi REML (B. Auvray) GIBBSF90 - simple block implementation of Gibbs sampling GIBBS1F90 - as above but faster for creating mixed model equations only once GIBBS2F90 - as above but with joint sampling of correlated effects GIBBS3F90 - as above with support for heterogeneous residual variances POSTGIBBSF90 - statistics and graphics for post-Gibbs analysis (S. Tsuruta) - Gibbs sampling for any combination of categorical and linear traits (D. Lee) THRGIBBSF90 - as above but simplified with several options (S. Tsuruta) THRGIBBS1F90 THRGIBBS3F90 - as above with heterogeneous residual variances for linear traits **RENUMF90** - a renumbering program that also can check pedigrees and assign unknown parent groups; supports large datasets - a program to calculate inbreeding coefficients with incomplete pedigree (I. **INBUPGF90** Aguilar) SEEKPARENTF90 - a program to verify paternity and parent discovery using SNP markers (I. Aguilar) PREDICTF90 - a program to calculate adjusted y,  $\hat{y}$ , and residuals (I. Aguilar) PREDF90 - a program to predict direct genomic values (DGV) and their reliabilities for animals based on genotypes and SNP solution **QCF90** - a quality-control tool on genotypes and pedigree information (Y. Masuda) - joint analysis of QTL and polygenic effects (M. Perez-Enciso) **QXPAK** Available by request MRF90 - Method R program suitable for very large data sets; contact T. Druet. COXF90 - Bayesian Cox model - contact J. P. Sanchez (JuanPablo.Sanchez@irta.cat) **BLUPF90HYP** - BLUPF90 with hypothesis testing (F and Chi2 tests) - contact J. P. Sanchez as above Available only under research agreement BLUP90IOD2 - BLUP by iteration on data with support for very large models (S. Tsuruta) - a combined program of BLUP90IOD2, BLUP90IOD2RR, BLUP90IOD2HR, and BLUP90IOD3 BLUP90MBE2 with new features CBLUP90IOD - BLUP by iteration on data for threshold-linear models ACCF90 - approximation of accuracies for breeding values - approximation of accuracies for genomic breeding values based on diagonals of ACCF90GS
  - - G

- ACCF90GS2 new approximation of accuracies for genomic breeding values based on block sparse inversion
- BLUP90MBE BLUP by iteration on data with support for very large models for multi-breed evaluations
- BLUP90ADJ BLUP with a data preadjustment tool

Included in application programs

- PREGSF90 genomic preprocessor that combines genomic and pedigree relationships (I. Aguilar)
- POSTGSF90 genomic postprocessor that extracts SNP solutions after genomic evaluations (single step, GBLUP) (I. Aguilar)

Other programming contributions were made by Miguel Perez-Enciso (user\_file) and François Guillaume (Jenkins hashing functions).

## Main programs in a chart



Application programs (BLUP\*, \*REMLF90, THRGIBBS\*, GIBBS\*, POSTGIBBSF90, PREGSF90, POSTGSF90, and PREDICTF90) are driven by parameter files and require data files with effects renumbered from 1 consecutively. Some programs (PREDF90, QCF90, and SEEKPARENTF90) use command line instead of a parameter file.

Renumbering and quality control can be done by RENUMF90, which is also driven by a parameter file (different from the previous programs). Separation of renumbering and application programs allows supporting complicated models.

Some models are not directly supported by RENUMF90 and require tweaking the parameter file in the application programs.

## Parameter file for application programs

The parameter file has keywords that are fixed (i.e., cannot be changed and should be typed exactly as shown here) followed by values, with the following structure. The example below comes from a 2-trait maternal model:

Keywords*	Description
DATAFILE	Name of file with phenotypes; free Fortran format (space-delimited file)
file.dat	
NUMBER OF TRAITS	Number of traits
2	
NUMBER OF EFFECTS	Number of effects in a model except for residual
6	
OBSERVATIONS(S)	Position(s) of observations in data file
1 2	
WEIGHTS	Position of weight on observations if used; otherwise blank
2	means that the weight is in column 2, and residual variance (R) is set to R/weight.
EFFECTS: POSITIONS_IN_DATAFILE NUM	BER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
4 4 10 cross	4 4 = crossclassified effect positions in data file for 2 traits; 10 = levels
5 0 100 cross	<b>5 0</b> = crossclassified effect, positions for 2 traits; <b>100</b> = levels
6 6 1 cov	6 6 = covariable positions in data file
7 7 10 cov 4 4	7 7 = covariable nested in effect position 4; 10 = levels
8 8 1000 cross	8 8 = crossclassified effect positions for 2 traits; 1000 = levels
0 9 1000 cross	<b>0 9</b> = crossclassified effect positions for 2 traits; <b>1000</b> = levels
RANDOM_RESIDUAL_VALUES	Residual variance or residual covariance matrix
10 1	For 2 trait model
1 10	
RANDOM_GROUP	List of effect numbers that form a group
5 6	For correlated random effects 5 6
RANDOM_TYPE	Type of random effect
add_animal	diagonal, add_sire, add_an_upg, add_an_upginb, par_domin, or user_file
FILE	Pedigree file or other file associated with random effect; blank if none
file.ped	
(CO)VARIANCES	(Co)variance matrix for each random effect
10 1 0 1	For 2 trait, maternal model
1 10 0 1	
0 0 0 0	
1 1 0 10	

\*Keywords need to be typed exactly (up to 20 characters). Hint: When preparing a new parameter file, consider modifying an existing file.

Note that this parameter file is for the application programs (BLUPF90, AIREMLF90, GIBBSF90, etc.) and not for RENUMF90. This program needs a different type of parameter file. See page <u>16</u> for details.

## **Description of effects**

The effects are specified after the keyword:

#### EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED]

Each line contains the following:

- Position(s) of each effect in the data file; t positions for t traits
- Number of levels (assumed consecutive from 1)
- Type of effect: "cross" for cross-classified, and "cov" for covariable
  - Cross-classified uses integer numbers starting at 1
  - o Covariable uses integer or real numbers
- For nested covariables, the following number (or t numbers for t traits) indicates the position of nesting in the data file
- Text after # can be used as a comment

Data and pedigree file should not have header; columns should be separated by at least one space (no TAB); hash (#) is interpreted as a comment initiator and should not be present inside the data and pedigree files. See page <u>15</u> for further details.

Consider the following dataset (copied to file.dat without the header):

i	j	k	y1	y2	<b>x</b> 1
2	2	3	4.30	5.67	22.40
1	2	2	2.76	3.20	18.00
3	1	1	2.20	5.30	7.25

Let i go from 1 to 50, j from 1 to 80, and k from 1 to 200. The model:

 $y1_{ij} = a_j + b_i + cx1 + e_{ij}$ 

will be specified in the parameter file as:

```
DATAFILE
file.dat
NUMBER_OF_TRAITS
1
NUMBER_OF_EFFECTS
3
OBSERVATIONS(S)
4
WEIGHTS
```

```
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
2 80 cross # position 2, 80 levels
1 50 cross # position 1, 50 levels
6 1 cov # covariable on position 6, one level
.....
```

By definition, a regular covariable has one level (i.e., a slope as regression).

For a similar model but with a nested covariable:

 $y_{1ij} = a_j + b_i + c_i x_1 + e_{ij}$ 

The description will change to:

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 2 80 cross # position 2, 80 levels 1 50 cross # position 1, 50 levels 6 50 cov 1 # covariable on position 6 nested in position 1; 50 levels

Assume a two-trait model:

 $y1_{ij} = a1_j + c1_ix1 + e1_{ij}$  $y2_{ij} = b2_i + c2_ix1 + e2_{ij}$ 

This corresponds to:

```
.....
NUMBER_OF_TRAITS
2
NUMBER_OF_EFFECTS
3
.....
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
2 0 80 cross # position 2 for trait 1 only, 80 levels
0 1 50 cross # position 1 for trait 2 only, 50 levels
6 6 50 cov 1 1 # covariable on position 6 for two traits nested in position 1
```

"0" in effect definitions means missing effect per trait.

The first two effects in the two-trait model above can be merged:

#### NUMBER OF EFFECTS

2

•••••

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED]

2 1 80 cross # positions 2 and 1 for traits 1 and 2, 80 is max(50,80) levels

6 6 50 cov 1 1 # covariable in position 6 for two traits nested in position 1

## **Definition of random effects**

**RANDOM\_GROUP** defines one group of random effects. A group is one effect or multiple (correlated) effects that share the same covariance structure, e.g., direct-maternal effect or random regressions.

The structure of **RANDOM GROUP** is:

RANDOM_GROUP 5	Corresponding to the effect number specified above; "5" means that the $5^{th}$ effect is random. Or "5 6" means that $5^{th}$ and $6^{th}$ are correlated random effects.
or	
RANDOM_GROUP 5 6	Corresponding to the effect number specified above; "5 6" means that $5^{th}$ and $6^{th}$ are correlated random effects.

**RANDOM\_TYPE** defines a covariance structure: diagonal var() =  $s \otimes I$  or **G** where s is a variance and **G** is a covariance matrix. For other types, see "Random effects and Pedigree files" on page <u>13</u>.

Assume a model:

y = farm + animal\_additive + permanent\_environment + error

```
with var(animal_additive) = A \otimes 2.5, var(permanent_environment) = I \otimes 5.1, var(error) = I \otimes 13.7
```

With these effects:

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 3 100 cross # effect 1: farm 2 1000 cross # effect 2: additive genetic 2 1000 cross # effect 3: permanent environment RANDOM\_RESIDUAL\_VALUES 13.7 RANDOM\_GROUP # this is for effect 2 on the effect list 2 RANDOM\_TYPE add\_animal # additive genetic FILE file.ped # name of pedigree file (CO)VARIANCES 2.5 RANDOM\_GROUP 3 # effect 3 on the effect list above RANDOM TYPE diagonal # permanent environment FILE # no file associated with diagonal structures (CO)VARIANCES 5.1

## **Correlated effects**

Assume a model:

y = farm + season + direct + maternal + error

var(direct,maternal)=  $\mathbf{A} \otimes \begin{bmatrix} 5 & 1 \\ 1 & 6 \end{bmatrix}$ 

with the effects as specified:

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED]

3100 cross# effect 1: farm44 cross# effect 2: season21000 cross# effect 3: direct

2 1000 cross # effect 3: maternal

The distribution of the random effects is specified below:

RANDOM\_GROUP 3 4 # direct and maternal effects RANDOM\_TYPE add\_animal # additive genetic FILE file.ped # name of pedigree file (CO)VARIANCES 5 1 1 6 ...

Random regression models may have many correlated random effects. Assume a data file with the following positions:

1 to 4: polynomials

- 5: animal number (1000 levels)
- 6: herd year season (50 levels)

```
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
                  # herd year season
6 50 cross
1 1000 cov 5
                  # first polynomial nested within the animal effect position 5
2 1000 cov 5
                  # second polynomial nested within the animal effect position 5
3 1000 cov 5
                  # third polynomial nested within the animal effect position 5
                  # fourth polynomial nested within the animal effect position 5
4 1000 cov 5
RANDOM_GROUP
2345
                  # all covariables are correlated (effects 2, 3, 4, and 5 on the list above)
RANDOM_TYPE
add_animal
                  # additive genetic
FILE
                  # name of pedigree file
file.ped
(CO)VARIANCES
 (4 x 4 matrix)
```

## **Random effects and Pedigree files**

There are a few types of additive genetic effects, each with a different pedigree format.

a) additive sire (add\_sire)

The pedigree file has the following format: sire number, sire's sire number, sire's maternal grandsire (MGS) number where unknown sire's sire and/or sire's MGS numbers are replaced by 0.

#### b) additive animal (add\_animal)

The pedigree file has the following format: animal number, sire number, dam number where unknown sire and/or dam numbers are replaced by 0.

## c) additive animal with unknown parent groups (add\_an\_upg)

The pedigree file has the following format:

animal number, sire number, dam number, parent code

where sire and/or dam numbers can be replaced by unknown parent group numbers

parent code = 3 - number of known parents:

1 (both parents known)

2 (one parent known)

3 (both parents unknown)

d) additive animal with unknown parent groups and inbreeding (add\_an\_upginb)

The pedigree file has the following format:

animal number, sire number, dam number, inb/upg code

where sire and/or dam numbers can be replaced by unknown parent group numbers

inb/upg code = 4000 / [(1+ms)(1-Fs) + (1+md)(1-Fd)]

where ms (md) is 0 whenever sire (dam) is known, and 1 otherwise, and Fs(Fd) is the coefficient of inbreeding of the sire (dam). For example, the inb/upg code for the animal with both parents known is 2000. The code should be an integer value.

#### e) user provided matrix (user\_file)

A file specified in FILE contains the inverse of a matrix in the following format:

row col value

as lower- or upper-triangular elements (but not full stored). The matrix is used directly by application programs. For example, to use a genomic relationship matrix **G**, the file needs to contain  $\mathbf{G}^{-1}$ .

f) user provided matrix with inversion (user\_file\_inv)

As above but the matrix in FILE is inverted by the application programs before being used. For example, to use a genomic relationship matrix **G**, the file needs to contain **G**. The inversion is by sparse matrix techniques, so it is efficient for sparse matrices but slow for dense matrices.

#### f) additive animal with selfing (add\_an\_self)

The pedigree file has the following format: animal number, sire number, dam number, number of selfing generations where unknown sire and/or dam numbers are replaced by 0. This option fits some breeding structures in plants.

### e) parental dominance (par\_domin)

The pedigree class file has the following format:

s-d s-sd s-dd ss-d ds-d ss-sd ss-dd ds-sd ds-dd code

where x-y is a combination number of animals x and y, s is sire, d is dam, sd is sire of dam, etc. Code is a number of 0 to 255 and refers to the combination of missing subclasses. If one line is:

#### p s0 s1 s2 s3 s4 s5 s6 s7 code

then code =  $\sum_{i=0}^{7} (a_i \times 2^i)$  where  $a_i = 0$  if  $s_i > 0$ , or  $a_i = 1$  otherwise.

For example, the code for a line with all nonzero parental subclasses is 255. For a line with only zero parental subclasses, if classes are ordered so that lines with zero parental subclasses, code=0. If lines are ordered so that p for parental classes with code = 0 are ordered last, they may be omitted and will be added automatically. The parental dominance file can be created by program **RENDOMN**.

## **Data and Pedigree files**

All files are free format, with fields separated by spaces. By default, 0 is a missing value for all effects, including covariables.

## Transferring a file from Windows (DOS) to Linux environment

Use "dos2unix" to convert the DOS (Windows) format to the UNIX (Linux) format if the programs show an error message while reading a file ("flip -u" can be also used instead of "dos2unix").

## Data file

- a. Space(s) is a delimiter. At least one space between columns is required.
- b. Dot (.) is just one character but not a missing value (default missing value = 0).
- c. Check the data again, especially when converting from another format or software such as EXCEL, SAS, ...
- d. For Gibbs sampling programs with "OPTION cont", copy the previous output files somewhere else just in case making mistakes and replacing those files.

## **Pedigree file**

- a. An original pedigree file for RENUMF90 can include alpha-numeric characters with free format.
- b. Remove duplicates.
- c. Use 0 for unknown parent(s).

## Error messages in the parameter file

a. Wrong data file name:

Check outputs for the data file name and the number of records on the screen. The program will not stop if the wrong file name already exists.

b. Wrong pedigree file name:

Check output for the pedigree file name and the number of animals on the screen. The program will not stop if the wrong file name exists.

- Wrong positions or formats for observations and effects:
   Program may not stop and may get wrong results. Check outputs for the number of levels for each effect on the screen.
- d. Missing or skipping one or more fixed lines in the parameter file: Program may stop. Check the missing line.
- e. Misspelling:

Program may stop. Correct the wrong spelling.

- f. Missing an empty last line:
   Program may not stop. Parameter, data, and pedigree files may need one more extra line at the end of the file.
- g. (Co)variance matrix is not symmetric, not positive definite, not right sized, ... :
   Program may not stop.
- h. A good result does not mean that your parameter file is correct. Always double-check it!

## **RENUMF90 parameter file**

## **Basic rules for RENUMF90 parameter file**

RENUMF90 is a renumbering program to create input (data, pedigree, and parameter) files for BLUPF90 programs and provide basic statistics. Note that RENUMF90 uses a different type of parameter file as used in BLUPF90 or other programs. RENUMF90-specific parameter file should be prepared as follows:

- The file consists of pairs of **keyword** and the corresponding **value(s)**. The keyword is always capital.
- First 7 keywords are mandatory and must appear in the following order: DATAFILE, TRAITS, FIELDS\_PASSED TO OUTPUT, WEIGHT(S), RESIDUAL\_VARIANCE and EFFECT. If you don't actually need FIELDS\_PASSED TO OUTPUT and WEIGHT(S), simply leave an empty line.
- The remaining keywords are optional but appear in the specific order shown below. For example, the FILE keyword must be followed by FILE\_POS (or by SNP\_FILE if FILE\_POS is omitted; or by PED\_DEPTH if both FILE\_POS and SNP\_FILE are omitted, and so on).
- Several **OPTION** lines can be included. RENUMF90 interpret a few options. Other options are simply passed through the template parameter file for BLUPF90 (*renf90.par*).

## **Parameter file**

**DATAFILF** 

f <sub>1</sub>	# data file na	me – input files cannot contain character # because it is used as a comment.
TRAITS		
$t_1 t_2 t_3 \dots$	# posit	ions of traits in data file
FIELDS_P/	ASSED TO OU	ТРИТ
p <sub>1</sub> p <sub>2</sub> p <sub>m</sub> WEIGHT(S	# posit	ions that are not renumbered; put empty line if not needed.
w	# posit	ion of weight - fraction to the residual variance; put empty line if not needed.
RESIDUAL	_VARIANCE	
R	# matr	ix of residual (co)variances
EFFECT		
<b>e</b> <sub>1</sub> <b>e</b> <sub>2</sub> <b>e</b> <sub>3</sub>	type form	<ul> <li># e<sub>1</sub> e<sub>2</sub> e<sub>3</sub> = position of this effect for each trait</li> <li># type = 'cross' for crossclassified or 'cov' for covariables</li> <li># form = 'alpha' for alphanumeric or 'numer' for numeric (form is only for cross)</li> </ul>
EFFECT		
$\begin{array}{c} d_1 \ d_2 \ d_3 \ \ldots \\ \textbf{NESTED} \end{array}$	<b>cov</b> # d <sub>1</sub> d <sub>2</sub>	$d_3 \dots$ = positions of covariables nested in the following cross-classified effects
<b>e</b> <sub>1</sub> <b>e</b> <sub>2</sub> <b>e</b> <sub>3</sub>	form # e <sub>1</sub> e <sub>2</sub>	e <sub>3</sub> = positions of cross-classified effects nested
	# form	= 'alpha' for alphanumeric or 'numer' for numeric
RANDOM		
random_t	ype #'diag	onal', 'sire' or 'animal' for random effect

#### **OPTIONAL**

o<sub>1</sub> o<sub>2</sub> o<sub>3</sub> ... # 'pe' for permanent environment, 'mat' for maternal, and 'mpe' for maternal permanent environment

#### FILE

fped # pedigree file name

#### FILE\_POS

animal sire dam alt\_dam yob # positions of animal, sire, dam, alternate dam (recipient dam), and year of birth in pedigree file (default 1 2 3 0 0).

#### SNP\_FILE

fsnp # specify a SNP file with ID and SNP information; the relationship matrix will include the genomic information; a fsnp file should start with ID with the same format as fped, and SNP info needs to start from a fixed column and include digits 0, 1, 2 and 5 (0, 1, and 2 for SNP count and 5 for missing SNP);

ID and SNP info need to be separated by at least one space; see more information in http://nce.ads.uga.edu/wiki/doku.php?id=readme.pregsf90.

#### PED\_DEPTH

# depth of pedigree search (default 3); all pedigrees are loaded if p = 0.

#### GEN\_INT

р

min avg max # minimum, average, and maximum generation interval; applicable only if year of birth present in pedigree file; minimum and maximum used for pedigree checks; average used to predict year of birth of parent with missing pedigree.

REC\_SEX

sex

t

# if only one sex has records, specifies which parent it is; used for pedigree checks.

#### UPG\_TYPE

# 'yob': based on year of birth.

# 'in\_pedigrees': the value of a missing parent should be -x, where x is UPG number that this missing parent should be allocated to; in this option, all known parents should have pedigree lines, i.e., each parent field should contain either the ID of a real parent, or a negative UPG number.

# 'group': it assigns different groups for sires and dams using a user-defined group label in the pedigree file. The field of the label should be specified as the 6th item in the FILE\_POS entry.

# 'group\_unisex': as above except assigning the same groups to sires and dams. # 'internal', allocation is by a user-written function custom\_upg (year\_of\_birth,sex,ID, parent\_code).

#### INBREEDING

S

# use of inbreeding coefficients to compute inb/upg code in the 4<sup>th</sup> column of the output pedigree file. Inbreeding calculation is default in RENUMF90  $\geq$  v1.157, even if this keyword is not used.

# 'pedigree': the program computes inbreeding coefficients with Meuwissen and Luo (1992) using the pedigree to be saved in renaddxx.ped; calculated inbreeding coefficients will be saved in a file "renf90.inb" with the original ID.

# 'file': the program reads inbreeding coefficients from an external file. You should put the filename after 'file' e.g. 'file inbreeding.txt'. The file has at least 2 columns: original\_ID and inbreeding value (from 0.0 to 1.0). The program skips unnecessary IDs.

# 'self x': Calculates inbreeding with selfing

x is the column in the pedigree file with the number of selfing generations # 'no-inbreeding': turn inbreeding calculation off in RENUMF90  $\geq$  v1.157.

## (CO)VARIANCES

G# (co)variances for animal effects or animal + maternal effects(CO)VARIANCES\_PEGPE# (co)variances for the PE effect(CO)VARIANCES\_MPEGMPE# (co)variances for the MPE effect

## **Combining fields**

How can we specify interactions? - Combining fields or interactions. Several fields in the data file can be combined into one using a **COMBINE** keyword.

COMBINE a b c ....# keywords COMBINE need to be on top of the parameter file (the first keyword).It can be placed after comments.

For example:

## **COMBINE 7 2 3 4**

combines content of fields 2 3 4 into field 7; the data file is not changed, only the program treats field 7 as fields 2 3 4 put together (without spaces). The combined fields can be treated as "numeric" with the total length is < 9 or "alpha". The keyword is optional but must be placed in the top of the parameter file.

Hints: type	renumf90show-template	to have a template parameter file.
type	renumf90version	to see the version number.

## **Options**

RENUMF90 parameter file can accept a few options. If the program detects non-RENUMF90 options, such option lines are simply transferred to *renf90.par*.

**OPTION alpha\_size** nn # new size Changes the maximum size of character fields (default 20 characters).

## **OPTION max\_string\_readline nn**

Changes the maximum length of characters in a line (default 800 characters).

#### **OPTION max\_field\_readline nn**

Changes the maximum number of fields capable in a line (default 100 fields).

#### **OPTION** missing **x**

It allows the indication that x represents a missing value (default is 0), for example if 0 is a valid record. This is only to represent the missing value in the data. If there are covariables in the data, 0 is treated as a value, not missing information. Missing pedigree is always 0 and cannot be changed to another value.

#### **OPTION** missing\_in\_weights

This indicates that, for a given trait, if a weight is 0, then the record value for that trait is converted to a "missing" in the output file *renf90.dat*. For instance, 0 when OPTION missing x is not used, or x otherwise.

#### **OPTION no\_basic\_statistics**

This causes the program to not compute descriptive statistics of the data (mean, minimum, correlations, ...), which can take time for very large datasets.

#### **OPTION inbreeding\_method m**

This allows the user to choose which method is used to compute inbreeding coefficients. Those inbreeding coefficients will be used later (in the other programs) to set up A-inverse. Acceptable values for m are:

- 1. Meuwissen and Luo (1992).
- 2. Modified Meuwissen & Luo by Sargolzaei and Iwaisaki (2004).
- 3. Modified Colleau by Salgolzaei et al. (2005).
- 4. Recursive tabular method.
- 5. Method of Tier (1990).
- 6. Parallel (OMP) version of Meuwissen and Luo (1992)
- 7. Recursive tabular with self-breeding generations.

The default is method 1. Method 6 can largely speed-up the computation, but it requires using many threads (e.g., OMP\_NUM\_THREADS=4).

The end of the parameter file for RENUMF90 can contain many lines with OPTION, those lines are passed to the parameter file *renf90.par* to be used by the other programs.

## **Output files**

RENUMF90 generates several files.

- renf90.par: parameter template file for BLUPF90 and other application programs
- renf90.dat: data file for BLUPF90

- renaddxx.ped: pedigree file for BLUPF90; xx is an integer number that indicates the position of animal effect among all model effects in renf90.par. This file will be created only if RANDOM animal is specified
- *SNPfile\_XrefID*: cross-reference file for genomic analysis, which contains renumbered ID and original ID; *SNPfile* is the original SNP marker file. This file will be created only if **SNP\_FILE** is specified
- *renf90.inb*: inbreeding coefficients. Inbreeding calculation is default in RENUMF90 ≥ v1.157, even if the INBREEDING keyword is not used.
- *renf90.tables*: table relating the original code and the renumbered code
- *renf90.fields*: has detailed description of the effects in each field of renf90.dat.

## **Output pedigree file**

The additive pedigree file built by RENUMF90 is renadd*xx*.ped. The pedigree file has the following structure:

- 1) animal number (from 1)
- 2) parent 1 number or unknown parent group number for parent 1
- 3) parent 2 number or unknown parent group number for parent 2
- 3 minus number of known parents (this column is replaced by inbreeding code if INBREEDING is specified or by default in RENUMF90 ≥ v1.157)
- 5) known or estimated year of birth (0 if not provided)
- 6) number of known parents (for genotyped animals, if any: 10 + number of known parents)
- 7) number of records
- 8) number of progenies as parent 1
- 9) number of progenies as parent 2
- 10) original animal id

## Example

#### Input file - data

## Pedigree file - ped

 aa
 ff
 ee
 2004

 bb
 hh
 gg
 2004

 cc
 hh
 ii
 2004

 dd
 ff
 0
 2004

 ee
 ff
 0
 2002

 ff
 0
 0
 2002

 gg
 ff
 0
 2002

hh 0 0 2002 ii 0 0 2002 kk 0 0 2000

0

0

Parameter file - testpar1 # Parameter file for program renumf90; it is translated to parameter file for BLUPF90 family of programs. DATAFILE data TRAITS 3 FIELDS\_PASSED TO OUTPUT 1 #passing original ID to the renumbered data file WEIGHT(S) **RESIDUAL\_VARIANCE** 1 EFFECT 2 cross num EFFECT 1 cross alpha RANDOM animal FILE ped FILE\_POS 12304 PED\_DEPTH 3 GEN\_INT 1210 UPG\_TYPE yob 2002 2003 (CO)VARIANCES 1 **Output log** RENUMF90 version 1.157 with zlib testpar1 datafile:data traits: 3

```
traits: 3
fields passed: 1
R
1.000
Processing effect 1 of type cross
item_kind=num
Processing effect 2 of type cross
item_kind=alpha
pedigree file name "ped"
positions of animal, sire, dam, alternate dam, yob, and group 1 2 3 0 4
```

21

pedigree traced to generation 3 Minimum, average and maximum generation intervals: 1 2 10 Unknown parent groups separated by years: 2002 2003 Reading (CO) VARIANCES: 1 x 1 Maximum size of character fields: 20 Maximum size of record (max\_string\_readline): 8000 Maximum number of fields for input file (max\_field\_readline): 100 Pedigree search method (ped\_search): convention Order of pedigree animals (animal order): default Order of UPG (upg\_order): default Missing observation code (missing): 0 Using prime hash function hash tables for effects set up first 3 lines of the data file (up to 70 characters) aa 1 10 aa 2 12 bb 1 11 7 records read table with 2 elements sorted added count Effect group 1 of column 1 with 2 levels 10000 records table expanded from 10000 to added count 2 of column Effect group 1 with 5 levels wrote statistics in file "renf90.tables" Basic statistics for input data (missing value code is '0') Pos Min Mean SD Max N 2 1.0000 2.0000 1.5714 0.53452 7 3 10.000 14.000 12.286 1.4960 7 Correlation matrix 2 3 1.00 0.80 2 3 0.80 1.00 Counts of nonzero values (order as above) 7 7 7 7 random effect 2 type:animal opened output pedigree file "renadd02.ped" first 3 lines of the file (up to 70 characters) aa ff ee 2004 bb hh gg 2004 cc hh ii 2004 read 10 pedigree records loaded 4 parent(s) in round 1 Pedigree checks ee: younger than parent 1 by 0 years

```
gg: younger than parent 1 by
                                 0 years
Unknown parent group allocation
Equation Group
                       #Animals
                                 Years
                       0
                                          2001
      10
             1
                                   0-
      11
                       8
                                  2002-
               2
                                          2002
      12
                       1
                                  2003-
               3
Max group = 3; Max UPG ID = 12
Computations for inbreeding coefficients
Tiny negative value will be replaced with 0 considered as numerical error.
Wrote inbreeding file "renf90.inb" with original id
Inbreeding statistics:
the maximum inbreeding coefficient = 0.2500
average inbreeding for inbred animals = 0.2500
                                                n = 1
                      for all animals = 0.0278 n = 9
                  3
max upg
Number of animals with records
                                                            5
Number of parents without records
                                                =
                                                            4
Total number of animals
                                                            9
Wrote parameter file "renf90.par"
Wrote renumbered data "renf90.dat" 7 records
Wrote field information "renf90.fields" for 4 fields in data
```

#### Output data file - renf90.dat

#observation, effect 1, animal number, original animal ID
10 1 4 aa
12 2 4 aa
11 1 2 bb
12 1 5 cc
14 2 5 cc
13 2 3 dd
14 2 1 ee

#### Output pedigree file - renadd02.ped

```
Animal, sire, dam, inbreeding code (3-#unknown parents if no-inbreeding), birth year, #known
parents, #records, #progeny of sire, # progeny of dam, original animal ID
1 6 11 1333 2002 1 1 0 1 ee
2 8 7 2000 2004 2 1 0 0 bb
7 6 11 1333 2002 1 0 0 1 gg
3 6 12 1333 2004 1 1 0 0 dd
9 11 11 1000 2002 0 0 0 1 ii
4 6 1 2000 2004 2 2 0 0 aa
6 11 11 1000 2002 0 0 4 0 ff
5 8 9 2000 2004 2 2 0 0 cc
8 11 11 1000 2002 0 0 2 0 hh
```

Output parameter file - renf90.par # BLUPF90 parameter file created by RENUMF90 DATAFILE renf90.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS

```
2
OBSERVATION(S)
1
WEIGHT(S)
```

```
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT[EFFECT NESTED]
```

```
2 2 cross

3 12 cross

RANDOM_RESIDUAL VALUES

1.0000

RANDOM_GROUP

2

RANDOM_TYPE

add_an_upginb

FILE

renadd02.ped

(CO)VARIANCES

1.0000
```

#### Output tables after renumbering - renf90.tables

Effect group 1 of column 1 with 2 levels, effect # 1 Value # consecutive number 1 3 1 2 4 2

#### **Output tables after renumbering - renf90.fields**

field	variable or	igfield	group	colum	n random	effect	file
1	trait	3	0	0	*	cov	*
2	renumbered	2	1	1	*	cross	*
3	renumbered	1	2	1	animal	cross	renadd02.ped
4	passed	1	0	0	*	cov	*

#### Output tables after renumbering - renf90.inb

ee 0.000000 1 bb 0.000000 2 gg 0.000000 7 dd 0.000000 3 ii 0.000000 9 aa 0.250000 4 ff 0.000000 6 cc 0.000000 5 hh 0.000000 8

## When to use which program and computing limits

### **BLUP**

**BLUPF90** sets up equations in memory. It can support a few million equations with a simple model but fewer equations with complicated models (multiple traits, maternal effects, random regression, etc). BLUPF90 uses three solvers, chosen with options. Preconditioned conjugate gradient (PCG) is the default solver and is usually the fastest one. Successive over-relaxation (SOR) requires less memory but usually converges slower. Sparse Cholesky (FSPAK) is usually the most accurate method but uses the most memory. The following options are available:

#### OPTION conv\_crit 1e-12

Sets convergence criteria (default 1e-12).

#### **OPTION maxrounds 10000**

Sets maximum number of rounds (default 5000).

#### **OPTION solv\_method FSPAK**

Selection of solving method: FSPAK, SOR, or PCG (default PCG).

#### **OPTION r\_factor 1.6**

Sets relaxation factor for SOR (default 1.4). This factor helps speeding up convergence if the value is optimal; non-optimal values lead to poor convergence. It should be within [0,2].

#### **OPTION sol se**

Stores solutions and standard errors. If this option is used, the solving method will turn to FSPAK.

#### OPTION store\_pev\_pec 6

Stores triangular matrices of standard errors and its covariances for correlated random effects such as direct-maternal and random regression effects in "*pev\_pec\_bf90*".

#### **OPTION missing -999**

Specify missing observations in the data file. Must be an integer value (default is 0).

#### **OPTION blksize 3**

Sets block size for preconditioner (default 1) to accelerate convergence (usually 2 to 5 times faster). For a multi-trait model, use the number of traits. This option is extremely important to ensure convergence in multi-trait models.

#### **OPTION prior\_solutions**

The previous solution file will be used to start the iteration. Additional software is required to set up files correctly before using this option.

#### **OPTION stdresidual**

It stores y-hat and student residuals in "yhat\_student\_residual".

#### **OPTION check\_levels 0**

Check levels (default 1 = true).

#### **OPTION use\_yams**

Runs the program with YAMS (modified FSPAK). The computing time can be dramatically improved compared to using **solv\_method** FSPAK

#### **OPTION hetres\_int 5 10**

The position (5) to identify the interval in the data file and the number of intervals (10) for heterogeneous residual variances as used in GIBBS3F90.

#### **OPTION hetres\_var file**

Combined with **hetres\_int**, heterogeneous residual variances are read from **file**. The file has to contain residual (co)variances for each interval class.

#### **OPTION SNP\_file snp**

Specifies the SNP file name snp to use genotype data.

#### **OPTION** snp\_p\_value

Computes the elements of the inverse of the Mixed Model Equations that are needed for exact GWAS with p-values using postGSf90. This requires quite a lot of memory and time.

#### **OPTION omit\_ainv**

This causes the program to avoid computation of  $A^{-1}$ . It is especially useful for GBLUP. For example, the following options can be used:

OPTION omit\_ainv OPTION TauOmega 1.0 0.0 OPTION AlphaBeta 0.95 0.05

With that, the program does not compute  $A^{-1}$  but calculates  $\tau G^{-1} - \omega A_{22}^{-1}$ ; since  $\omega = 0$ , only  $G^{-1}$  will be included in the mixed model equations. **OPTION AlphaBeta 0.95 0.05** blends **G** with  $A_{22}$  as  $0.95G + 0.05A_{22}^{-1}$  before inversion.

## **BLUP90IOD2**

**BLUP90IOD2** uses an iteration on data algorithm. It can handle hundreds of millions of equations with complicated models in a reasonable time. However, it is only available based on a research agreement with UGA. The following options are available:

#### OPTION conv\_crit 1e-12

Sets convergence criteria (default 1e-12).

#### **OPTION maxrounds 10000**

Sets maximum number of rounds (default 5000).

#### **OPTION blksize 3**

Sets block size for preconditioner (default 1). The **blksize** number has to be the same as the number of traits for optimal performance.

#### OPTION init\_eq 10

Sets the number of effects to be solved directly (default 0).

#### OPTION solv\_method FSPAK

Solving method for initial equations (default DIRECT).

#### **OPTION tol 1d-12**

Tolerance to get a positive definite matrix (default 1d-12).

#### **OPTION residual**

y-hat and residuals will be included in "yhat\_residual".

#### **OPTION avgeps 50**

Using the last 50 average eps for convergence.

## **OPTION cont 1** Restarts the program from the previous solutions.

**OPTION missing -1** Sets the missing value (default 0).

## **OPTION restart 100** Sets the number of iteration to recompute residuals (default 100).

#### **OPTION prior\_solutions**

Using the previous solution file to start the iteration. Additional software is required to use this option.

## **OPTION random\_upg 1 2**

Sets the UPG random. "1" is the computational algorithm used; only algorithm 1 is implemented. "2" is the weight ( $\gamma$ ) for the group effects, the weight will be inverted (e.g., 1/2=0.5).

#### **OPTION SNP\_file snp**

Specifies the SNP file name snp to use genotype data.

#### **OPTION origID**

Stores solutions with the original ID. The output is *trait effect level original\_id solution*, and is stored in solutions.original. Be aware that this option may not in some programs.

## Variance components estimation

There is not a single best choice for variance component estimation. The programs below offer choices for simple and complicated models. For advice on what works best under your circumstances, check this paper "Reliable computing in estimation of variance components".

**REMLF90** uses expectation maximization (EM) REML. It is the most reliable algorithm for most problems but can take hundreds of rounds of iterations. REMLF90 was found to have problems converging with random regression models. In this case, using starting variances that are too large than too small usually helps. Also, EM does not calculate standard errors for the estimates. The following options are available:

**OPTION conv\_crit 1d-12** Convergence criterion (default 1d-12).

**OPTION maxrounds 10000** Maximum rounds (default 5000).

**OPTION sol se** Stores solutions and standard errors (se).

**OPTION residual** y-hat and residuals will be included in "yhat residual".

#### **OPTION missing -999**

Specifies missing observations (default 0). This is only for data, not pedigree (always 0 for missing pedigrees). There is no missing covariable, so 0 is treated as a level.

#### **OPTION constant\_var 5 1 2**

5: effect number, 1: first trait number, 2: second trait number implying the covariance between traits 1 and 2 for effect 5 is fixed.

#### **OPTION SNP\_file snp**

Specifies the SNP file name **snp** to use genotype data.

#### **OPTION use\_yams**

Run the program with YAMS (modified FSPAK). The computing time can be dramatically improved.

**AIREMLF90** uses Average Information (AI) REML. It usually converges much faster but sometimes does not converge. Very slow convergence usually indicates that the model is over parameterized, and there is

insufficient information to estimate some variances. AI REML calculates standard errors for the estimates. The following options are available:

OPTION conv\_crit 1d-12

Convergence criterion (default 1d-12).

#### **OPTION maxrounds 500**

Maximum rounds (default 5000). When it is zero, the program calculates BLUP without running REML.

**OPTION EM-REML 10** Runs EM-REML for the first 10 rounds to get initial variances within the parameter space (default 0).

**OPTION tol 1d-18** Tolerance (or precision) for positive definite matrix and G-inverse subroutines (default 1d-14).

**OPTION sol se** Stores solutions and standard errors (se).

**OPTION missing -1** Sets the missing observation (default 0).

#### OPTION constant\_var 5 1 2

5: effect number, 1: first trait number, 2: second trait number implying the covariance between traits 1 and 2 for effect 5 is fixed.

#### **OPTION use\_yams**

Runs the program with YAMS (modified FSPAK). The computing time can be dramatically improved.

#### **OPTION fact\_once memory**

Saves the Cholesky factor of LHS in memory. It greatly improves the computing time instead of memory consumption.

#### **OPTION fact\_once file**

Saves Cholesky factor of LHS in a temporary file. It improves the computing time without extra memory.

#### **OPTION approx\_loglike**

Skips the exact computation of log-likelihood. It would improve the computing time.

## **OPTION store\_pev\_pec 6**

Stores standard errors and its covariances for correlated random effects such as direct-maternal and random regression effects in "*pev\_pec\_bf90*".

#### **OPTION** residual

y-hat and residuals will be included in "yhat\_residual".

#### Heterogeneous residual variances for a single trait

#### OPTION hetres\_pos 10 11

Specifies the positions of covariables.

#### OPTION hetres\_pol 4.0 0.1 0.1

Initial values of coefficients for heterogeneous residual variances. Use In(a0, a1, a2, ...) to make these values. When the number of positions = the number of polynomials, the regressions do not include the intercept (e.g., linear spline).

#### Heterogeneous residual variances for multiple traits (the convergence will be very slow)

#### **OPTION** hetres\_pos **10 10 11 11**

Specifies positions of covariables (trait first).

#### OPTION hetres\_pol 4.0 4.0 0.1 0.1 0.01 0.01

Initial values of coefficients for heterogeneous residual variances using ln(a0, a1, a2, ...) to make these values (trait first). "4.0 4.0" are the intercept for first and second traits. "0.1 0.1" could be linear and "0.01 0.01" could be quadratic. To transform back to the original scale, use exp(a0+a1\*X1+a2\*X2).

#### **OPTION SNP\_file snp**

Specifies the SNP file name **snp** to use genotype data.

#### Standard deviations for (co)variance functions including heritability

#### **OPTION** se\_covar\_function label function

Calculates SD for (co)variance functions by repeated sampling of parameter estimates from their asymptotic multivariate normal distribution, following idea presented by Meyer and Houle 2013. For details, see documentation at http://nce.ads.uga.edu/wiki/doku.php?id=readme.airemI.

#### **OPTION** samples\_se\_covar\_function **x**

This allows the user to set the number of samples to calculate the standard error for functions of (co)variance components (default value is 10000).

**GIBBSxF90** programs implement Bayesian methods. These methods potentially have better statistical properties. Also, they are more stable and use less memory for complicated models. After running any of the Gibbs sampling programs, samples can be analyzed (posterior means, SD, and convergence parameters) with the POSTGIBBSF90 program.

In practical cases, results from Gibbs samplers and REML are similar. Choose one or the other based on computing feasibility. If there are large differences beyond sampling errors, this indicates problems usually with the Gibbs sampler. Try longer chains or different priors.

Gibbs samplers may be slow to achieve convergence if initial values are far away from those at convergence, e.g., 100 times too low or too high. Before using more complicated models, Karin Meyer advocates using a series of simpler models.

**GIBBS1F90** can run models with over 20 traits. However, if models are different per trait, the lines due to effects need to be modified. Also, with too many differences in models among traits, the program becomes increasingly slower.

**GIBBS2F90** adds joint sampling of correlated effects. This results in faster mixing with random regression and maternal models. Memory requirements and CPU time per round are somewhat higher than in gibbs1f90.

Interactive inputs:

#### number of samples and length of burn-in?

In the first run, if you have no idea about the number of samples and burn-in, just type your guess (10000 or whatever) for samples and (0) for burn-in. You may need 2 or 3 runs to figure out the convergence.

#### Give **n** to store every n-th sample?

Gibbs samples are highly correlated, so you do not have to keep all samples (every 10th, 20th, 50th, ...).

The following options are available for GIBBSxF90:

#### OPTION fixed\_var all 1 2 3

Stores all solutions and posterior means and SD for effects 1, 2, and 3 are stored in "all\_solutions" and in "final\_solutions" every round using fixed variances. Without numbers, all solutions for all effects are stored.

#### OPTION fixed\_var mean 1 2 3

Posterior means and SD for effects 1, 2, and 3 in "final\_solutions" using fixed (known) variances.

#### **OPTION solution all 1 2 3**

Stores all solutions and posterior means and SD for effects 1, 2, and 3 in "all\_solutions" and in "final\_solutions" every round. Without numbers, all solutions for all effects are stored. Caution: this option will create a huge output solution file when you run many rounds and/or use a large model.

#### **OPTION** solution mean **1 2 3**

Posterior means and SD for effects 1, 2, and 3 are stored in "final\_solutions".

#### **OPTION cont 10000**

10000 is the number of samples run previously when restarting the program from the last run.

#### OPTION prior 52-15

The (co)variance priors are specified in the parameter file. Degree of belief for all random effects should be specified using the following structure:

OPTION prior eff1 db1 eff2 db2 ... effn dbn -1 dbres; where effx corresponds to the effect number and dbx to the degree of belief for this random effect, -1 corresponds to the degree of belief of the residual variance. In this example, 2 is the degree of belief for the 5th effect, and 5 is the degree of belief for the residual.

#### OPTION seed 123 321

Two seeds for a random number generator can be specified.

#### **OPTION SNP\_file snp**

Specifies the SNP file name **snp** to use genotype data.

**GIBBS3F90** adds estimation of heterogeneous residual covariances in classes. The computing costs usually increase with the number of classes.

#### **OPTION hetres\_int 5 10**

The position (5) to identify the interval in the data file and the number of intervals (10) for heterogeneous residual variances.

Other options are the same as for **GIBBS1F90** and **GIBBS2F90**. For **fixed\_var all** or **fixed\_var mean**, heterogeneous residual variances are read from a file 'hetres'. This file name cannot be changed.

**THRGIBBS1F90** is a Gibbs sampling program to analyze categorical and continuous traits simultaneously; categorical traits can be censored. The following options are available:

#### OPTION cat 0 0 2 5

"0" indicates that the first and second traits are linear. "2" and "5" indicate that the third and fourth traits are categorical with 2 (binary) and 5 categories.

#### OPTION thresholds 0.0 1.0 2.0

Set the fixed thresholds. No need to set 0 for binary traits.

**OPTION residual 1** Set the residual variance = 1.

**OPTION save\_halfway\_samples 5000** 

The program saves every "5000" samples to restart or recover the job right after the last saved samples. It is useful when the program accidentally stopped.

#### **OPTION censored 10**

Negative values of the last category in the data set indicate censored records. "1 0" determines that the first categorical trait is censored, and the second categorical trait is uncensored.

#### **OPTION pos\_def x.x**

This specifies the tolerance x.x (default = 1d-08) for checking post-def for fixed effects.

Using the following options for ordered categorical data with right censored records:

## OPTION cat 0 0 2 5 OPTION censored 1 0

The data file may look like

traits:	1	2	3	4
	1.71	11.1	1	1
	2.22	15.2	0	5
	3.29	16.4	2	1
	1.95	14.7	1	3
	2.25	20.8	-2	4
	3.64	19.2	1	5
	1.99	13.3	-1	2

Columns 1 and 2 are observations for linear traits and columns 3 and 4 are traits for 2 categories (binary) with censored records (negative values) and 5 categories.

Other options are the same as for GIBBS1F90 and GIBBS2F90.

**THRGIBBS3F90** works as THRGIBBS1f90 but with the estimation of heterogeneous residual covariances in classes as described for GIBBS3F90.

**POSTGIBBSF90** is a program to calculate posterior means and SD and diagnose the convergence of the Gibbs chain. The program reads "gibbs\_samples" and "fort.99" files from Gibbs sampling programs.

Read 1000 samples from round 10 to 10000

## Burn-in?

1000 # in the first run, type 0 for burn-in to include all samples.

#### Give n to read every n-th sample? (1 means read all samples)

10# Type the same number used with a Gibbs sampling program.# You should not type 1 unless you have typed 1 in the Gibbs sampling program.

#### # samples after burn-in = 9000

#### Input files:

gibbs\_samples, fort.99, and other files used in a parameter file from (THR)GIBBSxF90 Output files:

postgibbs\_samples, postout, postmean, postsd

#### postgibbs\_samples

A text file containing all Gibbs samples from **gibbs\_samples** for other software (EXCEL, SAS, R, ...) to calculate posterior means and SD, and to create graphs.

#### postmean

Posterior means

#### postsd

Posterior standard deviations

#### postout

					*****	Monte	Carlo	E	rror by	<b>Time Series</b>	******		
Pos.	eff1	eff2	trt1	trt2	мс	E Meai	n	н	PD	Effective	e Median	Mode	Independent
								Inter	val (95%)	sample size	9		chain size
1	4	4	1	1	1.362E-0	0.988	9 0	.7788	1.215	5 70.4	4 0.9844	0.9861	18
2	4	4	1	2	1.288E-0	1.00	6	0.777	1.219	84.:	1.006	0.952	18
3	4	4	2	2	1.847E-0	1.6	6	1.347	1.987	80.3	3 1.652	1.579	25
4	0	0	1	1	9.530E-0	3 24.4	7 :	24.07	24.84	425.6	5 24.47	24.53	2
5	0	0	1	2	8.253E-0	3 11.84	4	11.54	12.18	395.8	8 11.83	11.82	2
6	0	0	2	2	1.233E-0	30.:	1 :	29.65	30.58	387.8	30.09	29.97	5

#### \*\*\*\*\*\*\*\* Posterior Standard Deviation \*\*\*\*\*\*\*

Pos. eff1 eff2 trt1 trt2		rt2	PSD	Mean	PSD		Geweke	A	utocorrel	Independent			
							Interv	val (95%)	diagnostic	lag: 1	10	50	# batches
1	4	4	1	1	0.1144	0.9889	0.7648	1.213	-0.02	0.853	0.188	0.049	50
2	4	4	1	2	0.1182	1.006	0.7742	1.237	-0.11	0.828	0.111	-0.066	50
3	4	4	2	2	0.1656	1.66	1.335	1.984	0.06	0.828	0.108	-0.021	36
4	0	0	1	1	0.1967	24.47	24.09	24.86	-0.01	0.034	0.029	-0.062	450
5	0	0	1	2	0.1643	11.84	11.51	12.16	0.03	0.032	-0.006	-0.016	450
6	0	0	2	2	0.2429	30.1	29.62	30.57	-0.02	0.07	-0.014	0.037	180

where

"Pos."

position of each parameter in the parameter file. "eff1" and "eff2" effect number in the parameter file.

"trt1" and "trt2"

trait number in the parameter file (0 for residual).

"MCE"

Monte Carlo Error.

"Mean"

posterior means.

"HPD interval (95%)"

95% Highest Probability Density.

"Effective sample size"

at least > 10 is recommended; > 30 may be better.

"Median"

median of Gibbs samples.

"Mode"

when the distribution of the samples is not normal, "Mean" and "Mode" could be different. "Independent chain size"

number of independent cycles of Gibbs samples.

"PSD"

Posterior Standard Deviation.

"PSD interval (95%)"

95% Posterior Standard Deviation interval.

"Geweke diagnostic"

the ratio between the first and second halves of the samples should be < 1.0, but it may not be helpful because it is < 1.0 most of the time.

"Autocorrelations"

autocorrelations between two lags. High correlation implies samples are not independent. "Independent # batches"

**Hint 1:** when eff1, eff2, trt1, trt2 are all -1, the values presented are for thresholds (if THRGIBBSXF90 is used).

Choose a graph for samples (= 1) or histogram (= 2); or exit (= 0)

1

positions

123 # choose from the position numbers 1 through 6


If the graph is stable (not increasing or decreasing), the convergence is met. All samples before that point should be discarded as burn-in.

print = 1; other graphs = 2; or stop = 0
2
Choose a graph for samples (= 1) or histogram (= 2); or exit (= 0)
2
Type position and # bins
1 20



The distribution should be usually normal (Mean = Mode = Median).

```
print = 1; other graphs = 2; or stop = 0
0
**** Log Marginal Density for Bayes Factor ***
after 900 burn-in
log(p) = -179448.742766031
```

This value could be used when calculating Bayes Factor and/or DIC.

# **Combined programs**

## BLUPF90+

This software combines BLUPF90, REMLF90, and AIREMLF90. Therefore, it can take options used in each of these programs.

It has some new features such as the computation of reliabilities of (G)EBV based on PEV, and the ability to save solutions with original ID.

The default of this software is to run BLUP, unless variance components estimation options are used.

Hint: type blupf90+ --help to see all the BLUPF90+ options

or blupf90+ --help-genomic to see genomic options BLUPF90+ can take.

Specific options

# **OPTION method VCE**

Runs AIREMLF90 for variance component estimation.

## **OPTION EM-REML X**

Runs EM-REML (REMLF90) for first x rounds to get initial variances within the parameter space. After 100 rounds, it will switch to AI-REML (AIREMLF90) and continue until convergence. If the program converges within 100 rounds, it will show only the results from AI-REML

Examples:

OPTION EM-REML n

....Runs AI rounds until convergence or x after n EM rounds, showing AI output

**OPTION EM-REML or OPTION EM-REML pure** 

....Runs EM until convergence or x, showing EM output, which is equivalent to REMLF90

OPTION EM-REML AI or ai

....Runs EM until convergence and then switches to AI rounds until AI convergence or x, showing AI output

## **OPTION store\_accuracy eff**

Stores reliabilities based on PEV, where eff is the number of the animal effect. By default, it uses inbreeding (F) in the denominator of the reliability formula: reliability =  $1-\text{PEV}/(\sigma_u^2 (1+F))$ . It uses inbreeding based on the relationship matrix that is being used in the mixed model equations.

## **OPTION acctype 1.0**

Select 1.0 for dairy cattle (Reliability) or 0.5 for beef cattle (BIF accuracy) (default 1.0).

# **OPTION correct\_accuracy\_by\_inbreeding filename**

*filename* is the name of the inbreeding file if other than renf90.inb

#### OPTION correct\_accuracy\_by\_inbreeding\_direct 0

This option turns off the inbreeding correction in the reliability formula.

#### **OPTION origID**

Stores solutions with the original ID. The output is *trait effect level original\_id solution*, and is stored in solutions.original.

#### **OPTION store\_accuracy eff orig**

Stores reliabilities based on PEV, where **eff** is the number of the animal effect, and **orig** should be used to output reliabilities with original ID. Combine with OPTION origID if solutions should also be output with original ID. The resulting file, acc\_bf90, contains: trait, effect, level, original\_ID, solutions, reliabilities.

## OPTION set\_eig 1d-12

It allows to set a tolerance (or precision) for positive definite matrix and g-inverse subroutines (default is 1d-18).

Click here for more details on BLUPF90+

## GIBBSF90+

This software combines GIBBS1F90, GIBBS2F90, GIBBS3F90, THRGIBBS1F90, and THRGIBBS3F90. It takes any options from the above Gibbs programs. Click **here** for more details on GIBBSF90+

## **Genomic programs**

#### PREGSF90

PreGSF90 is an interface program to the genomic module to process the genomic information for the BLUPF90 family of programs. This software performs quality control of genomic data and constructs and inverts the genomic relationship matrix (**G**) and the pedigree relationship matrix for genotyped animals ( $A_{22}$ ). When the inverse of the relationship matrix based on the pedigree information (**A**) in the mixed model equations is replaced by the inverse of the realized relationship matrix (**H**), which combines pedigree and genomic information, BLUP becomes single-step GBLUP (**ssGBLUP**). The main difference between  $A^{-1}$  and  $H^{-1}$  is the structure of  $G^{-1} - A_{22}^{-1}$  added for the genotyped animals. Some of the options for **PREGSF90** can be also used with **BLUPF90**, (**AI**)**REMLF90**, **GIBBS1F90**, **GIBBS2F90**, **GIBBS3F90**, **THRGIBBS1F90**, **BLUPF90+**, **GIBBSF90+**, **BLUP90IOD2**, and **BLUP90IOD3**.

## Input files

## **OPTION SNP\_file <file>**

This option invokes the genomic routine in the application programs. The SNP file should contain Field 1 - animal ID with the same format as in pedigree file

Field 2 - genotypes with 0, 1, 2, and 5 (missing) or real values for gene content (or genotype probability) 0.120.890.54 (i.e., 0.12 0.89 0.54 without spaces). Be aware that some quality control steps are turned off when using genotype probabilities.

Two Fields (animal ID and SNP) need to be separated by at least one space, and Field 2 should have fixed format (i.e., all rows of genotypes should start at the same column number or position).

 80
 2110101100201201101101101111111211111210100
 8014

 8014
 21110101511101120221110111511112101112210100

 516
 21100101202252021120210121102111202212111101

 181
 2111011111220112055020002010102221221111100

The renumbered ID file for genotypes named after the genotype file, e.g., **file\_XrefID**, is created by RENUMF90 (using the SNP file), containing the renumbered ID and the original ID, which follows the same order as in the SNP file:

1732 80 8474 8014 406 516 9441 181

The pedigree file from RENUMF90 looks like:

17321101010584131210080847486919908131210080144068691982513121025169441869188291312100181

Map file for SNP can be used as optional:

**OPTION map\_file <file>**: reads SNP map information from the file.

The file should have a header with the following column names:

SNP\_ID #identification of the SNP (alphanumeric)

CHR #chromosome number (numeric), starting from 1

POS #position bp (numeric)

Extra columns are possible (optional).

The first SNP in the Map file corresponds to the first SNP in the genotype file, and so on.

Example:

SNP\_ID CHR POS

- 1 1 1201
- 2 1 8004 3 1 12006
- 4 1 16008

The map file is useful to check for Mendelian conflicts and HWE (with also **OPTION sex\_chr**) and for **POSTGSF90** (ssGWAS).

With other options, the program can read G or its inverse, A<sub>22</sub> or its inverse, etc.

# **Output files**

By default, PREGSf90 runs quality control and creates GimA22i in binary format for use by other

application programs, specifying **OPTION readGimA22i**. With **OPTION saveAscii**, this file can be stored as ASCII format: i, j,  $\mathbf{G}^{-1} - \mathbf{A}_{22}^{-1}$ .

"freqdata.count" contains allele frequencies in the original genotype file with the format: SNP number (related to the genotype file) and allele frequency as mentioned above.

"freqdata.count.after.clean" contains allele frequencies as used in calculations with the format: SNP number (related to the genotype file), allele frequency, and exclusion code. Exclusion codes:

Call Rate
 MAF
 Monomorphic
 Excluded by request
 Mendelian error
 HWE
 High Correlation with other(s) SNP

"Gen\_call\_rate" contains a list of animals excluded with call rate below the threshold.

"Gen\_conflicts" contains a report of animals with Mendelian conflicts with their parents.

The program can store files such as **G** or its inverse,  $A_{22}$  or its inverse, or other reports from QC as specified by their respective OPTIONs.

Options for creating the genomic relationship Matrix (G)

The genomic relationship matrix, **G**, can be created in different ways.

# **OPTION** whichG **x**

Specifies how **G** is created.

The variable x can be

1: 
$$\mathbf{G} = \frac{\mathbf{Z}\mathbf{Z}'}{k}$$
; VanRaden, 2008 (default)  
2:  $\mathbf{G} = \frac{\mathbf{Z}\mathbf{D}\mathbf{Z}'}{n}$ ; Amin et al., 2007; Leuttenger et al., 2003; where  $\mathbf{D} = \frac{1}{2p(1-p)}$ 

3: As 2 with modification UAR from Yang et al., 2010

# **OPTION** whichfreq **x**

Specifies which frequency is used for centering Z to create G.
The variable x can be
0: read from file "freqdata" or from the other file using OPTION FreqFile

1: 0.5

2: current calculated from genotypes (default)

# **OPTION** whichfreqScale **x**

Specifies which frequency is used to scale **G**. This can be applied to use different allele frequencies to center and scale **G**. The variable x can be:

0: read from file as specified using **OPTION FreqFile** 

1: 0.5

2: current calculated from genotypes (default)

# **OPTION FreqFile <file>**

Reads allele frequencies from a file. For example, based on allele frequencies calculated by estfreq.f90 (VanRaden, 2009) with format:

Field 1 – SNP number (sequential marker number)

Field 2 – allele frequency as a real value from 0 to 1

Example:

1 0.525333 2 0.293667 3 0.448333 4 0.510667

where SNP corresponds to the index of SNP based on the same order as in the genotype file. If whichfreq is set to 0, the default file name is "freqdata".

# **OPTION whichScale x**

Specifies how **G** is scaled.

The variable **x** can be

1:  $2\sum \{p(1-p)\}$ ; VanRaden, 2008 (default)

2:  $\frac{tr(\mathbf{ZZ'})}{n}$ ; Legarra, 2009, Hayes, 2009

3: correction; Gianola et al., 2009

# **OPTION weightedG <file>**

Reads weights from a file to create weighted genomic relationships. With weights,  $Z^* = Z \operatorname{sqrt}(D) \Rightarrow \mathbf{G} = Z^*Z^{*'} = ZDZ'$ . Format:

Field 1 – weight Example: 0.7837836E-01 0.4900770E-01 0.7538282 1.0 Each weight corresponds to each SNP marker defined in the map file.

Weights can be extracted from the output of **POSTGSF90**.

#### **OPTION maxsnp x**

Sets the maximum length of string to read marker data from a file. It is only necessary if greater than default (400,000).

# Quality Control (QC) for G

By default the following QC can be run: MAF Call rate (SNPs and animals) Monomorphic Parent-progeny conflicts (SNPs and animals)

Parameters can be modified with the following options:

## **OPTION** minfreq **x**

Ignores all SNP with MAF < x (default value = 0.05).

## **OPTION** callrate **x**

Ignores SNP with call rates < x (number of calls / number of individuals with genotypes). The default value is 0.90.

## **OPTION callrateAnim x**

Ignores genotypes with call rates < x (number of calls / number of SNPs). Default value is 0.90.

## **OPTION** monomorphic **x**

Ignores monomorphic SNPs. Optional parameter x can be used to enable (1) or disable (0) the check. The default value is 1.

## **OPTION hwe x**

Checks departure of heterozygous from Hardy-Weinberg equilibrium. By default, this QC is not run. The optional parameter x can be the maximum difference between observed and expected frequency (default value = 0.15) as used in Wiggans et al. (2009) in JDS.

## **OPTION** high\_correlation **x y**

Checks for highly correlated SNP. By default, this QC is not run. The optional parameter x can be the maximum difference in allele frequency to check a pair of loci. If no value is set, 0.025 is used. Decrease this value to speed up the calculation. A pair of loci is considered highly correlated if all genotypes are the same (0-0, 1-1, 2-2) or the opposite (0-2, 1-1, 2-0) (Wiggans et al., 2009. JDS). The optional parameter y can be used to set a threshold to check the number of identical samples out of the number of genotypes (default values: x=0.025, y=0.995).

## **OPTION verify\_parentage x**

Verifies parent-progeny Mendelian conflicts and writes a report into the "Gen\_conflicts" file. The optional parameter x can be

0: no action

1: only detects

2: detects and searches for an alternate parent; no change to any file. This option is implemented in the **SeekParentF90** program.

3: detects and eliminates progenies with conflicts (default).

## **OPTION exclusion\_threshold x**

Sets the number of parent-progeny exclusions as percentage. All SNP are used to determine wrong relationships (default value = 2).

## **OPTION** exclusion\_threshold\_snp x

Sets the number of parent-progeny exclusions for each locus as percentage. A pair of genotyped animals is evaluated to exclude SNP from the analysis (default value = 10).

#### **OPTION number\_parent\_progeny\_evaluations x**

Sets the number of minimum pair of parent-progeny evaluations to exclude SNP due to parent-progeny exclusion (default value = 100).

#### **OPTION outparent\_progeny x**

Creates a full log file "Gen\_conflicts\_all" with all pairs of parent-progeny tested for Mendelian conflicts.

## OPTION excludeCHR n1 n2 n3 ...

Excludes all SNP from chromosomes n1, n2, n3, ... A map file must be provided (see **OPTION map\_file**).

#### OPTION includeCHR n1 n2 n3 ...

Include all SNP from chromosomes n1, n2, n3, ... A map file must be provided (see OPTION map\_file).

## OPTION excludeSample n1 n2 n3 ...

Exclude genotype samples n1, n2, n3, ... Where n1, n2, n3, ... are row number of individuals in the genotype file.

#### OPTION sex\_chr n

Chromosomes with a number greater or equal to n are not considered as autosomes. If this option is used, sex chromosomes will not be used for checking parent-progeny, Mendelian conflicts, and HWE. A map file must be provided (see **OPTION map\_file**).

#### **OPTION threshold\_duplicate\_samples x**

Sets the threshold to issue warning for possible duplicate samples if G(i,j) / sqrt(G(i,i) \* G(j,j)) > x (default value = 0.9).

#### **OPTION** high\_threshold\_diagonal\_g x

Checks for extremely large diagonals in the genomic relationship matrix. If optional x is present, the threshold will be set (default value = 1.6).

#### **OPTION low\_threshold\_diagonal\_g x**

Checks for extremely low diagonals in the genomic relationship matrix. If optional x is present, the threshold will be set (default value = 0.7).

#### **OPTION plotpca print/noprint**

Plots the first two principal components to look for stratification in the population. With noprint the program will save the first two principal components of **G** without showing the PCA plot on the screen; otherwise, (print) it will print on the screen.

#### OPTION extra\_info\_pca <file> col

Reads the column col to plot with different colors for different classes from the file. The file should contain at least one variable with different classes for each genotyped individual, and the order should match the order of the genotype file. Variables could be alphanumeric and separated by one or more spaces.

## **OPTION calculate\_LD**

Calculates LD as the squared correlation of allele counts for two SNP. Results are stored in "ld\_results", columns: snp\_i, chr\_i, pos\_i, freq\_i, snp\_j, chr\_j, pos\_j,freq\_j, dist\_ij, Rsq\_ij

## OPTION LD\_by\_chr

Calculates LD within chromosome.

#### OPTION LD\_by\_pos x

Calculates LD within chromosome and windows of SNP based on position. Optional parameter x defines with windows size in Bp, default value 200000

## **OPTION filter\_by\_LD x**

Filters SNP with Rsq > threshold. Optional parameter x define the threshold. default value 0.8

#### **OPTION thr\_output\_LD x**

Threshold to print out Rsq between pair of SNP Optional parameter x define the threshold. default value 0.1

#### **OPTION saveCleanSNPs \***

Saves clean genotype data with excluded SNP and animals based on the OPTIONS specified.

- \*\_clean files are created:
- gt\_clean
- gt\_clean\_XrefID

- \*\_removed files are created:
- gt\_SNPs\_removed
- gt\_Animals\_removed

where "gt" is the genotype file.

## **OPTION no\_quality\_control**

Turns off all quality control. It speeds up computations when the QC was previously performed.

## **OPTION outcallrate**

Prints all call rate information for SNP and individuals. The files "callrate" for SNP and "callrate\_a" for individuals are created.

## **OPTION h2\_gene\_content**

This allows to check if the heritability of gene content is equal to 1.00 as described in Forneris et al. (2015). Markers whose estimated heritability is < 0.98 and significant p-value for the LRT (p < 0.01) will be removed, and a file "h2\_gc\_test" will be created with heritability and status of each marker. The test is useful for homogenous populations (breeds) but theory does not hold for crossbred animals. This test uses explicitly inv( $A_{22}$ ) so it is not suitable for very large populations.

Quality Control for Off-diagonal of  $A_{22}$  and G

# **OPTION thrWarnCorAG x**

Sets the threshold to issue warning if correlation between  $A_{22}$  and G < x (default value = 0.5).

## **OPTION thrStopCorAG x**

Sets the threshold to stop the analysis if correlation between  $A_{22}$  and G < x (default value = 0.3).

# **OPTION thrCorAG x**

Sets the threshold to calculate correlation between  $A_{22}$  and G for only  $A_{22} \ge x$  (default value = 0.02).

Options for **H** 

The options includes different weights to create  $\mathbf{G}^{-1}-\mathbf{A}_{22}^{-1}$  as

$$\tau(\alpha \mathbf{G} + \beta \mathbf{A_{22}} + \gamma \mathbf{I} + \delta \mathbf{11'})^{-1} - \omega \mathbf{A}_{22}^{-1}$$

where the parameters are to scale the genomic information to be compatible with the pedigree information, to make matrices invertible in the presence of clones, and to control bias. The default values are: tau ( $\tau$ ) = 1, alpha ( $\alpha$ ) = 0.95, beta ( $\beta$ ) = 0.05, gamma ( $\gamma$ ) = 0, delta ( $\delta$ ) = 0, and omega ( $\omega$ ) = 1. Options to change these defaults are specified with:

## **OPTION TauOmega tau omega**

# OPTION AlphaBeta alpha beta OPTION GammaDelta gamma delta

**Hint:** OPTION TauOmega was needed when inbreeding was not considered for  $A^{-1}$ . Because inbreeding is now considered for  $A^{-1}$ , we recommend not using this option anymore.

# **OPTION** tunedG **x**

Scales G based on A<sub>22</sub>. The variable x can be:
0: no scaling
1: mean(diag(G))=1 and mean(offdiag(G))=0
2: mean(diag(G))=mean(diag(A<sub>22</sub>)) and mean(offdiag(G))=mean(offdiag(A<sub>22</sub>)) (default)
3: mean(G)=mean(A<sub>22</sub>)
4: rescale G using the first adjustment as in Powell et al. (2010) or Vitezica et al. (2011).

# Options to extract the diagonal of H

The diagonal of **H** contains an improved estimator of inbreeding:  $F_H = diag(\mathbf{H}) - 1$ . For genotyped animals,  $F_H = F_G$  (because  $diag(\mathbf{H}) = diag(\mathbf{G})$ ). For non-genotyped animals  $diag(\mathbf{H})$  also includes pedigree-based estimates of genomic inbreeding. To extract  $diag(\mathbf{H})$  the following options can be used:

# **OPTION saveDiagH**

It outputs the diagonal of **H** with renumbered id's.

# **OPTION** saveDiagHOrig

It outputs the diagonal of **H** with original and renumbered id's.

The user can choose one of two equivalent methods:

# OPTION methodDiagH 1 OPTION methodDiagH 2

**OPTION methodDiagH 1** does a sparse inversion of  $\mathbf{H}^{-1}$  (default) which is very fast for medium size pedigrees. **OPTION methodDiagH 2** uses the third method described in Legarra et al. (2019) to compute  $\mathbf{M} = \mathbf{A}_{22}^{-1}(\mathbf{G} - \mathbf{A}_{22})\mathbf{A}_{22}^{-1}$ . This method is **recommended** for large pedigrees. The output depends on the used method. Method 1 shows only individual id and  $diag(\mathbf{H})$  and method 2 outputs individual id and the values of  $diag(\mathbf{H})$  and  $diag(\mathbf{A})$ , and the difference  $diag(\mathbf{H}) - diag(\mathbf{A})$ .

# General control of PREGSF90

# **OPTION num\_threads\_pregs n**

Specifies number of threads to be used with MKL-OpenMP for creation and inversion of matrices.

#### **OPTION num\_theads\_iod n**

Specifies number of threads to be used with MKL-OpenMP in BLUP90IOD for matrix-vector multiplications in the PCG algorithm.

#### **OPTION graphics s**

Allows to generate plots with GNUPLOT. If optional parameter s is present, set the time in seconds to show the plot. Avoid using in batch programs!!!

## **OPTION msg x**

Sets the level of verbose; 0 minimal; 1 prints lots of diagnostics on the screen.

Save and Read options:

#### **OPTION saveAscii**

Saves intermediate matrices (GimA22i, G, Gi, etc.) into files as ASCII (default = binary).

## **OPTION saveHinv**

Saves **H**<sup>-1</sup> in "Hinv.txt" (format: i, j, val; where i, j, are the index level for the additive genetic effect).

#### **OPTION saveAinv**

Saves  $A^{-1}$  in "Ainv.txt" (format: i, j, val; where i, j, are the index level for the additive genetic effect).

The following options use the information of the original ID (alphanumeric) stored in the 10th column of the "renaddxx.ped" file created by **RENUMF90**.

#### **OPTION saveHinvOrig**

Saves  $\mathbf{H}^{-1}$  with original IDs

**OPTION saveAinvOrig** Saves **A**<sup>-1</sup> with original IDs

#### **OPTION saveDiagGOrig**

Saves diagonal of **G** in "DiagGOrig.txt" (format: id, val; where id is the original ID).

## **OPTION saveGOrig**

Saves **G** in "G\_Orig.txt" (format: id\_i, id\_j, val; where id\_i and id\_j are the original IDs).

#### **OPTION saveA22Orig**

Saves A<sub>22</sub> in "A22\_Orig.txt" (format: id\_i, id\_j, val; where id\_i and id\_j are the original IDs).

#### **OPTION readOrigId**

Reads information from "renaddxx.ped" file, original ID, and possibly year of birth for its use in parent-

progeny conflict. Only needed if none of the previous "save\*Orig" is present.

#### **OPTION saveGimA22iRen**

Saves GimA22i matrix in GimA22i\_Ren.txt (format: id\_i, id\_j, val; where id\_i and id\_j are the IDs as stored in the first column of renaddXX.ped).

#### **OPTION saveGimA22iOrig**

Saves GimA22i matrix in GimA22i\_Orig.txt (format: id\_i, id\_j, val; where id\_i and id\_j are the IDs as stored in the original pedigree file and in column 10 of renaddXX.ped).

#### **OPTION savePLINK**

Saves genotypes in PLINK format files: toPLINK.ped and toPLINK.map.

#### **OPTION no\_full\_binary**

Saves the elements of half-matrix instead of the full matrix. It is useful to keep the compatibility with the older versions of preGSf90. The newer versions save the matrix in a more efficient way, where reading the information from the binary file is not trivial (i.e., not as *i*, *j*, *val* anymore).

The following options are used to save and read intermediate files:

#### OPTION readGimA22i <file>

Reads  $\mathbf{G}^{-1} - \mathbf{A}_{22}^{-1}$  from a file. This option can be used in the application programs (BLUPF90, REMLF90, etc.) to use the information already stored in the GimA22i file (default filename). In general, methods used to create and invert matrices in such programs do not use an optimized version. For a large number of genotyped animals, run first PREGSf90 and read stored matrices in the application programs.

The optional file can be used to specify a different file name (other than GimA22i) or a path. For example,

## OPTION readGimA22i ../../pregsrun/GimA22i

Other intermediate matrices files can be stored for inspection or for use in BLUPF90 programs as **user\_file** type of random effect. See **tricks** and **REMLF90** for details.

Individual output options:

#### **OPTION saveA22**

Saves  $A_{22}$  in "A22".

# **OPTION saveA22Inverse**

Saves  $\mathbf{A}_{22}^{-1}$  in "A22i".

#### **OPTION saveA22InverseOrig**

Saves  $A_{22}^{-1}$  with original id's (format id\_i, id\_j, and value).

### **OPTION saveG all**

If optional all is present, all intermediate matrices for **G** will be saved in separate files. If omitting all, only the final **G** will be saved in "G".

## **OPTION saveGInverse**

Saves  $\mathbf{G}^{-1}$  in "Gi".

## **OPTION saveGInverseOrig**

Saves  $\mathbf{G}^{-1}$  with original id's (format id\_i,id\_j, and value).

## **OPTION saveGmA22**

Saves  $\mathbf{G} - \mathbf{A}_{22}$  in "GmA22". This option is obsolete.

#### OPTION readG <file>

Reads **G** from "G" by default, or from a user-supplied **file**.

# **OPTION readGInverse <file>**

Reads  $G^{-1}$  from "Gi" by default, or from a user-supplied file. See the caution below.

#### **OPTION readA22 <file>**

Reads  $A_{22}$  from "A22" by default, or from a user-supplied file.

## OPTION readA22Inverse <file>

Reads  $A_{22}^{-1}$  from "A22i" by default, or from a user-supplied file. See the caution below.

## OPTION readGmA22 <file>

Reads  $\mathbf{G} - \mathbf{A}_{22}$  from "GmA22" by default, or from user-supplied file. This option is obsolete.

#### Caution:

With the options readGinverse and readA22Inverse combined OPTION TauOmega tau omega, the program applies  $\tau$  to the loaded  $\mathbf{G}^{-1}$  and  $\omega$  to the loaded  $\mathbf{A}_{22}^{-1}$  regardless of whether the matrices have been already scaled with  $\tau$  or  $\omega$ . In other words, the loaded matrix could be scaled twice if the user used  $\tau$  or  $\omega$  both in saving and reading the matrix. Be careful to use the scaling factors combined with the input/output options.

**Hint:** OPTION TauOmega was needed when inbreeding was not considered for  $A^{-1}$ . Because inbreeding is now considered for  $A^{-1}$ , we recommend not using this option anymore.

#### **POSTGSF90**

#### *Basic options*

The program calculates SNP effects using the ssGBLUP framework (Wang et al., 2012). The program needs OPTION map\_file to assign SNP to their location for Manhattan plots, so chromosomes are visualized in different colors. The following options for POSTGSF90 (ssGWAS) are available:

#### **OPTION Manhattan\_plot**

Plots the Manhattan plot (SNP effects) for each trait and correlated effects using GNUPLOT.

#### **OPTION Manhattan\_plot\_R**

Plots the Manhattan plot (SNP effects) for each trait and correlated effects using R. TIF images are created: manplot\_Sft1e2.tif (note: t1e2 corresponds to trait 1, effect 2).

#### **OPTION Manhattan\_plot\_R\_format format**

Controls the format type to create images in R. The format values accepted are: pdf (default), png, or tif.

#### **OPTION plotsnp n**

Controls the values of SNP effects to use in Manhattan plots 1: plots regular SNP effects: abs(val) 2: plots standardized SNP effects: abs(val/sd) (default)

#### **OPTION SNP\_moving\_average n**

Solutions for SNP effects will be by moving average of n adjacent SNPs.

#### **OPTION windows\_variance n**

Calculates the variance explained by n adjacent SNPs.

**Hint:** When this option is used, the sum of variance explained by n adjacent SNPs (column 8 of snp\_sol or column 3 of chrsnpvar) is not 100%. This is because moving variance is used. If windows size is 20, the proportion of variance assigned to SNP 1 is calculated from SNP 1 to 20, for SNP 2 it goes from 2 to 21, for SNP 3 it goes from 3 to 22, and so forth. A file called windows\_variance has variance that sums to 100% in column 9.

## **OPTION windows\_variance\_mbp n**

Calculates the variance explained by n Mb window of adjacent SNPs.

#### **OPTION windows\_variance\_type n**

Sets windows type for variances calculations 1: moving windows 2: exclusive windows

# **OPTION which\_weight x**

Generates a weight variable to construct a weighted genomic relationship matrix  $\mathbf{G} = \mathbf{Z}\mathbf{D}\mathbf{Z}'$ 1: w = y^2 \* (2(p(1-p))) 2: w = y^2 3: experimental with the degree of brief 4: w = C\*\*(abs(y\_i)/sqrt(var(y))-2) from VanRaden et al. (2009) nonlinearA: same as 4 where y is the SNP solution, with scaled weight = w \* nSnp/sum(w); and C is 1.125 by default (enable to change it using the second argument of the option line (OPTION which\_weight nonlinearA value), e.g., OPTION which\_weight nonlinearA 1.2

# **OPTION** solutions\_postGS **x**

Sets the file name for the solutions file (default = solutions).

# OPTION postgs\_trt\_eff x1 x2

Computes postGS solutions (SNP solutions, variance explained, etc.) for only trait: x1 and effect: x2

# **OPTION snp\_p\_value**

Computes p-values for GWAS from elements of the inverse of the Mixed Model Equations previously obtained from blupf90. This requires quite a lot of memory and time. See **Aguilar et al. (2019)** for more details.

# **OPTION snp\_var**

Creates a file with prediction error covariance (PEC) for SNP to be used in **PREDF90** to compute reliability for indirect predictions. This option works when **OPTION snp\_p\_value** is used in BLUPF90+.

# Output files for **POSTGSF90**:

"snp\_sol" contains solutions of SNP and weights

- 1: trait
- 2: effect
- 3: SNP
- 4: Chromosome
- 5: Position
- 6: SNP solution
- 7: weight (can be used as the weight to calculate the weighted **G** matrix)
- 8: variance explained by n adjacent SNP (if OPTION windows\_variance is used)
- 9: variance of the SNP solution (used to compute the p-value if **OPTION snp\_p\_value** is used)

"chrsnp" contains data to create the plot by GNUPLOT

1: trait

2: effect

3: values of SNP effects to use in Manhattan plots, i.e., (abs(SNP\_i)/var(SNP))

4: SNP

- 5: Chromosome
- 6: Position

# "chrsnp\_pval" contains data to create the plot by GNUPLOT

1: trait

- 2: effect
- 3: -log10(p-value)
- 4: SNP
- 5: Chromosome
- 6: Position

# "chrsnpvar" contains data to create plot by GNUPLOT

- 1: trait
- 2: effect
- 3: variance explained by n adjacent SNP
- 4: SNP
- 5: Chromosome
- 6: Position

"windows\_segment" contains information of windows segments used to get variance explained

- 1: label
- 2: window size (number of SNP)
- 3: Start SNP number for the window
- 4: End SNP number for the window
- 5: identification of window: (ChrNumber)'\_'(startPositionMBP)
- 6: Start (ChrNumber)'\_'(Position) for the window
- 7: End (ChrNumber)'\_'(Position) for the window

"windows\_variance" contains variance explained for the biggest non-overlapping windows segments

- 1: trait
- 2: effect
- 3: Start SNP number or SNP name for the window
- 4: End SNP number or SNP name for the window
- 5: window size (number of SNP)
- 6: Start (ChrNumber)'\_'(Position) for the window
- 7: End (ChrNumber)'\_'(Position) for the window
- 8: identification of window: (ChrNumber)'\_'(startPositionMBP)
- 9: variance explained by n adjacents SNP

"snp\_pred" contains allele frequencies + SNP effects

*Graphic control files:* 

Several files are created to generate graphics using either GNUPLOT or R.

File names rules

"Sft1e2.R". The first letter indicates "S" for solutions of SNP, "V" for variance explained, and "P" for p-values.

"t1e2" indicates that the file is for the trait 1 and the effect 2.

## Filename extension

xxx.gnuplot => GNUPLOT xxx.R => R programs xxx.pdf => image xxx.png => image xxx.tif => image

Misc. options:

## **OPTION num\_threads\_pregs n**

Specify the number of threads n to be used with MKL-OpenMP for creating and inverting matrices

## **OPTION num\_threads\_iod n**

Specify the number of threads n to be used with MKL-OpenMP in "BLUP90IOD" program for matrix-vector multiplications in the PCG algorithm

## **OPTION graphics s**

Allows to generate plots with "GNUPLOT" program. If present optional parameter s, set the time in seconds to show the plot. Avoid using in batch programs!

## **OPTION msg x**

x set level of verbose; 0 minimal; 1 gives more diagnostic information

## PREDF90

Predicts direct genomic value (DGV) for young animals based on only genotypes i.e.  $\hat{\mathbf{u}} = \mathbf{Z}\hat{\mathbf{a}}$ , where  $\hat{\mathbf{u}}$  is DGV and  $\hat{\mathbf{a}}$  is the SNP effects. The prediction is based on SNP effects obtained from **POSTGSF90**. For young animals that were not included in the previous analysis, DGV can be calculated using the "snp\_pred" file

from **POSTGSF90**. PREDF90 requires some output files from POSTGSF90 and a genotype file for the animals to be predicted. It does not accept a parameter file but takes command-line options.

PREDF90 does not accept a parameter file but takes command-line options.

#### --snpfile name

Provides the SNP file for animals to be indirectly predicted. PREDF90 will ask for the SNP file name if this command is not present. The SNP file has the same format as for PREGSF90.

#### --acc

Computes reliability for indirect predictions. It requires OPTION snp\_p\_value in BLUPF90+ and OPTION snp\_var in POSTGSf90. It reads "snp\_var", a file with SNP PEC created by POSTGSF90.

## --acc\_type

Select 1.0 for dairy cattle (Reliability) or 0.5 for beef cattle (BIF accuracy) (default 1.0).

#### --use\_diagG\_acc

Uses inbreeding (F) from **G** in the denominator of the reliability formula: reliability =  $1-\text{PEV}/(\sigma_u^2(1+F))$ .

#### --use\_mu\_hat

Adds the base ( $\hat{\mu}$ ) for DGV so the values are comparable to GEBV. See Legarra et al. (2021) and Lourenco et al. (2018) for more details.

## --use\_var\_mu\_hat

Considers the variance of  $\hat{\mu}$  when calculating the reliability of DGV and is automatically turned on if --use\_mu\_hat and --acc are present.

## --help

Shows the main options.

Usage:

predf90 --snpfile new\_genotypes.txt --use\_mu\_hat --acc --use\_diagG\_acc

With these commands, predf90 will compute indirect predictions for the animals in new\_genotypes.txt, including  $\hat{\mu}$  (i.e., DGV =  $\hat{\mu} + \mathbf{Z}\hat{\mathbf{a}}$ ), computing reliabilities adjusted for inbreeding in **G**.

# Input files:

This program automatically detects and read the following files:

## "snp\_pred"

- information about the random effect (number of traits + correlated effects)
- gene frequencies
- solutions of SNP effects

# SNP\_file\_for\_animals\_to\_predict

SNP file for animals to have DGV predicted. This file has the same format as used in PREGSF90 and POSTGSF90.

*Output file:* 

# "SNP\_predictions"

- ID, call rate, DGV, reliability (if --acc is present)

Constant parameters that cannot be changed by the users:

- 1. alpha fraction of G used (default=0.95); affects scale of prediction
- 2. callrate to be used later for discarding genotypes with poor quality (default=0.7)

# PREDICTF90

This program computes adjusted phenotypes. It reads the blupf90 parameter file, the solutions file, and the data file. It needs **OPTION include\_effects x1 x2 x3** followed by the effects (**x1 x2 x3**) that should NOT be used to adjust phenotypes (y). It computes:

y\_star = y adjusted by the effects not mentioned in **OPTION include\_effects x1 x2 x3** (i.e., the included effects)

y\_hat = sum of estimates of the included effects
residual = y - included effects (not a true residual)

Example: y = herd + age + animal + e If the parameter file has OPTION include\_effects 3.

y\_star = y - herd\_hat - age\_hat (y - effects to be adjusted for)
y\_hat = animal\_hat (effect to keep)

Which makes cor(y\_hat,y\_star) = cor(ebv, adjusted y), in this example, which is a measure of accuracy. However, this is done based on one dataset. Real validations are done between a benchmark computed with a complete dataset (e.g., adjusted phenotypes here) and a prediction using a reduced dataset (e.g., the ebv here). It outputs the correlation between y\_hat and y\_star, for instance cor(ystar,yhat)=cor(u+e, uhat) and outputs these columns into a file, together with animal id (if there is animal in the model) or record number (if not).

In addition, if animal effect is in the model, it produces a file with ebvs from the solutions file.

# *Output file:*

# "yhat\_residual"

The main file is yhat\_residual, which has corrected phenotypes and predicted residuals. The number of columns in this file depend on the number of traits (N).

Column 1: Animal ID (renumbered i.e., same as the 1st column in renaddxx.ped) Column 2 to N+1: "y\_star" explained above Column N+2 to 2N+1: "y\_hat" explained above Column 2N+2 to 3N+1: "residual" explained above

# **Demonstration for genomic analysis**

Data were simulated by D. Lourenco and the files are available here: https://github.com/danielall/Data\_ssGBLUP

# Preparation with RENUMF90

# "renum.par" for RENUMF90

# Parameter file for renumf90 # Data file = phenotypes.txt # 1 2 3 4 5 # animal, sex ,phenotype, TBV, generation # Pedigree file = pedigree.txt # 1 2 3 # animal sire dam # SNP file = genotypes.txt # SNP map file = gen\_map.txt DATAFILE phenotypes.txt TRAITS 3 FIELDS\_PASSED TO OUTPUT

WEIGHT(S)

RESIDUAL\_VARIANCE 0.60

EFFECT 2 cross alpha #sex EFFECT 1 cross alpha #animal RANDOM animal FILE pedigree.txt SNP\_FILE genotypes.txt (CO)VARIANCES 0.40 **OPTION** map\_file gen\_map.txt

#### **Run RENUMF90**

RENUMF90 version 1.157 with zlib renum.par . . . . . . . . . Inbreeding statistics: the maximum inbreeding coefficient = 0.3125 average inbreeding for inbred animals = 0.0621 n = 1292for all animals = 0.0067 n = 12010 Number of animals with records 10000 = Number of animals with genotypes 2024 = 10000 Number of animals with records or genotypes = Number of animals with genotypes and no records = 0 Number of parents without records or genotypes = 2010 Total number of animals = 12010

Wrote cross reference IDs for SNP file "genotypes.txt XrefID"

Wrote parameter file "renf90.par" Wrote renumbered data "renf90.dat" 10000 records Wrote field information "renf90.fields" for 3 fields in data

#### "renf90.par" from RENUMF90

# BLUPF90 parameter file created by RENUMF90 DATAFILE renf90.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 **OBSERVATION(S)** 1 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT[EFFECT NESTED]

2 2 cross

3 12010 cross

RANDOM\_RESIDUAL VALUES

0.60000 RANDOM\_GROUP 2 RANDOM\_TYPE add\_an\_upginb FILE renadd02.ped (CO)VARIANCES 0.40000 OPTION SNP\_file genotypes.txt OPTION map\_file gen\_map.txt

#### Analysis with BLUPF90

```
Run BLUPF90
```

BLUPF90 ver. 1.71

```
renf90.par
Parameter file:
                     renf90.dat
Data file:
Number of Traits
                      1
Number of Effects
                     2
Position of Observations
                      1
Position of Weights
                       0
Value of Missing Trait/Observation
                                   0
name of parameter file?renf90.par
... ... ...
*-----*
            Genomic Library: Version 1.308
                                           *
*
*
         Optimized OpenMP Version - 4 threads
                                           *
* Modified relationship matrix (H) created for effect: 2
                                           *
```

Read 12010 animals from pedigree file: "renadd02.ped" Number of Genotyped Animals: 2024 ... ...

round = 55 convergence = 0.1126E-11 round = 56 convergence = 0.5045E-12 56 iterations, convergence criterion= 0.5045E-12 solutions stored in file: "solutions"

Analysis with POSTGSF90

#### **Run POSTGSF90**

name of parameter file?renf90.par postGSf90 ver. 1.77 ... ... Solutions read from file: "solutions" Solutions for SNPs in file: "snp\_sol" Files for pedictions by SNP effects in file: "snp pred"

# Indirect Predictions with PREDF90

#### **Run PREDF90**

```
predf90 1.13
Predicts EBVs from genotypes based on results from single-step evaluation
 ... ... ...
Number of SNP:
                             4500
Number of traits: 1
number of correlated traits: 1
 . . . . . . . . . .
MU hat to adjust Za
    Trait: 1
    Correlated effect: 1
    mu hat: 0.1443
 ... ... ...
            3000 SNP
The genotype file contains 45000 SNP starting from position 14
  Firts 10 genotypes: Id, EBV
  UGA42014 0.4649608
  UGA42019
                        0.6343889
-U.1096066
UGA42047 0.6454658
UGA42051 0.5041275
UGA42052 1.7737031E-02
UGA42056 0.9935431
UGA42057 0.2609830
  Processed 2024 genotypes
  Average calling rate: 1.00
$head -5 SNP_predictions

        UGA42014
        1.00
        0.46496075

        UGA42019
        1.00
        0.63438886

        UGA42029
        1.00
        -0.10960658

        UGA42039
        1.00
        0.93601137

        UGA42047
        1.00
        0.64546579
```

Computing adjusted phenotypes with PREDICTF90

## **Run PREDICTF90**

This program is used to calculate adjusted y,  $\hat{y}$ , and residuals using the same parameter file and "solutions" as BLUPF90

Output files: "yhat\_residual" Format: record #, adjusted y, ŷ, residual "bvs.dat" The same format as "solutions" including (G)EBV.

```
# BLUPF90 parameter file created by RENF90 and extended to work with PREDICTF90
DATAFILE
renf90.dat
NUMBER_OF_TRAITS
     1
NUMBER_OF_EFFECTS
     2
OBSERVATION(S)
 1
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT[EFFECT NESTED]
2
     2 cross
3 12010 cross
RANDOM_RESIDUAL VALUES
0.60000
RANDOM_GROUP
  2
RANDOM_TYPE
add_an_upginb
FILE
renadd02.ped
(CO)VARIANCES
0.40000
OPTION SNP_file genotypes.txt
OPTION map_file gen_map.txt
OPTION include_effects 2 #phenotypes will be adjusted for all effects but effect number 2 (animal)
Run PREDICTF90
name of parameter file?
pred.par
*** include effects to predict Yhat n, effects
                                            1
                                                  2
```

PREDICTF90 ver. 1.6

 Animal Effect:
 2

 y(s), yhat(s), residual(s) in written in "yhat\_residual" file

 10000 records read

 Trait:
 1

 mean Y
 8.662515402103672E-002 var Y

 0.934465837702133

 mean Yhat
 8.662514367382973E-002 var Yhat

 0.181142370417667

 cov (Y,Yhat)
 0.344475853966058

## wrote bvs for animals in data in file "bvs.dat"

## Hints:

1) The effect that goes into OPTION include\_effects (e.g., OPTION include\_effects 2) is included in the Yhat. In this small example with 1 trait, the format of yhat\_residual is: Animal\_id, Y, Yhat, residual Where: Y = Phenotype  $-\mu$ 

Yhat = EBV (or animal effect) Residual = Phenotype - EBV

2) When 2 traits are used in the model, the format of yhat\_residual is: Animal\_id, Y1, Y2, Yhat1, Yhat2, residual1, residual2

3) corr (Y,Yhat) should not be used as a measure of predictivity because it uses adjusted phenotypes and EBVs from the same dataset. Usually, predictivity requires phenotypes adjusted for fixed effects in the complete data (benchmark) and (G)EBVs calculated from the reduced data (without records for validation animals). The regular predictivity measure is: corr[Y\_from\_PREDICTf90, (G)EBV\_reduced]

```
For this small example with 1 trait, a general Linux bash code is:
```

```
$awk '{print $1,$2}' ebv_complete/yhat_residual | sort +0 -1 > Y
$awk '{if ($2==2) print $3,$4}' ebv_reduced/solutions | sort +0 -1 > ebv.temp
$awk '{if ($2==2) print $3,$4}' gebv_reduced/solutions | sort +0 -1 > gebv.temp
$join -1 +1 -2 +1 Y validation_animals > file1.temp
$join -1 +1 -2 +1 file1.temp ebv.temp > file2.temp
$join -1 +1 -2 +1 file2.temp gebv.temp > Y_ebv_gebv
```

#obs: validation\_animals is a file that contains sorted ids for validation animals

#### An R code to calculate correlations is:

```
pred <- read.table("Y_ebv_gebv",header=F)
ebv_predictivity <- cor(pred[,2],pred[,3]); ebv_predictivity
gebv_predictivity <- cor(pred[,2],pred[,4]); gebv_predictivity</pre>
```

# **Examples of parameter files**

#### Sire model without A matrix

```
DATAFILE
test.dat
NUMBER_OF_TRAITS
1
NUMBER_OF_EFFECTS
2
OBSERVATION(S)
3
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
1 2 cross
2 3 cross
```

RANDOM\_RESIDUAL VALUES

10 RANDOM\_GROUP 2 RANDOM\_TYPE diagonal FILE

(CO)VARIANCES 1

## Sire model with A matrix

DATAFILE test.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 3 WEIGHT(S)

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 2 cross 2 3 cross RANDOM\_RESIDUAL VALUES 10 RANDOM\_GROUP 2 RANDOM\_TYPE add\_sire FILE sire.ped (CO)VARIANCES 1

## **Two-trait sire model**

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 3 4 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 1 2 cross 2 2 3 cross RANDOM\_RESIDUAL VALUES 10 1 1 5 RANDOM\_GROUP 2 RANDOM\_TYPE add\_sire FILE sire.ped (CO)VARIANCES 1 0.1 0.1 1

## **Animal model**

DATAFILE test.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 **OBSERVATION(S)** 3 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 12 cross 5 10 cross RANDOM\_RESIDUAL VALUES 10 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 1

# Multiple trait animal model # Example 1: two-trait animal model

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 3 4 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 1 2 cross 5 5 10 cross RANDOM\_RESIDUAL VALUES 10 1 1 5 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 1 0.1 0.1 1

# # Example 2: different model for each trait

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 3 **OBSERVATION(S)** 34 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 2 2 cross 5 5 10 cross 6 7 30 cross RANDOM\_RESIDUAL VALUES 10 1 15 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 10.1 0.11 RANDOM\_GROUP 3 RANDOM\_TYPE diagonal FILE

(CO)VARIANCES 10 01

#### Animal model with UPG

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 34 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 112 cross 5 5 13 cross RANDOM\_RESIDUAL VALUES 10 1 15 RANDOM\_GROUP 2 RANDOM\_TYPE add\_an\_upg FILE animal.ped (CO)VARIANCES 10.1 0.11 Animal model with inbreeding

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 3 4 WEIGHT(S)

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 1 2 cross 5 5 13 cross RANDOM\_RESIDUAL VALUES 10 1 15 RANDOM\_GROUP 2 RANDOM\_TYPE add\_an\_upginb FILE animal.ped (CO)VARIANCES 10.1 0.11

## **Repeatability model – single trait**

DATAFILE test.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 3 OBSERVATION(S) 3 WEIGHT(S)

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 2 cross 5 5 cross 5 5 cross RANDOM\_RESIDUAL VALUES 10 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 1 RANDOM\_GROUP 3 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 1

#### **Repeatability model – two traits**

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 3 **OBSERVATION(S)** 34 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 112 cross 5 5 5 cross 555 cross RANDOM\_RESIDUAL VALUES 10 1 15 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 10.1 0.1 1 RANDOM\_GROUP 3 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 10.1 0.11 **Maternal effect model** DATAFILE maternal.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 4 **OBSERVATION(S)** 4 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 3 946 cross 1 22473 cross

2 22473 cross

2 22473 cross RANDOM\_RESIDUAL VALUES 1050 RANDOM\_GROUP 23 RANDOM\_TYPE add\_animal FILE maternal.ped (CO)VARIANCES 450 -100 -100 340 RANDOM\_GROUP 4 RANDOM\_TYPE diagonal FILE

(CO)VARIANCES 370

# # For (THR)GIBBSxF90

# Example 1 – declaring the random, diagonal effect separately for effects 4 and 5.

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 5 **OBSERVATION(S)** 34 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 102 cross 0 2 2 cross 5 5 10 cross 6 0 30 cross 0 7 20 cross RANDOM\_RESIDUAL VALUES 10 1 15 RANDOM\_GROUP 3 RANDOM\_TYPE add animal FILE animal.ped (CO)VARIANCES

10.1 0.11 RANDOM\_GROUP 4 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 10 00 RANDOM\_GROUP 5 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 00 01

# Example 2 – joint declaration for the random, diagonal effects 4 and 5.

DATAFILE test.dat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 5 **OBSERVATION(S)** 34 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 102 cross 0 2 2 cross 5 5 10 cross 6 0 30 cross 0730 cross RANDOM\_RESIDUAL VALUES 10 1 15 RANDOM\_GROUP 3 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 10.1

0.1 1 RANDOM\_GROUP 45 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 1000 0000 0000 0001 **#** Dominance model DATAFILE dom.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 4 **OBSERVATION(S)** 3 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 11 cross 4 1 cov 2 30001 cross 5 10412 cross RANDOM\_RESIDUAL VALUES 100 RANDOM\_GROUP 3 RANDOM\_TYPE add\_an\_upginb FILE add.ped (CO)VARIANCES 10 RANDOM\_GROUP 4 RANDOM\_TYPE par\_dom FILE dom.ped (CO)VARIANCES 2 **Random regression model** 

**# Single trait**
```
DATAFILE
data_score
NUMBER_OF_TRAITS
1
NUMBER_OF_EFFECTS
10
OBSERVATION(S)
9
WEIGHT(S)
```

1 10 1 1 1 10

**# Two traits** 

NUMBER\_OF\_TRAITS

DATAFILE test.dat1

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 788 cross 2 32 cross 5 1 cov 6 1 cov 3 15097 cross 5 15097 cov 3 6 15097 cov 3 3 81883 cross 5 81883 cov 3 6 81883 cov 3 RANDOM\_RESIDUAL VALUES 100 RANDOM\_GROUP 567 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 100 1 1 1 10 1 1 1 10 RANDOM\_GROUP 8910 RANDOM\_TYPE add\_an\_upg FILE ped\_score (CO)VARIANCES 100 1 1

### 73

```
2
NUMBER_OF_EFFECTS
9
OBSERVATION(S)
34
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
112 cross
661 cov
771cov
2 2 5 cross
665 cov 22
775 cov 22
2 2 10 cross
6 6 10 cov 2 2
7710 cov 22
RANDOM_RESIDUAL VALUES
10 1
15
RANDOM_GROUP
456
RANDOM_TYPE
diagonal
FILE
(CO)VARIANCES
1 0.1 0.1 0.1 0.1 0.1
0.1 1 0.1 0.1 0.1 0.1
0.1 0.1 1 0.1 0.1 0.1
0.1 0.1 0.1 1 0.1 0.1
0.1 0.1 0.1 0.1 1 0.1
0.1\,0.1\,0.1\,0.1\,0.1\,1
RANDOM_GROUP
789
RANDOM_TYPE
add_animal
FILE
animal.ped
(CO)VARIANCES
1 0.1 0.1 0.1 0.1 0.1
0.1 1 0.1 0.1 0.1 0.1
0.1\,0.1\,1\,0.1\,0.1\,0.1
0.1 0.1 0.1 1 0.1 0.1
0.1 0.1 0.1 0.1 1 0.1
0.1 0.1 0.1 0.1 0.1 1
```

### # Example 3

DATAFILE

test.dat2 NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 10 **OBSERVATION(S)** 34 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 112 cross 661 cov 771 cov 8 8 1 cov 665 cov 22 775 cov 22 885 cov 22 6 6 10 cov 2 2 7 7 10 cov 2 2 8 8 10 cov 2 2 RANDOM\_RESIDUAL VALUES 10 1 15 RANDOM\_GROUP 567 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 1 0.1 0.1 0.1 0.1 0.1 0.1 1 0.1 0.1 0.1 0.1 0.1 0.1 1 0.1 0.1 0.1 0.1 0.1 0.1 1 0.1 0.1 0.1 0.1 0.1 0.1 1 0.1 0.1 0.1 0.1 0.1 0.1 1 RANDOM\_GROUP 8910 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 1 0.1 0.1 0.1 0.1 0.1 0.1 1 0.1 0.1 0.1 0.1 0.1 0.1 1 0.1 0.1 0.1  $0.1\,0.1\,0.1\,1\,0.1\,0.1$ 0.1 0.1 0.1 0.1 1 0.1 0.1 0.1 0.1 0.1 0.1 1

Random regression model with heterogeneous residual variances

### using airemlf90 **# Example 1: with intercept** DATAFILE test.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 9 **OBSERVATION(S)** 3 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 2 cross 6 1 cov 7 1 cov 5 5 cross 6 5 cov 5 7 5 cov 5 5 10 cross 6 10 cov 5 7 10 cov 5 RANDOM\_RESIDUAL VALUES 10 RANDOM\_GROUP 456 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 10.10.1 0.1 1 0.1 0.1 0.1 1 RANDOM\_GROUP 789 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 10.10.1 0.1 1 0.1 0.1 0.1 1

# Example 2: with no intercept

OPTION hetres\_pos 6 7 OPTION hetres\_pol 4.0 1.0 0.1 DATAFILE test.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 7 OBSERVATION(S) 3 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 12 cross 6 1 cov 7 1 cov 6 5 cov 5 7 5 cov 5 6 10 cov 5 7 10 cov 5 RANDOM\_RESIDUAL VALUES 10 RANDOM\_GROUP 45 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 10.1 0.11 RANDOM\_GROUP 67 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 10.1 0.1 1 OPTION hetres\_pos 6 7 OPTION hetres\_pol 1.0 0.1 ### using GIBBS3F90

DATAFILE test.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 9 OBSERVATION(S) 3

WEIGHT(S)

### EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 2 cross 6 1 cov 7 1 cov 5 5 cross 6 5 cov 5 7 5 cov 5 5 10 cross 6 10 cov 5 7 10 cov 5 RANDOM\_RESIDUAL VALUES 10 RANDOM\_GROUP 456 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 10.10.1 0.1 1 0.1 0.1 0.1 1 RANDOM\_GROUP 789 RANDOM\_TYPE add\_animal FILE animal.ped (CO)VARIANCES 10.10.1 0.1 1 0.1 0.1 0.1 1 **OPTION hetres\_int 8 5**

### Competitive model (i.e., social interaction effects)

DATAFILE competition.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 19 OBSERVATION(S) 24 WEIGHT(S)

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT[EFFECT NESTED]

2 88 cross 3 362 cross 21 2409 cross 4 8004 cross 22 0 cov 5 22 0 cov 6 22 0 cov 7 22 0 cov 8 22 0 cov 9 22 0 cov 10 22 0 cov 11 22 0 cov 12 22 0 cov 13 22 0 cov 14 22 0 cov 15 22 0 cov 16 22 0 cov 17 22 0 cov 18 22 8004 cov 19 RANDOM\_RESIDUAL VALUES 1225.8 RANDOM\_GROUP 45 RANDOM\_TYPE add\_animal FILE renadd04.ped (CO)VARIANCES 267.03 25.313 25.313 104.44 RANDOM\_GROUP 2 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 89.187 RANDOM\_GROUP 3 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 167.34

# Appendix A (single trait animal model)

Single trait "USDA-type" animal model. The files used in this example are available here.

 $y_{ijkl} = hys_i + hs_{ij} + p_k + a_k + e_{ijkl}$ 

where

<b>y</b> ijkl	<ul> <li>production yield</li> </ul>
hys <sub>i</sub>	<ul> <li>fixed herd year season</li> </ul>
hs <sub>ij</sub>	- random herd x sire interaction
p <sub>k</sub>	- random permanent environment
a <sub>k</sub>	- random animal

and

var( hs<sub>ij</sub>) = .05, var(p<sub>k</sub>)=.1, var(a<sub>k</sub>)=.5, var(e<sub>ijkl</sub>)=1

Data file (ic)

Format: animal/hys/p/hs/y 1 1 1 1 10 2 1 2 1 11

 3
 2
 3
 2
 15

 4
 2
 4
 3
 13

 5
 3
 5
 4
 14

 6
 3
 6
 3
 12

Pedigree file (is)

Format: animal/dam/sire/code

Parameter file

# Example of single-trait animal model with one fixed effect
DATAFILE
ic
NUMBER\_OF\_TRAITS
1
NUMBER\_OF\_EFFECTS
4
OBSERVATION(S)
5
WEIGHT(S)

```
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
2 3 cross
36 cross
4 4 cross
1 14 cross
RANDOM_RESIDUAL VALUES
1
RANDOM_GROUP
2
RANDOM_TYPE
diagonal
FILE
(CO)VARIANCES
.1
RANDOM_GROUP
3
RANDOM_TYPE
diagonal
FILE
(CO)VARIANCES
.05
RANDOM_GROUP
4
RANDOM_TYPE
add_an_upg
FILE
is
(CO)VARIANCES
.5
Execution
name of parameter file?exiap
    BLUPF90 1.00
Parameter file:
                           exiap
Data file:
                            ic
Number of Traits
                            1
Number of Effects
                             4
                           5
Position of Observations
Position of Weight (1)
                               0
Value of Missing Trait/Observation
                                              0
EFFECTS
                      position (2)
# type
                                            levels
                                                      [positions for nested]
1cross-classified22cross-classified3
                                               3
                        3
                                                6
3cross-classified44cross-classified1
                                                4
                                               14
```

```
Residual (co)variance Matrix
    1.000
Random Effect
                  2
Type of Random Effect:
                          diagonal
trait effect (CO) VARIANCES
        2
                0.100
 1
Random Effect
                  3
Type of Random Effect:
                          diagonal
trait effect (CO) VARIANCES
        3
                0.050
 1
Random Effect
                  4
                          additive animal
Type of Random Effect:
Pedigree File:
                          is
trait effect
                (CO) VARIANCES
 1
        4
                0.500
REMARKS
  (1) Weight position 0 means no weights utilized
  (2) Effect positions of 0 for some effects and traits means that such
     effects are missing for specified traits
Data record length = 5
original G
  0.10
inverted G
 10.00
original G
  0.05
inverted G
 20.00
original G
  0.50
inverted G
  2.00
solutions stored in file: "solutions"
trait/effect level solution
 1 1
         1
                11.8589
 1 1
           2
                13.7539
 1 1
                14.7086
           3
                -0.0088
 12
           1
 12
           2
                0.0088
                -0.0159
 12
           3
 12
                0.0159
           4
 12
           5
                 0.0321
 12
           6
                -0.0321
 1 3
           1
                 0.0000
 1 3
           2
                -0.0079
 13
                -0.0081
           3
 13
           4
                 0.0161
 14
           1
                 -1.7627
 14
           2
                 -0.9553
 14
           3
                 1.4288
 1
   4
           4
                 -0.9206
 1
   4
           5
                 -1.0781
 14
           6
                -2.3474
 14
           7
                 0.8511
 14
           8
                 -0.1521
 14
           9
                 3.8926
 14
          10
                 -2.7717
```

1	4	11	0.8528
1	4	12	-3.1911
1	4	13	7.9976
1	4	14	-6.3340

## **Appendix B (multiple trait sire model)**

Example of multiple trait sire model (from L.R. Schaeffer notes of 1985).

### Models

Trait 1:  $y_{1i}=h_i+s_{1j}+e_{1ijk}$ Trait 2:  $y_{2i}=\mu+s_{2j}+e_{2jk}$ 

### where

h - fixed herd

s - random sire

and

var(s)=A[8 6; 6 17], var(e)=I[10 10; 10 20]

Data file (lrsdat) Format:  $h/\mu/s/y_1/y_2$ 1 0 1 3.4 0 2 0 2 1.3 0 1 1 3 .8 50.3 2 1 4 4.5 52.6 0 1 5 0 55.0

Pedigree file (Irsrel)

Format: bull/sire/MGS 1 3 0 2 0 5 3 0 0 4 0 0 5 0 0

Parameter file (Irsex) # Example of two trait sire model with unequal models DATAFILE Irsdat NUMBER\_OF\_TRAITS 2 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 4 5 WEIGHT(S)

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 2 2 cross 3 3 5 cross RANDOM\_RESIDUAL VALUES 10 10 10 20 RANDOM\_GROUP 2 RANDOM\_TYPE add\_sire FILE Irsrel (CO)VARIANCES 86 617 **Execution** name of parameter file?lrsex BLUPF90 1.00 Parameter file: lrsex Data file: lrsdat Number of Traits 2 Number of Effects 2 45 Position of Observations Position of Weight (1) 0 Value of Missing Trait/Observation 0 EFFECTS # type position (2) levels [positions for nested] 12 1 cross-classified 2 2 cross-classified 33 5 Residual (co)variance Matrix 10.000 10.000 10.000 20.000 Random Effect 1 Type of Random Effect: additive sire Pedigree File: lrsrel trait effect (CO) VARIANCES 2 8.000 6.000 1 2 2 6.000 17.000 REMARKS (1) Weight position 0 means no weights utilized (2) Effect positions of 0 for some effects and traits means that such effects are missing for specified traits Data record length = 5original G 8.00 6.00 6.00 17.00 inverted G 0.17 -0.06 -0.06 0.08 solutions stored in file: "solutions"

85

trait/effect		level	solution
1	1	1	2.3877
2	1	1	52.4449
1	1	2	3.2180
2	1	2	0.0000
1	2	1	0.2243
2	2	1	-0.0210
1	2	2	-0.8217
2	2	2	-0.3866
1	2	3	-0.4969
2	2	3	-0.7512
1	2	4	0.6178
2	2	4	-0.0769
1	2	5	0.2217
2	2	5	1.0851

# Appendix C (test-day model)

This test-day model example comes from the paper of Schaeffer and Dekkers (WCGALP94 18:443). The files used in this example are available **here**.

Model

 $y_{ijkl} = h_i + \beta_1 X_{1j} + \beta_2 X_{2j} + a_k + \gamma_{1k} X_{1j} + \gamma_{2k} X_{2j} + e_{ijkl}$ 

where

and

 $\begin{array}{ll} y_{ijkl} & - \mbox{ yield of test day} \\ h_i & - \mbox{ test day effect} \\ X_{1j} & - \mbox{ days in milk} \\ X_{2j} & - \mbox{ log(days in milk)} \\ \beta_{1}, \beta_{2} & - \mbox{ fixed regressions} \\ a_k & - \mbox{ random animal} \\ \gamma_{1k}, \gamma_{2k} & - \mbox{ random regressions for each animal} \end{array}$ 

 $var(e_{ijkl}) = 1; var(a_k, \gamma_{1k}, \gamma_{2k}) = [2.254 - .7; 4137512; -.71294]^{-1}$ 

### Data file (Irsrrdat)

Pedigree file (Irsrrrel)

Format: animal/sire/dam

- 197
- 2 10 8

392

4 10 8

```
5 11 7
6 11 1
700
800
900
10 0 0
11 0 0
Parameter file (exlrsrr)
# Example of single-trait random-regression model
DATAFILE
Irsrrdat
NUMBER_OF_TRAITS
1
NUMBER_OF_EFFECTS
6
OBSERVATION(S)
5
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
16 cross
3 1 cov
4 1 cov
2 11 cross
3 11 cov 2
4 11 cov 2
RANDOM_RESIDUAL VALUES
1
RANDOM_GROUP
456
RANDOM_TYPE
add_animal
FILE
Irsrrrel
(CO)VARIANCES
.447906 -0.001334 0.003506
-0.001334 0.000732 -0.000103
0.003506 -0.000103 .010678
Execution
name of parameter file?exlrsrr
     BLUPF90 1.00
Parameter file:
                             exlrsrr
Data file:
                            lrsrrdat
Number of Traits
                              1
Number of Effects
                               6
Position of Observations
                              5
Position of Weight (1)
                               0
Value of Missing Trait/Observation
                                                0
```

EFFECTS

# type position (2) levels [positions for nested] 1 cross-classified 1 6 2 covariable 3 1 3 covariable 4 1 11 4 cross-classified 2 5 covariable 3 11 2 6 covariable 4 11 2 Residual (co)variance Matrix 1.000 correlated random effects 456 Type of Random Effect: additive animal Pedigree File: lrsrrrel trait effect (CO) VARIANCES 4 0.448 -0.001 0.004 1 1 5 -0.001 0.001 0.000 1 6 0.004 0.000 0.011 REMARKS (1) Weight position 0 means no weights utilized (2) Effect positions of 0 for some effects and traits means that such effects are missing for specified traits Data record length = 5original G 0.45 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.01 inverted G 2.25 4.00 -0.70 4.001375.09 11.95 -0.70 11.95 94.00 solutions stored in file: "solutions" trait/effect level solution 1 1 1 19.9496 1 1 2 20.3729 1 1 3 20.6095 1 1 4 19.7278 1 1 5 18.6035 1 1 6 17.8500 12 -0.0498 1 1 3 5.2912 1 14 1 -0.4430 14 2 0.2704 14 -0.7288 3 14 4 1.1019 14 5 -0.1626 14 6 -0.4828 14 7 -0.0988 14 8 0.4574 14 9 -0.6288 14 10 0.4574 14 -0.1872 11 1 5 1 0.0369 1 5 2 -0.0661 15 3 0.0068 15 4 -0.0054 15 5 0.0069 15 6 0.0167 15 7 0.0133

1	5	8	-0.0238
1	5	9	0.0350
1	5	10	-0.0238
1	5	11	-0.0008
1	6	1	-0.0370
1	6	2	0.0325
1	6	3	-0.0479
1	6	4	0.0767
1	6	5	-0.0149
1	6	6	-0.0377
1	6	7	-0.0103
1	6	8	0.0364
1	6	9	-0.0480
1	6	10	0.0364
1	6	11	-0.0145

# Appendix D (multibreed maternal effect model)

This model was used for studies on multibreed evaluation in beef cattle. It is provided as an example of a model with maternal effect and different models per trait.

```
Model (in concise form, with most indices omitted)
```

 $y_1 = cg_1 + bt + mbt + a + M + e$   $y_2 = cg_2 + bt + mbt + a + M + pe + e$  $y_3 = cg_3 + bt + mbt + a + e$ 

where

<b>Y</b> 1-3	<ul> <li>birth weight, weaning weight, and gain</li> </ul>
cg <sub>1-3</sub>	- contemporary groups separate for each trait
br	- breed type
mbt	- maternal breed type
а	- additive effect
m	- maternal effect

pe - permanent environmental effect of the dam

### Data file (data.out)

Format:

- 1. contemporary group for trait 1
- 2. contemporary group for trait 2
- 3. contemporary group for trait 3
- 4. animal breed type
- 5. maternal breed type
- 6. animal id
- 7. dam id
- 8. birth weight
- 9. weaning weight
- 10. gain

### Pedigree file (pedi.outok)

Format:

animal sire or unknown parent group dam or unknown parent group "1 + number of missing parents" Parameter file (param.out) DATAFILE data.out NUMBER\_OF\_TRAITS 3 NUMBER\_OF\_EFFECTS 6 OBSERVATION(S) 8 9 10 WEIGHT(S)

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 123 133085 cross 4 4 4 181 cross 5 5 0 165 cross 666 1724112 cross 770 1724112 cross 070 1724112 cross RANDOM\_RESIDUAL VALUES 26.3 40.7 20.3 40.7 1312.9 141.9 20.3 141.9 1246.3 RANDOM\_GROUP 45 RANDOM\_TYPE add\_an\_upg FILE pedi.outok (CO)VARIANCES 22.9 36.3 18.6 -4.6 0.0 0.0 36.6 500.2 110.8 0.0 -91.6 0.0 18.6 110.8 313.0 0.0 0.0 0.0 -4.6 0.0 0.0 10.1 0.0 0.0 0.0 -91.6 0.0 0.0 419.1 0.0 0.0 0.0 0.0 0.0 0.0 0.0 RANDOM\_GROUP 2 RANDOM\_TYPE diagonal FILE (CO)VARIANCES 0.263 0.0 0.0 0.0 13.129 0.0 0.0 12.463 0.0 RANDOM\_GROUP 3 RANDOM\_TYPE diagonal

FILE

(CO)VARIANCES 0.263 0.0 0.0 0.0 13.129 0.0 0.0 0.0 0.0 RANDOM\_GROUP 6 RANDOM\_TYPE diagonal FILE

### (CO)VARIANCES

0.00.00.00.045.50.00.00.00.0

# **Appendix E (random regression model)**

A single-trait random regression model for test-day milk is using cubic Legendre polynomials.

Model

$$y_{ijkl} = hym_{ij} + \sum_{m=1}^{4} \alpha_m(l)h_{im} + \sum_{m=1}^{4} \alpha_m(l)u_{km} + \sum_{m=1}^{4} \alpha_m(l)pe_{im} + e_{ijkl}$$

where

- y<sub>ijkl</sub> test day milk
- hym<sub>ij</sub> hear-year-test for herd i and year-test j
- h<sub>i</sub> effects of herd i
- $\alpha_m(I)$  value of m-th Legendre polynomial at point corresponding to DIM=I
- u additive effects
- pe permanent environmental effects

Data file (datarr)

Format:

1.herd

- 2. hear-year-test
- 3-6. values of Legendre polynomials
- 7. weight for residuals: 100/var(eijkl)
- 8. test day
- 9. animal

Relationship file (pedirr)

Format:

animal sire dam

```
Parameter file (exrr3)

DATAFILE

datarr

NUMBER_OF_TRAITS

1

NUMBER_OF_EFFECTS

13

OBSERVATION(S)

8

WEIGHT(S)

7

EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT
```

2 3726 cross #herd-year-test 3 84 cov 1 #herd 4 84 cov 1 5 84 cov 1 6 84 cov 1 3 21874 cov 9 #additive 4 21874 cov 9 5 21874 cov 9 6 21874 cov 9 3 21874 cov 9 #pe 4 21874 cov 9 5 21874 cov 9 6 21874 cov 9 RANDOM\_RESIDUAL VALUES 100 RANDOM\_GROUP 6789 RANDOM\_TYPE add\_animal FILE pedirr (CO)VARIANCES (4 x 4 matrix) RANDOM\_GROUP 10 11 12 13 RANDOM\_TYPE diagonal FILE (CO)VARIANCES (4 x 4 matrix)

## Appendix F (terminal cross model)

A terminal cross model by Fernando et al. and Lo et al.

breed A:	ya	=	cga	+	ua			+	ea
breed B:	yb	=	cgb	+			ub	+	eb
cross:	yab	=	cgab	+	uaab	+	ubab	+	eab

Data file (data\_cross)

1. cg A (85 levels)

2. cg B (110 levels)

3. cg crossbred (87 levels)

4. animal - breed A (2400 animals) or parent from breed A

5. animal - breed B (3000 animals) or parent from breed B

6. ya

7. yb

8. yc

Pedigree files: pedig\_A for breed A and pedig\_B for breed B

Parameter file # Example of a terminal-cross model DATAFILE data-cross NUMBER\_OF\_TRAITS 3 NUMBER\_OF\_EFFECTS 3 **OBSERVATION(S)** 678 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT [EFFECT NESTED] 1 2 3 110 cross 4042400 cross 0 5 5 3000 cross RANDOM\_RESIDUAL VALUES 100 0 0 0 100 0 00100 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE pedig\_A (CO)VARIANCES (3 x 3 matrix)

RANDOM\_GROUP 3 RANDOM\_TYPE add\_animal FILE pedig\_B (CO)VARIANCES (3 x 3 matrix)

# Appendix G (competitive model)

Example of a competitive model (a la Muir and Schinkel)

y=cg + a +c1 + c2 +..+c5 + e

ci is the effect of the i-th competitor; assumed pen size of up to 6.

```
Datafile (data_comp)

1. y

2. cg (max 120)

3. animal (max 3000)

4. competitor 1

5. c 2

...

8. c 5
```

If pen size is less than 6, unused fields set to 0.

```
Parameter file
# Example of a competitive model
DATAFILE
data_comp
NUMBER_OF_TRAITS
1
NUMBER_OF_EFFECTS
7
OBSERVATION(S)
1
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT NESTED]
2 120 cross
3 3000 cross
40 cross
                                           The 2<sup>nd</sup> effect (position 3 in the data) is additive
50 cross
                                           direct effect and 3<sup>rd</sup> to 7<sup>th</sup> effects (positions 4 to 8
60 cross
                                           in the data) are competitive effects (animal ID for
70 cross
                                           competitors).
8 3000 cross
RANDOM_RESIDUAL VALUES
50
RANDOM_GROUP
23
RANDOM_TYPE
add_animal
FILE
```

pedig (CO)VARIANCES 40 -10 -10 10 The covariance matrix contains variance for the second effect, variance for effects 3 to 7 (accumulated to 7), and covariance between direct and competitive effects.

# Appendix H (genomic model)

# Example of evaluation /variance component estimation using phenotypic, pedigree and genomic information in single-step evaluation

Files simulated by Huiyu Wang using program QMSim by Mehdi Sargolzaei & Flavio Schenkel.

### Parameter file for renumbering program RENUMF90

DATAFILE phenotypes.txt TRAITS 3 FIELDS\_PASSED TO OUTPUT

WEIGHT(S)

RESIDUAL\_VARIANCE 0.9038 EFFECT 1 cross alpha #fixed effect EFFECT 2 cross alpha #animal RANDOM animal FILE pedigree SNP\_FILE marker.geno.clean (CO)VARIANCES 0.9951E-01

### Phenotype file

phenotypes.txt

1 1	1 2	4. 3.	16 47	0 0
1	3	4.	5 (	D
1	4	4.	97	0
1	5	5.	98	0
1	6	6.	63	0
1	7	з.	32	0
1	8	5.	85	0
1	9	4.	77	0
1	10	) 4	1.2	20

### **Pedigree file**

### pedigree

Phenotypes.txt – phenotype file Single trait in position 3 Fixed effect in position 1 read as alphanumeric Random animal effect in position 3 Pedigree file pedigrees SNP file marker.geno.clean

#### SNP file for the first 50 SNP

#### \$cut -c1-50 marker.geno.clean|head -10

#### **Run RENUMF90**

```
RENUMF90 version 1.86
name of parameter file?renum.par
renum.par
datafile:phenotypes.txt
traits:
                3
fields passed:
                        4
R
 0.9038
Processing effect 1 of type cross
item_kind=alpha
Processing effect 2 of type cross
item kind=alpha
pedigree file name "pedigree"
positions of animal, sire, dam, alternate dam and yob
                                                            1
                                                                          2
         3
                    0
                                 0
SNP file name "marker.geno.clean"
all pedigrees to be included
Reading (CO) VARIANCES:
                                1 x
                                             1
Maximum size of character fields: 20
Maximum size of record (max string readline): 800
Maximum number of fields innput file (max field readline): 100
hash tables for effects set up
table expanded from 10000 to
                                          20000 records
table expanded from
                          20000 to
                                           40000 records
           15800 records
read
table with
                     1 elements sorted
added count
Effect group
                      1 of column
                                              1 with
                                                                 1 levels
table expanded from
                          10000 to
                                           10000 records
added count
Effect group
                       2 of column
                                              1 with
                                                             15800 levels
wrote statistics in file "renf90.tables"
Basic statistics for input data (missing value code is 0)
Pos Min
                                      SD
                            Mean
                Max
                                                          N
 3
    0.73000
                 8.8300
                              4.9793
                                         1.0069
                                                      15800
```

```
random effect with SNPs 2
type: animal
file: marker.geno.clean
read SNPs 1500 records
                                          1 with
Effect group
                     2 of column
                                                            15800 levels
random effect 2
type:animal
opened output pedigree file "renadd02.ped"
           15800 pedigree records
read
Pedigree checks
Number of animals with records:
                                    15800
                                      1500
Number of animals with genotypes:
Number of animals with records or genotypes:
                                                 15800
Number of animals with genotypes and no records
                                                        0
                                                        0
Number of parents without records or genotypes:
Total number of animals:
                            15800
Wrote cross reference IDs for SNP file "marker.geno.clean XrefID"
Wrote parameter file "renf90.par"
Wrote renumbered data "renf90.dat"
```

Parameter file for application programs with renumbered fields

### renf90.par

```
# BLUPF90 parameter file created by RENF90
DATAFILE
renf90.dat
NUMBER_OF_TRAITS
    1
NUMBER_OF_EFFECTS
    2
OBSERVATION(S)
    1
WEIGHT(S)
```

```
renf90.dat – phenotype file
Single trait in position 1
Two effects in model
Fixed effect in position 1 cross-classified with 1 level (μ)
Animal effect in position 3
Second effect (Random Group 2) is additive-animal with
renadd02.ped – pedigree file
SNP file marker.geno.clean
```

#### EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT[EFFECT NESTED]

2 1 cross 3 15800 cross RANDOM\_RESIDUAL VALUES 0.9038 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE renadd02.ped (CO)VARIANCES 0.9951E-01 OPTION SNP\_file marker.geno.clean

**Renumbered pedigree file** 

renadd02.ped

```
1 5742 14705 1 0 2 1 0 0 14670
2 2302 1384 1 0 2 1 0 0 12367
3 4248 15309 1 0 12 1 0 2 9123
4 4241 3492 1 0 2 1 0 0 7455
5 14459 14202 1 0 2 1 0 0 5736
6 1029 1292 1 0 2 1 0 3 5877
7 10876 7596 1 0 2 1 0 0 9638
8 13589 12642 1 0 2 1 0 0 14136
9 7070 11562 1 0 2 1 0 0 6010
10 6449 2448 1 0 2 1 0 0 15498
```

#### **Renumbered phenotype file**

#### renf90.dat

 $\begin{array}{cccccc} 4.16 & 1 & 5903 & 0 \\ 3.47 & 1 & 3628 & 0 \\ 4.5 & 1 & 1329 & 0 \\ 4.97 & 1 & 14808 & 0 \\ 5.98 & 1 & 12481 & 0 \\ 6.63 & 1 & 10205 & 0 \\ 3.32 & 1 & 7935 & 0 \\ 5.85 & 1 & 5639 & 0 \\ 4.77 & 1 & 3348 & 0 \\ 4.22 & 1 & 1951 & 0 \end{array}$ 

#### **Run BLUPF90**

```
name of parameter file?renf90.par
* SNP file: marker.geno.clean
 * SNP Xref file: marker.geno.clean XrefID
 * Frequency to Center Z=M-p to create G=ZZ'/k (default whichfreq = 2):
         2
    BLUPF90 1.42
Parameter file:
                            renf90.par
Data file:
                            renf90.dat
Number of Traits
                             1
Number of Effects
                             2
Position of Observations
                              1
Position of Weight (1)
                              0
Value of Missing Trait/Observation
                                             0
EFFECTS
# type
                       position (2)
                                         levels [positions for nested]
1 cross-classified
                        2
                                                                                  1
2 cross-classified
                        3
                                                                              15800
Residual (co)variance Matrix
0.90380
Random Effect(s) 2
Type of Random Effect:
                            additive animal
Pedigree File:
                            renadd02.ped
                  (CO) VARIANCES
 trait effect
        2 0.9951E-01
 1
REMARKS
  (1) Weight position 0 means no weights utilized
  (2) Effect positions of 0 for some effects and traits means that such
     effects are missing for specified traits
Data record length =
                                3
 # equations =
                    15801
G
0.99510E-01
```

15800 records in 3.5994001E-02 s, 31601 nonzeroes read 15800 additive pedigrees read \*-----\* \* Setup Genomic: Version 1.76 \* \* Modified relationship matrix (H) created for effect: 2 \*\_\_\_\_\_\* Read 15800 animals from pedigree file Pedigree was in not chronological order (parent first format), reodering will be performed !!! Current OPTIONS Genomic Matrix Make/Read Which Save Test File StorageType 1 F F G densem Make Rel. Matrix A22 Make/Read Which Save Test File StorageType 4 F F A22 densem Make Inv. Genomic Matrix Make/Read Which Save Test File StorageType F F Gi densem Make 9 Inv. Rel. Matrix A22 StorageType Make/Read Which Save Test File 9 F F A22i densem Make Genomic - A22 Matrix Make/Read Which Save Test File StorageType None 9 F F GmA22 densem Inv. Genomic- A22 Matrix Make/Read Which Save Test File StorageType Make 0 F F GimA22i densem Other options Allele Frequency file: freqdata Center Allele Frequency: 2 Scale Allele Frequency: 2 Scale Method: 1 Regression G on A: F 2 Tuned G Method: Creation of GimA22i tau inv(alpha G + beta A22 + gamma I + delta) - omega inv(A22) alpha,beta 0.950 0.050 gamma,delta 0.000 0.000 1.000 1.000 tau, omega Number of Genotyped Animals 1500 Creating A22 Extracting subset of: 3432 pedigrees from: 15800 elapsed time: 0.0000 Calculating Inbreeding by M&L function.. elapsed time 1.0000020E-03 Calculating A22 Matrix by Colleau ...elapsed time 0.3299500 Statistics for A22 Statistic of Rel. Matrix A22 
 Min
 Max

 1.000
 1.250

 0.000
 0.750

 N
 Mean
 Min

 Diagonal
 1500
 1.001
 1.000

 Off-diagonal
 2248500
 0.003
 0.000
 Var 0.000 0.001

Statistics for SNP file

Reading SNP file

Column position in file for the first marker: 7 Format to read SNP file: (6x,400000i1) Number of SNPs : 3000 Number of Genotyped animals: 1500 Reading SNP file elapsed time 0.4639290 Statistics of alleles frequencies in the current population 3000 N: 0.501 Mean: Several quality checks performed; no error messages as all files for this Min: 0.132 0.890 Max: example have been simulated Var: 0.014 Quality Control - Check call rate for animals Quality Control - Check Parent-Progeny Mendelian conflicts Total animals: 15800 - Genotyped animals: 1500 Number of Individual - Sire pairs: 470 Number of Individual - Dams pairs: 256 Number of Individual - Sire - Dam trios: 152 Checking SNPs for Mendelian conflicts 726 Total number of parent-progeny evaluations: Number of SNPs with Mendelian conflicts: 0 Checking Animals for Mendelian conflicts Statistics of alleles frequencies in the current population after Quality Control (MAF, monomorphic, call rate) N: 3000 Mean: 0.501 Min: 0.132 Max: 0.890 Var: 0.014 Locus Freq 0-2p 1-2p 2-2p 1 0.751333 -1.502667 -0.502667 0.497333 2 0.382333 -0.764667 0.235333 1.235333 3 0.568667 -1.137333 -0.137333 0.862667 4 0.680000 -1.360000 -0.360000 0.640000 5 0.184333 -0.368667 0.631333 1.631333 6 0.298333 -0.596667 0.403333 1.403333 7 0.392000 -0.784000 0.216000 1.216000 8 0.379667 -0.759333 0.240667 1.240667 9 0.596667 -1.193333 -0.193333 0.806667 10 0.352333 -0.704667 0.295333 1.295333 Genotypes missings (%): 0.000000E+00 Average denom. (scale): 1415.90178466665 Center Matrix elapsed: 8.3986998E-02 Creating G Matrix Calculating G Matrix Wall time: 08-05-2011 16h 57m 34s 213 MMP - OPTML Elapsed time 18.47419 Wall time: 08-05-2011 16h 58m 09s 371 Statistics of G calculated assuming current allele frequencies Statistic of Genomic Matrix N Mean Min Max Var 1500 0.999 0.889 1.463 0.002 Diagonal

Correlation of Genomic Inbreeding and Pedigree Inbreeding

-0.001

-0.147

0.830

0.002

2248500

Off-diagonal

Correlation: 0.3220 All elements - Diagonal / Off-Diagonal Estimating Regression Coefficients G = b0 11' + b1 A + e Regression coefficients b0 b1 = -0.004 0.997 Correlations of off-diagonal elements of G Correlation all elements G & A 0.644 and A22 is 0.660; low numbers indicated genotyped mistakes Off-Diagonal or poor pedigrees Using 70386 elements from A22 >= 0.02000 Estimating Regression Coefficients G = b0 11' + b1 A + e Regression coefficients b0 b1 = -0.006 1.000 Correlation Off-Diagonal elements G & A 0.660 Blend G as alpha\*G + beta\*A22: (alpha,beta) 0.950 0.050 Statistic of Genomic Matrix N Mean Min Max Var Diagonal 1500 0.999 0.894 1.446 0.002 Off-diagonal 2248500 0.000 -0.139 0.820 0.002 Frequency - Diagonal of G N: 1500 Diagonal elements of G should be 1± 0.2. Too large or Mean: 0.999 too small elements indicate: Min· 0.894 Max: 1.446 **Genotyping mistakes** Range: 0.028 **Mixed lines** Class: 20 See Simeone et al. (2011) #Class Class Count 1 0.8942 9 2 0.9218 86 3 0.9494 343 4 0.9770 480 1.005 5 361 6 1.032 139 1.060 7 51 8 1.087 16 9 1.115 6 10 1.142 2 1.170 11 1 12 1.198 1 1.225 1.253 13 1 14 1 15 1.280 0 1.308 16 0 17 1.336 0 1.363 18 2 19 1.391 0 1.418 20 1 21 1.446 0 Scale G matrix according to A22 - Method: 2 0.003 0.004 0.998 Diagonal A: 1.001 Offdiagonal A: All A: Difference: Diagonal G: 0.999 Offdiagonal G: 0.000 All G: 0.000 Difference: 0.999 0.999 Diff G Diag - G OffDiag: (da-oa)/(dg-og): 0.998 Diff A OffDiag - G OffDiag: 0.004 Diff A all - G all: 0.004 New Alpha: 0.948 New Beta: 0.050 :New Delta 0.004 Final Pedrigree-Based Matrix 

Statistic of Rel. Matrix A22

Diagonal Off-diagonal	N 1500 2248500	Mean 1.001 0.003	Min 1.000 0.000	Max 1.250 0.750	Var 0.000 0.001
Statistics of G after so Statistics should be s	caling as in Ch ame as for A2	en et al (20) 2.	11) or Vitezi	ca et al. (20	11)
Final Genomic Matr					
Statistic of Genomi	c Matrix				
Diagonal Off-diagonal	N 1500 2248500	Mean 1.001 0.003	Min 0.896 -0.134	Max 1.447 0.822	Var 0.002 0.002
Correlation of Genc Correlation:	mic Inbreedi 0.3363	ing and Peo	ligree Inbı	reeding	
All elements - Diag Estimating Regre Regression coeff	onal / Off-I ssion Coeffi icients b0 b	Diagonal icients G = D1 = (	= b0 11' + ).000 (	b1 A + e ).995	
Correlation all	elements G &	A 0.0	563		
Off-Diagonal Using 70386 elem	ents from A2	22 >= 0.020	000		
Estimating Regre Regression coeff	ession Coeffi ficients b0 b	icients G = o1 = -(	= b0 11' + ).001 (	b1 A + e ).998	
Correlation Off-	Diagonal ele	ements G &	A 0.67	9	
Creating A22-invers Wall time: 08-05 Inverse using ginv2 elapsed time 3.54 Wall time: 08-05	e -2011 16h 5 446100000000 -2011 16h 5	58m 10s 869 ) 58m 17s 693	5 L		
Statistics of A <sub>22</sub> -1					
Statistic of Inv. F	el. Matrix A	422			
Diagonal Off-diagonal	N 1500 2248500	Mean 1.607 -0.001	Min 1.056 -1.067	мах 9.221 0.533	0.575 0.001
Creating G-inverse Wall time: 08-05 Inverse using ginv2 elapsed time 4.24 Wall time: 08-05	-2011 16h 5 6 635400000000 -2011 16h 5	58m 17s 98' ) 58m 26s 044	7		

```
Statistics of G<sup>-1</sup>
2 x diag(G<sup>-1</sup> - A<sub>22</sub><sup>-1</sup>) is approx. measure of extra genomic info in terms of effective daughters
```

Statistic of Inv. Genomic Matrix N 1500 Min 3.597 Mean Diagonal 8.007

	N	Mean	Min	Max	Var
Diagonal	1500	8.007	3.597	64.893	21.055
Off-diagonal	2248500	-0.005	-12.697	6.632	0.056

Creating GimA22i in file: "GimA22i" Calculating GmA22/GimA22i Matrix Densem storage Calculating GmA22/GimA22i Matrix...elapsed time 0.1269817

```
Setup Genomic Done.
wGimA22i 1.0000000000000
hash matrix increased from 100000 to 150000 % filled:
                                                          0.9000
hash matrix increased from 150000 to 225000 % filled:
                                                          0.9000
                                                           0.9000
hash matrix increased from 225000 to 337500 % filled:
hash matrix increased from 337500 to 506250 % filled:
                                                           0.9000
hash matrix increased from 506250 to 759375 % filled:
                                                           0.9000
hash matrix increased from 759375 to 1139062 % filled:
                                                           0.9000
hash matrix increased from 1139062 to 1708593 % filled:
                                                            0.9000
finished peds in 30.68333
                               s, 1193064 nonzeroes
                1 convergence= 3.234776127905992E-004
round
                  2 convergence= 1.615955145159698E-005
round
                      convergence= 9.675137058360991E-006
convergence= 6.533482675941447E-006
round
                 3
round
                  4
                 5
                      convergence= 2.711751165983321E-006
round
..... . .
..... . .
                      convergence= 2.721030958617683E-012
                 64
round
                       convergence= 1.931029578758311E-012
round
                 65
                      convergence= 1.610472992188148E-012
convergence= 1.259204136643006E-012
round
                 66
                 67
round
                      convergence= 9.025592862452768E-013
round
                 68
          68 iterations, convergence criterion= 9.025592862452768E-013
 solutions stored in file: "solutions"
 Solution file
solutions
trait/effect level solution
                    4.97591211
  1 1 1
                      0.10194865
0.33749439
0.04475742
  1
      2
               1
              2
3
  1
      2
     2
  1
               4
                      -0.31055520
  1
     2
  12
                5
                       0.22368631
   1
      2
                 6
                       -0.09454804
     2
                      -0.03186435
                7
  1
   1
      2
                 8
                       0.18033163
 Variance component estimation by AIREMLF90
name of parameter file?renf90.par
* SNP file: marker.geno.clean
```

```
* SNP Xref file: marker.geno.clean XrefID
 * Frequency to Center Z=M-p to create G=ZZ'/k (default whichfreq = 2):
          2
     AI-REMLF90 ver. 1.96
                             renf90.par
Parameter file:
Data file:
                             renf90.dat
Number of Traits
                              1
Number of Effects
                              2
                            1
Position of Observations
Position of Weight (1)
                               0
Value of Missing Trait/Observation
                                              0
····· • •
..... . .
Statistic of Inv. Genomic Matrix
                           N
                                   Mean
                                             Min
                                                        Max
                                                                  Var
                         1500
                                  8.007
                                            3.597
                                                     64.893
                                                               21.055
     Diagonal
     Off-diagonal
                     2248500
                                 -0.005
                                         -12.697
                                                      6.632
                                                                0.056
```

Creating GimA22i in file: "GimA22i"
Calculating GmA22/GimA22i Matrix Densem storage Calculating GmA22/GimA22i Matrix...elapsed time 0.1089821 Setup Genomic Done. wGimA22i 1.0000000000000 hash matrix increased from 85428 to 128142 % filled: 0.9000 hash matrix increased from 128142 to 192213 % filled: 0.9000 hash matrix increased from 192213 to 288319 % filled: 0 9000 hash matrix increased from 288319 to 432478 % filled: 0.9000 hash matrix increased from 432478 to 648717 % filled: 0.9000 hash matrix increased from 648717 to 973075 % filled: 0.9000 hash matrix increased from 973075 to 1459612 % filled: 0.9000 hash matrix increased from 85428 to 128142 % filled: 0.9000 hash matrix increased from 128142 to 192213 % filled: 0.9000 hash matrix increased from 192213 to 288319 % filled: 0.9000 hash matrix increased from 288319 to 432478 % filled: 0.9000 hash matrix increased from 432478 to 648717 % filled: 0.9000 hash matrix increased from 648717 to 973075 % filled: 0.9000 hash matrix increased from 973075 to 1459612 % filled: 0.9000 1193064 nonzeroes 32.01313 finished peds in s, rank= 15801 \*\*\*\*\* \*\*\*\* FSPAK \*\*\* \*\*\*\*\* MPE / IM / MAE Jun 1994 SPARSE STATISTICS 15801 DIMENSION OF MATRIX = RANK 15801 STORAGE AVAILABLE = 7061497 MAXIMUM NEEDED \_ 7061497 NZE IN UPPER TRIANGULAR = 1208865 = NZE IN FACTOR 1521840 NO. OF CALLS NUM FACT = 1 NO. OF CALLS SOLVE = 1 NO. OF CALLS SPARS SOLV = 0 NO. OF CALLS DET / LDET = 1 NO. OF CALLS SPARS INV = 1 TOTAL CPU TIME IN FSPAK = 9.465561 TIME FOR FINDING ORDER = 2.568611 TIME FOR SYMBOLIC FAC = 0.676899 TIME FOR NUMERICAL FAC = 2.017693 TIME FOR SOLVE = 0.008995 TIME FOR SPARSE SOLVE = 0.00000 
 TIME FOR SPARSE INVERSE =
 4.147369

 -2logL =
 43515.7413644011
 : AIC =
 43519.7413644011
 In round 1 convergence= 0.423851780381002 delta convergence= 0.252173522062583 new R 0.58510 new G 0.28516 53013.2734486053 : AIC = 53017.2734486053 -21ogL = 2 convergence= 0.141351613622645 In round delta convergence= 0.117430758820623 new R 0.52205 new G 0.45696 52800.6601605267 : AIC = 52804,6601605267 -21ogL = 3 convergence= 1.725330565925358E-002 In round delta convergence= 4.769938966058494E-002 new R 0.49575 new G 0.52606 -21ogL = 52785.2479463395 : AIC = 52789.2479463395 4 convergence= 1.101891763451498E-004 In round delta convergence= 3.662497104484009E-003 new R 0.49400

```
new G
0.53164
-2logL = 52785.1635385807 : AIC = 52789.1635385807
In round 5 convergence= 2.804695847240073E-009
delta convergence= 1.777604045032979E-005
new R
0.49400
new G
0.53167
```

**Estimates of variance components** 

```
Final Estimates
Genetic variance(s) for effect 2
 0.53167
Residual variance(s)
 0.49400
inverse of AI matrix (Sampling Variance)
0.40448E-03 -0.17367E-03
-0.17367E-03 0.14702E-03
Correlations from inverse of AI matrix
             -0.71219
  1.0000
-0.71219
                1.0000
SE for R
 0.12125E-01
SE for G
 0.20112E-01
solutions stored in file: "solutions"
```

# Appendix I (complete genomic analysis)

Data files are available at http://nce.ads.uga.edu/wiki/doku.php?id=course\_materials\_-\_from\_uga\_2014.

Using RENUMF90, PREGSF90, BLUPF90 (BLUP), BLUPF90 (ssGBLUP), PREDICTF90, POSTGSF90 (ssGWAS)

# **Simulated data**

Single trait with heritability of 0.30 and phenotypic variance = 1.0 Five generations Total of 994 parents from generations 1 to 4 were genotyped Three hundred progeny from 5<sup>th</sup> generation had genotypes and pedigree, but phenotypes were removed for traditional and genomic evaluations

Data Structure:

#Animal Generation Sex Mu QTL Residual Phenotype
1 0 1 1 -0.826104 1.586661 1.76056
2 0 1 1 -1.093034 -0.451821 -0.544855
3 0 1 1 -0.135824 0.984936 1.84911
4 0 1 1 0.044242 -0.802145 0.242097
5 0 1 1 0.342068 0.028434 1.3705
...
6095 5 1 1 1.801324 -0.494822 2.3065
6096 5 2 1 0.772964 0.791936 2.5649
6097 5 2 1 0.748241 0.285815 2.03406
6098 5 1 1 1.042522 -1.606656 0.435866
6099 5 1 1 0.891319 0.179843 2.07116
6100 5 1 1 0.745873 0.034715 1.78059

Pedigree: 6100 animals

#Animal Sire Dam

Genotypes: 1294 animals genotyped for 1000 SNP across 5 chromosomes # Animal SNP<sub>1</sub>SNP<sub>2</sub>SNP<sub>3</sub>SNP<sub>4</sub>SNP<sub>5</sub>...SNP<sub>1000</sub> 6100 22212...1

(Phenotype = Mu + QTL + Residual)

112

# Parameter file for RENUMF90

DATAFILE newdata.txt TRAITS 7 FIELDS\_PASSED TO OUTPUT 2 WEIGHT(S) **RESIDUAL\_VARIANCE** 0.70 EFFECT 4 cross alpha #mu EFFECT 1 cross alpha #animal RANDOM animal FILE ped.txt FILE\_POS 12300 SNP\_FILE snp.txt PED\_DEPTH 0 (CO)VARIANCES 0.30 **OPTION** map\_file map.txt

#### Log file for RENUMF90

RENUMF90 version 1.104 name of parameter file? renum.par datafile:newdata.txt traits: 7 fields passed: 2 R 0.7000 Processing effect 1 of type cross item\_kind=alpha Processing effect 2 of type cross

item kind=alpha pedigree file name "ped.txt" positions of animal, sire, dam, alternate dam and yob 1 2 3 0 0 SNP file name "snp.txt" all pedigrees to be included Reading (CO) VARIANCES: 1 x 1 Maximum size of character fields: 20 Maximum size of record (max\_string\_readline): 800 Maximum number of fields for input file (max\_field\_readline): 100 hash tables for effects set up read 6100 records table with 1 elements sorted added count Effect group 1 of column 1 with 1 levels 10000 records table expanded from 10000 to added count Effect group 2 of column 1 with 6100 levels wrote statistics in file "renf90.tables" Basic statistics for input data (missing value code is 0) Pos Min Max Mean SD N -2.8883 5.0863 1.0042 0.99034 6100 7 random effect with SNPs 2 type: animal file: snp.txt read SNPs 1294 records Effect group 2 of column 1 with 6100 levels random effect 2 type:animal opened output pedigree file "renadd02.ped" 6100 pedigree records read Pedigree checks Number of animals with records: 6100 Number of animals with genotypes: 1294 6100 Number of animals with records or genotypes: Number of animals with genotypes and no records 0 Number of parents without records or genotypes: 0 6100 Total number of animals: Wrote cross reference IDs for SNP file "snp.txt\_XrefID" Wrote parameter file "renf90.par" Wrote renumbered data "renf90.dat" Parameter file for PREGSF90 without quality control DATAFILE renf90.dat

NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 **OBSERVATION(S)** 1 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT[EFFECT NESTED] 2 1 cross 3 6100 cross RANDOM\_RESIDUAL VALUES 0.70000 RANDOM\_GROUP 2 **RANDOM TYPE** add animal FILE renadd02.ped (CO)VARIANCES 0.30000 **OPTION SNP\_file snp.txt OPTION** map\_file map.txt

#### Log file for PREGSF90 without quality control

**OPTION no\_quality\_control** 

```
name of parameter file?
renf90.par
    preGS 1.10
 Parameter file:
                            renf90.par
Data file:
                            renf90.dat
Number of Traits
                             1
Number of Effects
                             2
Position of Observations
                             1
Position of Weight (1)
                             0
Value of Missing Trait/Observation
                                            0
EFFECTS
 # type
                       position (2)
                                          levels
                                                   [positions for nested]
1 cross-classified
                        2
                                                                                 1
2 cross-classified
                                                                              6100
                        3
Residual (co)variance Matrix
0.70000
Random Effect(s) 2
                          additive animal
Type of Random Effect:
 Pedigree File:
                           renadd02.ped
 trait effect (CO) VARIANCES
 1
         2 0.3000
REMARKS
  (1) Weight position 0 means no weights utilized
  (2) Effect positions of 0 for some effects and traits means that such
     effects are missing for specified traits
Options read from parameter file:
* SNP file: snp.txt
```

```
* SNP Xref file: snp.txt XrefID
* Map file: map.txt
* No Quality Control Checks !!!!! (default .false.): T
*
                Genomic Library: Version 1.164
 *
 *
                  Optimized OpenMP Version
                                                        *
* Modified relationship matrix (H) created for effect:
                                                   2
*_____*
Read 6100 animals from pedigree file: "renadd02.ped"
Number of Genotyped Animals: 1294
Creating A22
   Extracting subset of: 2312 pedigrees from: 6100 elapsed time:
                                                              0.0150
   Calculating A22 Matrix by Colleau OpenMP...elapsed time: .0190
   Numbers of threads=8 16
Reading SNP file
   Column position in file for the first marker: 8
   Format to read SNP file: (7x,400000i1)
   Number of SNPs: 1000
   Number of Genotyped animals: 1294
   Reading SNP file elapsed time: .06
Statistics of alleles frequencies in the current population
              1000
   N:
             0.504
   Mean:
   Min:
             0.043
             0.929
   Max:
             0.032
   Var:
Reading MAP file: "map.txt" - 1000 SNPs out of 1000
   Min and max # of chromosome: 1 5
   Min and max # of SNP: 1 1000
Genotypes missings (%): 0.000
Calculating G Matrix
   Dgemm MKL #threads=
                        8 16 Elapsed omp_get_time:
                                                      0.7359
Scale by Sum(2pq). Average: 435.221580281360
Blend G as alpha*G + beta*A22: (alpha,beta) 0.950 0.050
Frequency - Diagonal of G
   N:
           1294
            0.999
   Mean:
   Min:
              0.895
             1.468
   Max:
   Range:
              0.029
           20
   Class:
#Class
          Class Count
      1 0.8949
                  27
      2 0.9236
                     109
      3 0.9523
                     300
```

380

4 0.9810

115

5	1.010	287
6	1.038	137
7	1.067	33
8	1.096	14
9	1.124	3
10	1.153	1
11	1.182	0
12	1.210	2
13	1.239	0
14	1.268	0
15	1.296	0
16	1.325	0
17	1.354	0
18	1.382	0
19	1.411	0
20	1.440	1
21	1.468	0

Check for diagonal of genomic relationship matrix

Check for diagonal of genomic relationship matrix, genotypes not removed: 0

```
Final Pedrigree-Based Matrix
```

-----

```
Statistic of Rel. Matrix A22
                  N Mean
1294 1.001
                                                      Var
                            Mean
                                     Min
                                              Max
                                   1.000
    Diagonal
                                          1.250
                                                    0.000
    Off-diagonal 1673142 0.005 0.000
                                          0.750
                                                    0.001
-----
 Final Genomic Matrix
------
Statistic of Genomic Matrix
                 N Mean
1294 1.001
                           Mean
                                     Min
                                             Max
                                                      Var
    Diagonal
                                   0.898
                                             1.469
                                                     0.002
    Off-diagonal 1673142 0.005 -0.158 0.791
                                                    0.002
Correlation of Genomic Inbreeding and Pedigree Inbreeding
    Correlation: 0.2177
All elements - Diagonal / Off-Diagonal
   Estimating Regression Coefficients G = b0 11' + b1 A + e
   Regression coefficients b0 b1 = 0.000 0.991
   Correlation all elements G & A 0.717
Off-Diagonal
   Using 83426 elements from A22 >= .02000
   Estimating Regression Coefficients G = b0 11' + b1 A + e
   Regression coefficients b0 b1 = -0.003 0.999
   Correlation Off-Diagonal elements G & A
                                      0.777
Creating A22-inverse
   Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp get time:
                                                                  0.1071
------
```

Final A22 Inv Matrix ------Statistic of Inv. Rel. Matrix A22 
 N
 Mean
 Min
 Max
 Var

 Diagonal
 1294
 1.851
 1.067
 5.812
 0.431

 Off-diagonal
 1673142
 -0.001
 -1.200
 0.600
 0.001
 Creating G-inverse Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp\_get\_time: 0.1050 \_\_\_\_\_ Final Genomic Inv Matrix Statistic of Inv. Genomic Matrix 
 N
 Mean
 Min
 Max
 Var

 Diagonal
 1294
 13.457
 5.827
 45.588
 27.985

 Off-diagonal
 1673142
 -0.010
 -13.500
 6.896
 0.226
 Check for diagonal of Inverse Genomic - Inverse of pedigree relationship matrix Saving GimA22i in file: "GimA22i" ------Final G Inv - A22 Inv Matrix -----Statistic of Inv. Genomic- A22 Matrix N Mean Min Max Var 1294 11.606 4.746 40.310 21.707 Diagonal Off-diagonal 1673142 -0.009 -12.500 6.396 0.211 \*----\* \* Setup Genomic Done !!! \* \*----\* Parameter file for PREGSF90 with quality control DATAFILE renf90.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 **OBSERVATION(S)** 1 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT[EFFECT NESTED] 2 1 cross 3 6100 cross RANDOM\_RESIDUAL VALUES 0.70000 **RANDOM GROUP** 

2

RANDOM\_TYPE

add\_animal FILE renadd02.ped (CO)VARIANCES 0.30000 **OPTION SNP\_file snp.txt OPTION** map\_file map.txt Log file for PREGSF90 with quality control name of parameter file? renf90.par preGS 1.10 Parameter file: renf90.par Data file: renf90.dat Number of Traits 1 Number of Effects 2 1 0 Position of Observations Position of Weight (1) Value of Missing Trait/Observation 0 EFFECTS # type position (2) levels [positions for nested] 1 cross-classified 2 1 2 cross-classified 3 6100 Residual (co)variance Matrix 0.70000 Random Effect(s) 2 Type of Random Effect: additive animal Pedigree File: renadd02.ped trait effect (CO) VARIANCES 2 0.3000 1 REMARKS (1) Weight position 0 means no weights utilized (2) Effect positions of 0 for some effects and traits means that such effects are missing for specified traits Options read from parameter file: \* SNP file: snp.txt \* SNP Xref file: snp.txt\_XrefID \* Map file: map.txt \*-----\* Genomic Library: Version 1.164 \* Optimized OpenMP Version \* \* Modified relationship matrix (H) created for effect: 2 \* \*-----\* Read 6100 animals from pedigree file: "renadd02.ped" Number of Genotyped Animals: 1294

Creating A22

Extracting subset of: 2312 pedigrees from: 6100 elapsed time: 0.0160 Calculating A22 Matrix by Colleau OpenMP...elapsed time: .0189 Numbers of threads=8 16 Reading SNP file Column position in file for the first marker: 8 Format to read SNP file: (7x,400000i1) Number of SNPs: 1000 Number of Genotyped animals: 1294 Reading SNP file elapsed time: .06 Statistics of alleles frequencies in the current population N: 1000 0.504 Mean: Min: 0.043 Max: 0.929 Var: 0.032 Reading MAP file: "map.txt" - 1000 SNPs out of 1000 Min and max # of chromosome: 1 5 Min and max # of SNP: 1 1000 Quality Control - SNPs with Call Rate < callrate ( 0.90) will removed: 0 Quality Control - SNPs with MAF < minfreq ( 0.05) will removed: 1 Quality Control - Monomorphic SNPs will be removed: 0 Quality Control - Removed Animals with Call rate < callrate ( 0.90): 0 Quality Control - Check Parent-Progeny Mendelian conflicts Total animals: 6100 - Genotyped animals: 1294 - Effective: 1294 Number of pairs Individual - Sire: 450 Number of pairs Individual - Dam: 440 Number of trios Individual - Sire - Dam: 206 No sex Chromosome information is available Parent-progeny conflicts or HWE could eliminate SNPs in sex Chr Provide map information and sex Chr to checks using autosomes Checking SNPs for Mendelian conflicts Total number of effective SNP: 999 Total number of parent-progeny evaluations: 890 Number of SNPs with Mendelian conflicts: 0 Checking Animals for Mendelian conflicts Total number of effective SNP for checks on Animals: 999 Number of Parent-Progeny Mendelian Conflicts: 0 Number of effective SNPs (after QC): 999 Number of effective Indiviuals (after QC): 1294 Statistics of alleles frequencies in the current population after

Quality Control (MAF, monomorphic, call rate, HWE, Mendelian conflicts)

N: 999 Mean: 0.504 Min: 0.051 Max: 0.929 0.032 Var: Genotypes missings (%): 0.100 Genotypes missings after cleannig (%): 0.000 Calculating G Matrix Dgemm MKL #threads= 8 16 Elapsed omp\_get\_time: 0.9840 Scale by Sum(2pq). Average: 435.140185710293 Blend G as alpha\*G + beta\*A22: (alpha,beta) 0.950 0.050 Frequency - Diagonal of G N: 1294 Mean: 0.999 0.895 Min: 1.469 0.029 Max: Range: 0. 20 #Class Class Count 1 0.8951 27 2 0.9238 109 3 0.9524 304 4 0.9811 379 285 5 1.010 6 1.038 137 7 1.067 32 8 1.096 14 9 1.125 3 10 1.153 1 11 1.182 0 12 1.211 2 13 1.239 0 14 1.268 0 15 1.297 0 16 1.325 0 17 1.354 0 18 1.383 0 0 19 1.411 20 1.440 1 0 21 1.469 Check for diagonal of genomic relationship matrix Check for diagonal of genomic relationship matrix, genotypes not removed: 0 -------Final Pedrigree-Based Matrix ------Statistic of Rel. Matrix A22 N Mean Min Max Var 
 N
 Mean
 Min
 Max

 Diagonal
 1294
 1.001
 1.000
 1.250

 Off-diagonal
 1673142
 0.005
 0.000
 0.750
 0.000 0.001

-----

Final Genomic Matrix ------Statistic of Genomic Matrix N Mean Min Max Var 1.470 1294 1.001 0.898 Diagonal 0.002 0.005 -0.158 Off-diagonal 1673142 0.791 0.002 Correlation of Genomic Inbreeding and Pedigree Inbreeding Correlation: 0.2180 All elements - Diagonal / Off-Diagonal Estimating Regression Coefficients G = b0 11' + b1 A + e Regression coefficients b0 b1 = 0.000 0.991 Correlation all elements G & A 0.717 Off-Diagonal Using 83426 elements from A22 >= .02000 Estimating Regression Coefficients G = b0 11' + b1 A + e Regression coefficients b0 b1 = -0.003 0.999 Correlation Off-Diagonal elements G & A 0.777 Creating A22-inverse Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp\_get\_time: 0.1068 -----Final A22 Inv Matrix ------Statistic of Inv. Rel. Matrix A22 N Mean Min Max Var Diagonal 1294 1.851 1.067 5.812 0.431 Off-diagonal 1673142 -0.001 -1.200 0.600 0.001 Creating G-inverse Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp get time: 0.1047 \_\_\_\_\_ Final Genomic Inv Matrix -----Statistic of Inv. Genomic Matrix N Mean Min Max Var 5.863 45.587 1294 13.466 28.023 Diagonal Off-diagonal 1673142 -0.010 -13.521 0.227 6.897 Check for diagonal of Inverse Genomic - Inverse of pedigree relationship matrix Saving GimA22i in file: "GimA22i" ------Final G Inv - A22 Inv Matrix ------Statistic of Inv. Genomic- A22 Matrix N Mean Min Max Var 1294 4.782 Diagonal 11.615 40.309 21.740 Off-diagonal 1673142 -0.009 -12.521 6.397 0.211

\*----\*

```
* Setup Genomic Done !!! *
```

# Parameter file for PREGSF90 with quality control, removing SNP from chromosome 5 and saving the clean SNP file

DATAFILE renf90.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 1 WEIGHT(S)

EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT[EFFECT NESTED]

```
2
      1 cross
 3 6100 cross
RANDOM_RESIDUAL VALUES
 0.70000
RANDOM_GROUP
  2
RANDOM_TYPE
add animal
FILE
renadd02.ped
(CO)VARIANCES
 0.30000
OPTION SNP_file snp.txt
OPTION map_file map.txt
OPTION excludeCHR 5
OPTION saveCleanSNPs
```

# Log file for PREGSF90 with quality control, removing SNP from chromosome 5 and saving the clean SNP

```
file
name of parameter file?
renf90.par
    preGS 1.10
                           renf90.par
Parameter file:
Data file:
                            renf90.dat
Number of Traits
                            1
Number of Effects
                             2
Position of Observations
                             1
Position of Weight (1)
                              0
Value of Missing Trait/Observation
                                            0
EFFECTS
# type
                       position (2)
                                          levels
                                                   [positions for nested]
1 cross-classified
                        2
                                                                                 1
2 cross-classified
                        3
                                                                              6100
```

```
Residual (co)variance Matrix
0.70000
Random Effect(s)
                2
Type of Random Effect:
                        additive animal
Pedigree File:
                         renadd02.ped
trait effect (CO) VARIANCES
       2 0.3000
 1
REMARKS
  (1) Weight position 0 means no weights utilized
  (2) Effect positions of 0 for some effects and traits means that such
     effects are missing for specified traits
Options read from parameter file:
* SNP file: snp.txt
* SNP Xref file: snp.txt XrefID
* Map file: map.txt
 * Save Clean SNP data to (SNP file) clean file (default .false.)
 * Exclude Chromosomes (default .false.): 5
 *-----*
                 Genomic Library: Version 1.164
 *
 *
                   Optimized OpenMP Version
 * Modified relationship matrix (H) created for effect: 2
 *-----*
Read 6100 animals from pedigree file: "renadd02.ped"
Number of Genotyped Animals: 1294
Creating A22
   Extracting subset of: 2312 pedigrees from: 6100 elapsed time:
                                                                0.0150
   Calculating A22 Matrix by Colleau OpenMP...elapsed time: .0190
   Numbers of threads=8 16
Reading SNP file
   Column position in file for the first marker: 8
   Format to read SNP file: (7x,40000011)
   Number of SNPs: 1000
   Number of Genotyped animals: 1294
   Reading SNP file elapsed time: .06
Statistics of alleles frequencies in the current population
              1000
   N:
              0.504
   Mean:
             0.043
   Min:
   Max:
             0.929
   Var:
              0.032
Reading MAP file: "map.txt" - 1000 SNPs out of 1000
   Min and max # of chromosome: 1 5
   Min and max # of SNP: 1 1000
Excluded 199 SNPs from 1 chromosomes: 5
Quality Control - SNPs with Call Rate < callrate ( 0.90) will removed: 199
```

Quality Control - SNPs with MAF < minfreq ( 0.05) will removed: 1 Quality Control - Monomorphic SNPs will be removed: 0 Quality Control - Removed Animals with Call rate < callrate ( 0.90): 0 Quality Control - Check Parent-Progeny Mendelian conflicts Total animals: 6100 - Genotyped animals: 1294 - Effective: 1294 Number of pairs Individual - Sire: 450 Number of pairs Individual - Dam: 440 Number of trios Individual - Sire - Dam: 206 No sex Chromosome information is available Parent-progeny conflicts or HWE could eliminate SNPs in sex Chr Provide map information and sex Chr to checks using autosomes Checking SNPs for Mendelian conflicts Total number of effective SNP: 801 Total number of parent-progeny evaluations: 890 Number of SNPs with Mendelian conflicts: 0 Checking Animals for Mendelian conflicts Total number of effective SNP for checks on Animals: 801 Number of Parent-Progeny Mendelian Conflicts: 0 Number of effective SNP was reduced to 801 Number of effective SNPs (after QC): 801 after removing chromosome 5 Number of effective Indiviuals (after QC): 1294 Statistics of alleles frequencies in the current population after Quality Control (MAF, monomorphic, call rate, HWE, Mendelian conflicts) N: 801 0.503 Mean: Min: 0.051 Max: 0.928 Var: 0.032 List of SNPs removed in: "snp.txt\_SNPs\_removed" Clean genotype file was created: "snp.txt\_clean" New files with clean genotypes Cross reference ID file was created: "snp.txt\_clean\_XrefID" Genotypes missings (%): 19.900 Genotypes missings after cleannig (%): 0.000 Calculating G Matrix Dgemm MKL #threads= 8 16 Elapsed omp\_get\_time: 0.8764 Scale by Sum(2pq). Average: 349.571560214902 Blend G as alpha\*G + beta\*A22: (alpha,beta) 0.950 0.050 Frequency - Diagonal of G N: 1294 Mean: 1.000

Min:		0.874	
Max:		1.593	
Range :	:	0.036	
Class	2	0	
#Class	C	lass	Count
1	0.8741		17
2	0.9100		107
3	0.9460		341
4	0.9819	1	419
5	1.018		281
6	1.054		98
7	1.090		20
8	1.126		4
9	1.162		4
10	1.198		1
11	1.234		0
12	1.270		1
13	1.306		0
14	1.342		0
15	1.377		0
16	1.413		0
17	1.449		0
18	1.485		0
19	1.521		0
20	1.557		1
21	1.593		0

Check for diagonal of genomic relationship matrix

Check for diagonal of genomic relationship matrix, genotypes not removed:  $\boldsymbol{0}$ 

-----Final Pedrigree-Based Matrix -----Statistic of Rel. Matrix A22 
 N
 Mean
 Min
 Max
 Var

 Diagonal
 1294
 1.001
 1.000
 1.250
 0.000
 Off-diagonal 1673142 0.005 0.000 0.750 0.001 -----Final Genomic Matrix ------Statistic of Genomic Matrix N Mean Min Max Var 1294 1.001 0.876 1.593 0.002 Diagonal Off-diagonal 1673142 0.005 -0.169 0.861 0.003 Correlation of Genomic Inbreeding and Pedigree Inbreeding Correlation: 0.2092 All elements - Diagonal / Off-Diagonal Estimating Regression Coefficients G = b0 11' + b1 A + e Regression coefficients b0 b1 = 0.000 0.991 Correlation all elements G & A 0.677 Off-Diagonal Using 83426 elements from A22 >= .02000

```
Estimating Regression Coefficients G = b0 11' + b1 A + e
   Regression coefficients b0 b1 = -0.002 0.996
   Correlation Off-Diagonal elements G & A 0.742
Creating A22-inverse
   Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp_get_time:
                                                                           0.1409
 -----
 Final A22 Inv Matrix
 ------
Statistic of Inv. Rel. Matrix A22

        N
        Mean
        Min
        Max
        Var

        Diagonal
        1294
        1.851
        1.067
        5.812
        0.431

        Off-diagonal
        1673142
        -0.001
        -1.200
        0.600
        0.001

Creating G-inverse
   Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp_get_time: 0.1370
 -----
 Final Genomic Inv Matrix
 -----
Statistic of Inv. Genomic Matrix
                   N Mean Min Max
1294 17.075 7.840 56.092
                                                              Var
                                                          43.645
    Diagonal
    Off-diagonal 1673142 -0.013 -16.499
                                                 8.893
                                                            0.309
Check for diagonal of Inverse Genomic - Inverse of pedigree relationship matrix
Saving GimA22i in file: "GimA22i"
 -----
 Final G Inv - A22 Inv Matrix
 ------
Statistic of Inv. Genomic- A22 Matrix
                       N Mean
                                         Min Max
                                                             Var
                     1294 15.223 6.759 51.043 35.648
    Diagonal
    Off-diagonal 1673142 -0.012 -15.499 8.393 0.289
*----*
* Setup Genomic Done !!! *
*----*
```

# Parameter file for PREGSF90 with quality control and PCA analysis

Include extra option: OPTION plotpca



# Parameter file for BLUPF90 without genomic information



name of parameter file?

```
renf90.par
* convergence criterion (default=1e-12): 1.000000E-15
    BLUPF90 1.48
                          renf90.par
Parameter file:
Data file:
                          renf90 5.dat
Number of Traits
                           1
Number of Effects
                          2
                          1
Position of Observations
Position of Weight (1)
                           0
Value of Missing Trait/Observation
                                          0
EFFECTS
# type
                     position (2)
                                      levels [positions for nested]
1 cross-classified
                      2
2 cross-classified
                       3
                                                                          6100
Residual (co)variance Matrix
0.70000
Random Effect(s) 2
Type of Random Effect:
                          additive animal
Pedigree File:
                          renadd02.ped
 trait effect (CO) VARIANCES
       2 0.3000
 1
REMARKS
  (1) Weight position 0 means no weights utilized
  (2) Effect positions of 0 for some effects and traits means that such
     effects are missing for specified traits
Data record length =
                              3
                    6101
# equations =
G
0.30000
read
           6100 records in 1.4997000E-02 s,
                                                                12201
 nonzeroes
 read
            6100 additive pedigrees
finished peds in 1.9996000E-02 s,
                                                    27178 nonzeroes
round = 1 convergence = 0.1730E-03
round =
        2 convergence = 0.7971E-03
round = 3 convergence = 0.5923E-04
round = 4 convergence = 0.6219E-04
round = 5 convergence = 0.2122E-04
        40 convergence = 0.1230E-13
round =
         41 convergence = 0.3164E-14
round =
round =
         42 convergence = 0.2804E-14
         43 convergence = 0.1081E-14
round =
round =
        44 convergence = 0.5761E-15
  44 iterations, convergence criterion= 0.5761E-15
solutions stored in file: "solutions"
```

#### Solutions for BLUPF90 without genomic information

solution	level	/effect	trait
1.02176505	1	1	1
-0.24665178	1	2	1

1

1	2	2	0.16420973
1	2	3	0.32371581
1	2	4	0.00318130
1	2	5	-0.13277100

#### The solution file (solutions) has 4 columns:

- 1) Trait [only 1 trait in this example]
- 2) Effect [we have 2 effects: overall mean (effect 1) and additive genetic direct (effect 2)]
- 3) Level [number of the level for each effect in the model]
- 4) Solution

# **EBV accuracy**

If accuracy of EBV is desired, it can be calculated based on standard errors (se) for EBV. **BLUPF90** has an option for calculating se:

# **OPTION sol se**

# Solutions for BLUPF90 with option to calculate se

trait,	/effect	level	solution	s.e.
1	1	1	1.02176504	0.02496866
1	2	1	-0.24665117	0.39158195
1	2	2	0.16421026	0.40488662
1	2	3	0.32371755	0.29405286
1	2	4	0.00318218	0.38229658
1	2	5	-0.13277154	0.46566701

The solution file now includes a 5<sup>th</sup> column with EBV standard errors

```
Parameter file for BLUPF90 with genomic information (ssGBLUP)
DATAFILE
renf90_5.dat
NUMBER_OF_TRAITS
     1
NUMBER_OF_EFFECTS
     2
OBSERVATION(S)
 1
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT[EFFECT NESTED]
 2
      1 cross
 3 6100 cross
RANDOM RESIDUAL VALUES
 0.70000
RANDOM_GROUP
  2
RANDOM_TYPE
add_animal
FILE
renadd02.ped
(CO)VARIANCES
 0.30000
OPTION SNP_file snp.txt
OPTION map_file map.txt
OPTION conv_crit 1e-15
```

```
Log file for BLUPF90 with genomic information (ssGBLUP)
name of parameter file?
renf90.par
* convergence criterion (default=1e-12): 1.000000E-15
Options read from parameter file:
* SNP file: snp.txt
 * SNP Xref file:snp.txt_XrefID
* Map file: map.txt
    BLUPF90 1.48
Parameter file:
                       renf90.par
Data file:
                        renf90_5.dat
Number of Traits
                          1
Number of Effects
Position of Observations 1
5 Weight (1) 0
Value of Missing Trait/Observation
                                      0
EFFECTS
# type
                                    levels [positions for nested]
                   position (2)
1 cross-classified
                     2
                                                                         1
2 cross-classified
                                                                      6100
                     3
Residual (co)variance Matrix
0.70000
Random Effect(s) 2
Type of Random Effect:
                       additive animal
Pedigree File:
                        renadd02.ped
trait effect (CO) VARIANCES
      2 0.3000
 1
REMARKS
  (1) Weight position 0 means no weights utilized
  (2) Effect positions of 0 for some effects and traits means that such
     effects are missing for specified traits
Data record length =
                            3
# equations = 6101
G
0.30000
read 6100 records in 0.1499770 s,
                                                           12201
 nonzeroes
 read
           6100 additive pedigrees
 *------
 *
                Genomic Library: Version 1.164
 *
 *
                 Optimized OpenMP Version
                                                        *
 * Modified relationship matrix (H) created for effect: 2 *
 *_____
```

Read 6100 animals from pedigree file: "renadd02.ped" Number of Genotyped Animals: 1294

Creating A22

Extracting subset of: 2312 pedigrees from: 6100 elapsed time: 0.0150 Calculating A22 Matrix by Colleau OpenMP...elapsed time: .0346 Numbers of threads=8 16 Reading SNP file Column position in file for the first marker: 8 Format to read SNP file: (7x,400000i1) Number of SNPs: 1000 Number of Genotyped animals: 1294 Reading SNP file elapsed time: .06 Statistics of alleles frequencies in the current population N: 1000 0.504 Mean: Min: 0.043 Max: 0.929 Var: 0.032 Reading MAP file: "map.txt" - 1000 SNPs out of 1000 Min and max # of chromosome: 1 5 Min and max # of SNP: 1 1000 Quality Control - SNPs with Call Rate < callrate ( 0.90) will removed: 0 Quality Control - SNPs with MAF < minfreq ( 0.05) will removed: 1 Quality Control - Monomorphic SNPs will be removed: 0 Quality Control - Removed Animals with Call rate < callrate ( 0.90): 0 Quality Control - Check Parent-Progeny Mendelian conflicts Total animals: 6100 - Genotyped animals: 1294 - Effective: 1294 Number of pairs Individual - Sire: 450 Number of pairs Individual - Dam: 440 Number of trios Individual - Sire - Dam: 206 No sex Chromosome information is available Parent-progeny conflicts or HWE could eliminate SNPs in sex Chr Provide map information and sex Chr to checks using autosomes Checking SNPs for Mendelian conflicts Total number of effective SNP: 999 Total number of parent-progeny evaluations: 890 Number of SNPs with Mendelian conflicts: 0 Checking Animals for Mendelian conflicts Total number of effective SNP for checks on Animals: 999 Number of Parent-Progeny Mendelian Conflicts: 0 Number of effective SNPs (after QC): 999 Number of effective Indiviuals (after QC): 1294 Statistics of alleles frequencies in the current population after

Quality Control (MAF, monomorphic, call rate, HWE, Mendelian conflicts)

999 N: Mean: 0.504 Min: 0.051 Max: 0.929 0.032 Var: Genotypes missings (%): 0.100 Genotypes missings after cleannig (%): 0.000 Calculating G Matrix Dgemm MKL #threads= 8 16 Elapsed omp\_get\_time: 1.0240 Scale by Sum(2pq). Average: 435.140185710293 Blend G as alpha\*G + beta\*A22: (alpha,beta) 0.950 0.050 Frequency - Diagonal of G N: 1294 Mean: 0.999 0.895 Min: 1.469 0.029 Max: Range: 0 20 Max: #Class Class Count 1 0.8951 27 2 0.9238 109 3 0.9524 304 4 0.9811 379 5 1.010 285 6 1.038 137 7 1.067 32 8 1.096 14 9 1.125 3 10 1.153 1 11 1.182 0 12 1.211 2 13 1.239 0 14 1.268 0 15 1.297 0 16 1.325 0 17 1.354 0 18 1.383 0 0 19 1.411 20 1.440 1 0 21 1.469

Check for diagonal of genomic relationship matrix

Check for diagonal of genomic relationship matrix, genotypes not removed: 0

----- Final Pedrigree-Based Matrix

-----

Statistic of Rel.	Matrix A22				
	N	Mean	Min	Max	Var
Diagonal	1294	1.001	1.000	1.250	0.000
Off-diagonal	1673142	0.005	0.000	0.750	0.001

-----Final Genomic Matrix \_\_\_\_\_ Statistic of Genomic Matrix Min Max N Mean Var 1294 1.001 0.898 1.470 0.002 Diagonal 1673142 0.005 -0.158 0.791 0.002 Off-diagonal Correlation of Genomic Inbreeding and Pedigree Inbreeding Correlation: 0.2180 All elements - Diagonal / Off-Diagonal Estimating Regression Coefficients G = b0 11' + b1 A + e Regression coefficients b0 b1 = 0.000 0.991 Correlation all elements G & A 0.717 Off-Diagonal Using 83426 elements from A22 >= .02000 Estimating Regression Coefficients G = b0 11' + b1 A + e Regression coefficients b0 b1 = -0.003 0.999 Correlation Off-Diagonal elements G & A 0.777 Creating A22-inverse Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp\_get\_time: 0.1059 ------Final A22 Inv Matrix ------Statistic of Inv. Rel. Matrix A22 N Mean Min Max Var 1294 1.851 1.067 5.812 Diagonal 0.431 Off-diagonal 1673142 -0.001 -1.200 0.600 0.001 Creating G-inverse Inverse LAPACK MKL dpotrf/i #threads= 8 16 Elapsed omp\_get\_time: 0.1093 -----Final Genomic Inv Matrix \_\_\_\_\_ Statistic of Inv. Genomic Matrix Mean Min 13.466 5.863 45.587 6.897 N Diagonal 1294 Var 13.466 28.023 Off-diagonal 1673142 -0.010 -13.521 6.897 0.227 Check for diagonal of Inverse Genomic - Inverse of pedigree relationship matrix \_\_\_\_\_ Final G Inv - A22 Inv Matrix -----

Statistic of Inv. Genomic- A22 Matrix

		N	Mean	Min	Max	Var	
Diagona	al	1294	11.615	4.782	40.309	21.740	
Off-dia	agonal	1673142	-0.009	-12.521	6.397	0.211	
*		*					
* Setup Con	mia Done	*					
*		<b>*</b>					
hash matrix	increased	from	131072	to	262144	<pre>% filled:</pre>	0.8000
hash matrix	increased	from	262144	to	524288	<pre>% filled:</pre>	0.8000
hash matrix	increased	from	524288	to	1048576	<pre>% filled:</pre>	0.8000
hash matrix	increased	from	1048576	to	2097152	<pre>% filled:</pre>	0.8000
finished pe	eds in	25.61810	s,		861721	nonzeroes	
round =	1 conver	gence =	0.6397E-03				
round =	2 conver	gence =	0.4280E-03				
round =	3 conver	gence =	0.3112E-03				
round =	4 conver	gence =	0.9994E-04				
round =	5 conver	gence =	0.8129E-04				
round = 9	90 conver	gence =	0.3590E-14				
round =	91 conver	gence =	0.2549E-14				
round =	92 conver	gence =	0.2022E-14				
round =	93 conver	gence =	0.1453E-14				
round =	94 conver	gence =	0.9599E-15				
94 iterat	tions, c	onvergen	ce criterion=	0.9599E-1	5		
		e:1	. 1				

solutions stored in file: "solutions"

#### Solutions for BLUPF90 with genomic information (ssGBLUP)

The solution file has the same format as in blupf90 without genomic information. The option for calculating se for EBV can also be used here.

#### Parameter file for PREDICTF90

Predictivity can be measured as correlation between adjusted phenotypes and (G)EBV. In this example we show how to use PREDICTF90 to adjust phenotypes for genotyped animals in the validation population.

#### 1) Adjusting phenotypes

As this program needs solution file, it can be run in the same folder as BLUP with complete data

Parameter file: DATAFILE pred.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 OBSERVATION(S) 1 WEIGHT(S)

pred.dat is the data file only for genotyped animals in the 5<sup>th</sup> generation (validation animals). Lines can be extracted from renf90.dat 2 1 cross 3 6100 cross RANDOM\_RESIDUAL VALUES 0.70000 RANDOM\_GROUP 2 RANDOM\_TYPE add\_animal FILE renadd02.ped (CO)VARIANCES 0.30000 OPTION include\_effects 2

# Log file for adjusting phenotypes for genotyped animals in 5<sup>th</sup> generation

```
name of parameter file?
pred.par
*** include effets to predict Yhat n, effects
                                                        1
                                                                    2
    PREDICTF90 1.3
Parameter file:
                            gen.par
Data file:
                           pred.dat
Number of Traits
                            1
Number of Effects
                             2
                           1
Position of Observations
Position of Weight (1)
                             0
Value of Missing Trait/Observation
                                            0
EFFECTS
# type
                       position (2)
                                          levels
                                                  [positions for nested]
1 cross-classified
                        2
                                                                                 1
2 cross-classified
                        3
                                                                              6100
Residual (co)variance Matrix
0.70000
Random Effect(s)
                    2
                            additive animal
Type of Random Effect:
Pedigree File:
                            renadd02.ped
 trait effect
                  (CO) VARIANCES
 1
         2 0.3000
REMARKS
  (1) Weight position 0 means no weights utilized
  (2) Effect positions of 0 for some effects and traits means that such
     effects are missing for specified traits
Data record length =
                                з
 # equations =
                      6101
*** effets to include in Yhat (T/F): F T
solutions read from file: soltutions
Animal Effect:
                        2
y(s), yhat(s), residual(s) in written in "yhat residual" file
        300 records read
Trait:
                1
                            300
                -5.204056186291079E-002 var Y
                                                        0.979795877964320
   mean Y
   mean Yhat -1.187536126623551E-002 var Yhat
                                                        7.349890384221654E-002
```

cov (Y,Yhat) 8.232182257800019E-002 corr (Y,Yhat) 0.306765659847626 wrote bvs for animals in data in file "bvs.dat"

# Output files from PREDICTF90 yhat\_residual

1 2 4644 0.415535

0.094263

1 2 2176

yhat_res	sidual has 4 colum	ıns: animal   y	yhat   residual	
4644 2176 <b>bvs.dat</b>	-0.266520 -0.418925	0.415535 0.094263	0.339710 0.508577	Because OPTION include_effects 2 was used: y is phenotype minus all effects other than animal yhat receives the second effect, which is the animal effect residual is phenotype minus animal effect
bvs.dat l	has 4 columns: tra	iit   effect   Anin	nal   solution (EB)	0

**Hint:** corr (Y,Yhat) from the output of PREDICTF90 (corr (Y,Yhat) 0.306765659847626) should not be used as a measure of predictivity because it uses adjusted phenotypes and EBVs from the same dataset. Usually, predictivity requires phenotypes adjusted for fixed effects in the complete data (benchmark) and (G)EBVs calculated from the reduced data (without records for validation animals). The regular predictivity measure is: corr[Y\_from\_PREDICTf90, (G)EBV\_reduced]

#### For this small example with 1 trait, a general Linux code to merge files is:

```
$awk '{print $1,$2}' ebv_complete/yhat_residual | sort +0 -1 > Y
$awk '{if ($2==2) print $3,$4}' ebv_reduced/solutions | sort +0 -1 > ebv.temp
$awk '{if ($2==2) print $3,$4}' gebv_reduced/solutions | sort +0 -1 > gebv.temp
$join -1 +1 -2 +1 Y ebv.temp > file1.temp
$join -1 +1 -2 +1 file1.temp gebv.temp > Y_ebv_gebv
```

#### An R code to calculate correlations is:

```
pred <- read.table("Y_ebv_gebv",header=F)
ebv_predictivity <- cor(pred[,2],pred[,3]); ebv_predictivity
gebv_predictivity <- cor(pred[,2],pred[,4]); gebv_predictivity</pre>
```

# Parameter files for GWAS using ssGBLUP (ssGWAS)

Run BLUPF90 with genomic information and salve G<sup>-1</sup> and A<sub>22</sub><sup>-1</sup> DATAFILE renf90.dat NUMBER\_OF\_TRAITS

```
1
NUMBER_OF_EFFECTS
     2
OBSERVATION(S)
 1
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT[EFFECT NESTED]
 2
      1 cross
 3
    6100 cross
RANDOM_RESIDUAL VALUES
 0.70000
RANDOM_GROUP
  2
RANDOM_TYPE
add_animal
FILE
renadd02.ped
(CO)VARIANCES
 0.30000
OPTION SNP_file snp.txt
OPTION map_file map.txt
OPTION no_quality_control
OPTION saveGinverse
OPTION saveA22Inverse
OPTION weightedG wei
```

Weights for SNP can be updated by an iterative process, where the initial weights are all equal to 1.

Linux code to get initial weights for 1000 SNP: \$awk 'BEGIN { for (i==1;i<1000;i++) print 1}' > wei

# Run POSTGSF90 and read G<sup>-1</sup> and A<sub>22</sub><sup>-1</sup>

```
DATAFILE
renf90.dat
NUMBER_OF_TRAITS
     1
NUMBER_OF_EFFECTS
    2
OBSERVATION(S)
 1
WEIGHT(S)
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT[EFFECT NESTED]
2
     1 cross
3 6100 cross
RANDOM_RESIDUAL VALUES
0.70000
RANDOM_GROUP
  2
RANDOM_TYPE
add_animal
FILE
renadd02.ped
(CO)VARIANCES
0.30000
```

OPTION SNP\_file snp.txt OPTION map\_file map.txt OPTION no\_quality\_control OPTION Manhattan\_plot OPTION readGInverse OPTION readA22Inverse OPTION weightedG wei OPTION windows\_variance 5

Moving average of SNP effects can be obtained by using the following option: OPTION SNP\_moving\_average n where n is the number of SNP

# Manhattan plots for SNP windows variance



# Manhattan plots for SNP effect using moving average of 2 SNP



# **Output files for ssGWAS**

# snp\_sol

1	2	1	1	0	0.7001368E-02	0.2209213	0.1119293	0.1126648E-03
1	2	2	1	0	-0.1359349E-01	0.5065436	0.2104747	0.2118577E-03
1	2	3	1	0	0.8714214E-02	0.3917027	0.7757968	0.7808942E-03
1	2	4	1	0	-0.4223401E-02	0.6873333E-	01 1.271113	0.1279465E-02
1	2	5	1	0	0.5471629E-03	0.1539137E-	02 1.261010	0.1269296E-02

snp\_sol has 9 columns because "OPTION windows\_variance" was used: trait | effect | SNP | chromosome | position | SNP\_solution | weight | % of variance explained by n adjacent SNP | variance explained by n adjacent SNP

# chrsnpvar

1	2	0.1119293459	1	1	0
1	2	0.2104747339	2	1	0
1	2	0.7757968029	3	1	0
1	2	1.2711127978	4	1	0
1	2	1.2610103595	5	1	0

chrsnpvar has 6 columns: trait | effect | % of variance explained by n adjacent SNP | SNP | chromosome | position

This file is used by POSTGSF90 for Manhattan plots

# Appendix J (custom relationship matrices)

When a relationship (or dispersion) matrix cannot be created within the application programs, it can be prepared separately and then included as a custom relationship matrix. Two options exist for inclusion of such a matrix. Option user\_file incorporates this matrix directly. Option user\_file\_inv incorporates the inverse of this matrix.

The example below presents a model from the previous Appendix with matrix **H**<sup>-1</sup> created externally and then read as a custom matrix. The custom matrix (Hinverse.txt) is stored as below, with each line containing: row, column and value.

1 3.0000 1 1 422 -1.0000 1 870 0.5000 1 4326 -1.0000 1 4612 -1.0000 . . • . . 6096 6100 -0.0527 6097 6097 2.5000 6098 6098 11.0000 6099 6099 2.0000 6100 6100 12.0236

Parameter file for BLUPF90 with a custom relationship matrix

DATAFILE renf90\_5.dat NUMBER\_OF\_TRAITS 1 NUMBER\_OF\_EFFECTS 2 **OBSERVATION(S)** 1 WEIGHT(S) EFFECTS: POSITIONS\_IN\_DATAFILE NUMBER\_OF\_LEVELS TYPE\_OF\_EFFECT[EFFECT NESTED] 2 1 cross 3 6100 cross RANDOM\_RESIDUAL VALUES 0.70000 RANDOM GROUP 2 RANDOM\_TYPE user\_file FILE Hinverse.txt (CO)VARIANCES 0.30000 OPTION conv\_crit 1e-15

# Log file for BLUPF90 with a custom relationship matrix

name of parameter file? user.par \* convergence criterion (default=1e-12): 1.000000E-15 BLUPF90 1.48 Parameter file: user.par Data file: renf90\_5.dat Number of Traits 1 Number of Effects 2 Position of Observations 1 Position of Weight (1) 0 Value of Missing Trait/Observation 0 EFFECTS # type position (2) levels [positions for nested] 1 cross-classified 2 1 2 cross-classified 3 6100 **Residual (co)variance Matrix** 0.70000 Random Effect(s) 2 Type of Random Effect: user defined from file User File: Hinverse.txt The name of custom matrix used is shown here trait effect (CO)VARIANCES 2 0.3000 1 REMARKS (1) Weight position 0 means no weights utilized (2) Effect positions of 0 for some effects and traits means that such effects are missing for specified traits Data record length = 3 # equations = 6101 G 0.30000 read 6100 records in 4.7991998E-02 s, 12201 nonzeroes ••• g\_usr\_inv: read 855620 elements largest row, column, diagonal: 6100 6100 6100 ••• finished peds in 1.776729 s, 861721 nonzeroes round = 1 convergence = 0.5737E-03 ... round = 80 convergence = 0.9128E-15 80 iterations, convergence criterion= 0.9128E-15 solutions stored in file: "solutions"

# **Appendix K (selected programming details)**

This section provides some programming insights into an early version of the blupf90 program. The model is completely described in the module MODEL.

```
module model
implicit none
        Types of effects
integer, parameter::effcross=0, & !effects can be cross-classified
                 effcov=1 !or covariables
        Types of random effects
integer, parameter :: g_fixed=1,&
                                     ! fixed effect
                      g A UPG=4, & ! additive animal with unknown
                                       !
                                              parent groups
                    & g_A_UPG_INB=5, & ! additive animal with unknown
                                             parent groups and inbreeding
                                       !
                    & g As=6,&
                                       ! additive sire
                      g PD =7, &
                                       ! parental dominance
                                     ! last type
                      g_last=8
character (40)
                :: parfile, &
                                   !name of parameter file
                      datafile
                                   !name of data set
integer :: ntrait,&
                                  !number of traits
          neff,&
                                  Inumber of effects
          miss=0
                                    !value of missing trait/effect
integer,allocatable :: pos y(:)
                                  !positions of observations
integer ::
                    pos_weight
                                    ! position of weight of records; zero if none
integer, allocatable :: pos_eff(:,:),& !positions of effects for each trait
                                    !number of levels
                     nlev(:),&
                     effecttype(:),& !type of effects
                     nestedcov(:,:),&!position of nesting effect for each trait
                                    ! if the effect is nested covariable
                   & randomtype(:),& ! status of each effect, as above
                     randomnumb(:) ! number of consecutive correlated effects
character (40),allocatable:: randomfile(:)
                                           ! name of file associated with given
                                                ! effect
                                   !residual (co)variance matrix
real, allocatable :: r(:,:),&
                     rinv(:,:),&
                                    ! and its inverse
                     g(:,:,:) ! The random (co)variance matrix for each trait
end module model
```

The core of the program is presented below.

```
type (sparse ija):: xx ija
                                     ! X'X in IJA form, for use with FSPAK only
real, allocatable:: xy(:),sol(:)
                                        !X'Y and solutions
real,allocatable :: weight cov(:,:)
integer,allocatable:: address(:,:)
                                        ! start and address of each effect
                                         ! number of equations and io-status
integer :: neq,io,&
                                         ! length of data record to read
           data_len,&
           i,j,k,l
                                         ! extra variables
real:: val, dat_eff
call read_parameters
call print_parameters
neq=ntrait*sum(nlev)
data_len=max(pos_weight,maxval(pos_y),maxval(pos_eff))
print*, 'Data record length = ', data len
allocate (xy(neq), sol(neq), address(neff, ntrait), &
          weight_cov(neff,ntrait),y(ntrait),indata(data_len))
call zerom(xx,neq); xy=0
1
call setup_g
                                ! invert R matrices
open(50,file=datafile)
                               !data file
! Contributions from records
do
  read(50,*,iostat=io)indata
  if (io.ne.0) exit
  call decode record
  call find_addresses
   call find rinv
  do i=1,neff
       do j=1,neff
          do k=1,ntrait
             do l=1,ntrait
                 val=weight cov(i,k)*weight cov(j,l)*weight y*rinv(k,l)
                 call addm(val,address(i,k),address(j,l),xx)
             enddo
          enddo
       enddo
       do k=1,ntrait
          do l=1,ntrait
              xy(address(i,k)) = xy(address(i,k)) + rinv(k, 1) * y(1) * weight_cov(i,k) &
                                                               *weight_y
          enddo
       enddo
   enddo
enddo
.
     Random effects' contributions
do i=1,neff
   select case (randomtype(i))
    case (g_fixed)
       continue
                                 ! fixed effect, do nothing
     case (g_diag)
        call add_g_diag(i)
     case (g_A, g_As, g_A_UPG,g_A_UPG_INB)
        call add g_add (randomtype(i), i)
     case (g PD)
       call add_g_domin(i)
     case default
      print*, 'unimplemented random type', randomtype(i)
   endselect
enddo
if (neq < 15) then
  print*,'left hand side'
  call printm(xx)
  print '( '' right hand side:'' ,100f8.1)',xy
endif
```

call solve\_iterm(xx,xy,sol)

! Comment the line above and uncomments the lines below only if ! solutions by FSPAK are desired !xx\_ija=xx; !call fspak90('solve',xx\_ija,xy,sol)

if (neq <15) print '( '' solution:'' ,100f7.3)',sol

call store\_solutions
# **Modules and Libraries**

## **Module DENSEOP**

Subroutines and functions for dense matrix manipulation in Fortran 90. Uses F90 LAPACK implementation by Alan Miller for some low level routines.

Written by:Tomasz Strabel & Ignacy Misztal, University of Georgia e-mail:<br/>strabel@au.poznan.pl, ignacy@uga.edu, Oct/5/98-June 8, 2006

The module implements matrix operations on dense general and symmetric matrices. Each subroutine/function is overloaded to work with several types of arguments. The module is primarily designed for matrix operations where timing and memory requirements are not critical.

#### Symmetric matrices

Each of the functions/subroutines works with full-stored and packed (half-stored) matrices. Each matrix or vector can be single or double precision. However, in one function/subroutine, all arguments should be of the same precision, and all matrices should be stored the same way.

#### **Subroutines**

```
call chol(a,rank) - Cholesky decomposition
call inverse_s(A,rank) - Generalized inverse: AI = A-
call eigen(A,d,V) - Eigenvalues and eigenvectors: A =V diag(d)*V'
call solve_s(A,b,x) - Generalized solutions: x: Ax=b
The optional variable rank returns the rank of the matrix.
```

#### **Functions**

fchol(A)	- Cholesky decomposition
finverse_s(A)	- Generalized inverse
fsolve_s(A,b)	- Generalized solve
fdet_s(A)	- Determinant of A

Procedures for symmetric matrices work with generalized matrices. Redundant rows/columns equations are determined by operational zero, which is kept in global variable denseop\_tol with default value is 10-

10. To change the limit, change the value of the variable in the application program, e.g., denseop\_tol=1d-12

Conversions

Let A be a square matrix and AP be a packed matrix

```
call packit(A,AP) - Conversion from square to packed form; only lower-diagonal elements
are used.
call unpackit(AP,A) - Conversion from packed to square form; the matrix is assumed
symmetric.
```

## **General matrices**

Each matrix or vector can be single or double precision. However, in one function/subroutine, all arguments should be of the same precision. All matrices are assumed full-rank.

Subroutines		
call inverse(A	) - Inverse: AI = A-1 call solve(A,b,x)	- Solutions: x: Ax=b
Functions		
AI=finverse(A)	<ul> <li>Returns inverse: AI = Ax=fsolve(A,b)</li> </ul>	- Computes solutions: x: Ax=b

## Printing

call printmat (matrix, text, fmt, un) print any type of matrix using the specified format fmt and preceded by text. Both text and fmt are optional. If optional un is present, the output is send to file with unit un.

Warning: The printmat function prints the symmetric packed matrices in full. If a half-stored matrix is in packed form, it will be printed as full-stored matrix.

## Additional subroutines and functions

The subroutine(s) and functions below work only with double precision arguments (r8) and fullstored matrices.

call pos\_def(x,text,min\_eig,stat) Cor

Corrects X if it is not "sufficiently" positive-

definite; ignores rows/columns with 0 elements only.

X - real (r8) symmetric square matrix

text - optional character variable that is printed if X is corrected

- min\_eig optional real (r8) variable that sets the minimum relative eigenvalue in X; if min\_eig is missing, 1e-5 is used.
- stat optional logical variable that is set to .true. if X was corrected and .false. if not.
- A = diag(b) creates square diagonal real (r8) matrix with values of real (r8) vector b on diagonal
- b = diag(A) creates real (r8) vector b containing diagonals of real (r8) matrix A
- A=kron(B,C) A = B "Kronecker product" C; works with real(r4) and real (r8) matrices

### **Technical details**

The basic operations are done in full storage and double precision. Operations with other formats and precision are obtained by conversions. Computing of eigenvalues/eignevectors and general matrix operations use parts of LAPACK subroutines as converted by Alan Miller. These subroutines may contain many more functionality than necessary and may be trimmed to reduce size of the object code.

#### The modules consist of two files:

lapack90r.f90 - Part of LAPACK denseop.f90 - Interfaces, subroutines, functions and conversion codes. For compilation, module kind in file kind.f90 that contains definitions of single and double precision is also needed.

In the BLUPF90 distribution, these files are included in directory libs and are compiled as denseop.a. One way to use the denseop module is via a Makefile from an application program in the blupf90 package.

## Example (exdense.f90)

#### Program Example:

```
use kinds; use denseop
real (r4):: xpacked4(3)=(/1,3,10/)  ! Symmetric packed single
precision
real (r4)::x4(2,2)  ! Full single precision
real (r8)::x8(2,2)  ! Full double precision
call printmat(xpacked4,' X ')
call printmat(fchol(xpacked4),' Cholesky(X) ','(10(f10.2))')
x4=xpacked4
x8=x4
print*,' Determinant(xpacked4)=',fdet_s(xpacked4)
print*,' Determinant(x8)=',fdet_s(x8)
print*,' Determinant(x4)=',fdet_s(x4)
end
```

## Compilation

To compile standalone:

f90 kind.f90 lapack90r.f90 denseop.f90 exdense.f90 This assumes that all files are in the same directory.

To compile in subdirectory of the blupf90 distribution under Linux/Absoft,

f90 -p ../libs exdense.f90 ../libs/denseop.a

where option -p specifies library directory. This option (-p) is different under different platforms. See documentation on blupf90 distribution for details.

## **Module SPARSEM**

Collection of sparse matrix modules for Fortran 90 useful in animal breeding problems

Written by: Ignacy Misztal, University of Georgia e-mail: ignacy@uga.edu, 9/4/1997 - 5/25/2007

### Introduction

Traditionally, programming in animal breeding is done in 2 stages: in a matrix language and in a regular programming language. Programs in a matrix language such as IML SAS, Matlab, Mathematica or APL are reasonably simple and useful for creating examples but inefficient for large problems. Programs in a regular programming language such as Fortran or C/C++ are much more efficient but could take much longer to write and require substantial training.

Matrix languages are easy to deal with matrices partly because usually only one format is usually supported: dense rectangular. Operations on such matrices are easy to specify and program, but large matrices require large memory and long running time. Also, memory and computations are equal whether matrices are sparse (contain very few nonzero elements) or not. In animal breeding, many matrices are sparse. If that sparsity is taken into account, the memory requirements and computations can decrease dramatically. Unfortunately, there is more than one format for storing sparse matrices, and some computations are fast with one format and but not with another one. Also, the storage formats and operations are considerably more complicated than dense rectangular matrices. A library to handle multiple matrix formats and multiple operations would contain many subroutines, each with a long list of arguments. Such a library would involve considerable learning, and many details associated with the library would create many opportunities for making a mistake.

One matrix package, Matlab, has some forms of sparse-matrix storage and operations included.

Modern programming languages with "object-oriented" features, such as C++ or Fortran 90, have abilities to create classes/modules, where many implementation details on specific data structures can be hidden. A technique called overloading allows single function/subroutine to work with different formats of its arguments. Therefore, the number of details to remember can be drastically reduced. Subsequently, programming can be done much easier and quicker.

SPARSEM is a module for Fortran 90 that enables programming common sparse matrix operations almost as easily as with dense matrices. It supports two dense matrix formats, useful for testing, and two sparse matrix formats. Changing a program from dense to sparse-matrix format using DENSEM can be as simple as changing one declaration line. SPARSEM incorporates an interface to FSPAK, which enables efficient sparse matrix factorization, solving, sparse inversion and calculation of determinant on matrices much larger than possible with dense matrix structures.

### **Matrix formats**

Four matrix formats are available.

DENSEM - dense square matrix.

DENSE\_SYMM -dense symmetric upper-stored.

It has approximately only half memory requirements of the dense square matrix.

SPARSE\_HASHM - sparse triple accessed by hash algorithm.

This is a very efficient format for set-up and for iterative-solving of sparse matrices. SPARSE\_IJA - Sparse IJA.

This is a memory-efficient format for sparse matrices used by sparse matrix packages. Format IJA cannot easily be set up directly but can be derived by conversion from the hash format.

For more information on all these formats see Duff et al, George and Liu, or my class notes.

A popular format that is not included here is linked list. That format is reasonably efficient for creating and computing with sparse matrices if the number of nonzero elements per row is not too high and the matrix is not too large. However, the combination of hash plus ija is generally more efficient.

## **Matrix operations**

The following subroutines/functions are supported. All real scalars and vectors are single precision unless indicated otherwise.

Operation	Description	Comments
call init(x)	Initialize x	Required by standard but usually not necessary because on most systems pointers are initialized automatically
call zerom(x,n)	Allocate storage for x as an n*n matrix and zero it	If x was set before, it is reallocated <sup>1</sup>

call reset(x)	Deallocates storage	
call addm(a,i,j,x)	Add to matrix: x(i,j)=x(i,j)+a	Does not work on SPARSE_IJA
call setm(a,i,j,x)	sets element of matrix: x(i,j)=a	Does not work on SPARSE_IJA
y=getm(i,j,x)	find element of matrix: y=x(l,j)	real(4) function; returns lower- diagonal elements of upper- stored matrix
x=y	Conversion between formats	Conversion from sparse to dense formats may require too much storage
call printm(x)	Prints x as square matrix	print(x,'internal') prints sparse matrices in internal format
call solve_iterm(x,rs,sol)	Solves: x sol=rs iteratively by SOR	
call default_iter (conv,maxround,relax, zerosol)	Changes default iteration parameters	All parameters are optional; default values are: conv(ergence criterion)=1e-10, max round(s)=1000, relax(ation factor)=1.0, zerosol(utions ar beginning of iteration) = .true.
x=block(y,i1,i2,j1,j2)	Selects block from y: x=y(i1:i1,j1:j2)	does not work on dense_symm format; may not work with unsymmetric blocks from symmetric matrices
q=quadrf(u,x,v)	q=u'Xv	real(8) function; does not work on dense_symm format
tr=trace(x,γ)	Self explanatory	real(8) function; x and y must be in same formats; works on densem and sparse_ija formats only
tr=traceblock(x,y,i1,i2,j1, j2)	tr=trace(xy(i1:i2,j1:j 2))	Works as a block-trace combination; produces correct results when blocks of y are nonsymmetric

<sup>1</sup>The hash matrix is allocated for a default number of elements. If the default is too small, the hash matrix is enlarged automatically. To change the default p elements, use call zerom(x,n,p). One matrix element in hash format takes 12 bytes, and for efficient operation there should be at least 10% more nonzero elements available than used.

All operations assume that the densem type is general while all the other types are upperstored.

Operations tr, quadf work with both upper- and full-stored matrices but the block operation works literally, i.e., selecting a lower block would return an empty matrix and selecting an upper block would return only an upper-stored matrix. This could be a source of incompatibility between densem and other formats that use the block operation without taking its limitations into consideration. Potential problems can be noticed in examples by printing matrices of interest.

#### **Storage type**

Matrices in the hash or ija format are half-stored by default. To change the storage type to full, add the option 'f' to the addm subroutine: call addm (a, i, j, x, 'f')

The subsequent conversion to the ija format will also be full-stored. For conversion from half-stored hash matrix to full-stored ija, please see a documentation for the GIBBS module.

The printing and other functions/subroutines have been designed for half-stored hash and ija matrices. Results may not be correct with full-stored matrices.

#### **Numerical accuracy**

Module KINDS defines precision r4 to be equivalent to real\*4, and r8 to be equivalent to r8. Precision rh can be set up to r4 or r8 dependent on whether memory or precision is more important.

Formats DENSEM, DENSE\_SYMM, and SPARSE\_IJA use precision r8. Format

SPARSE\_HASHM uses precision rh. Whenever the precision of numbers in SPARSEM functions/subroutines is not specified, it is of type rh. Setting rh to r4 is useful when memory usage needs to be reduced, e.g., for large BLUP programs. Setting rh to r8 is necessary when numerical accuracy is important, e.g., in variance component programs, and is usually a safer choice.

#### **Diagnostics**

Printing of some diagnostic messages depends on the value of an integer variable sparsem\_msg. The value of 3 means maximum diagnostic messages while the value of 0 means no diagnostic messages. The default is 2. This variable can be set in any part of the application program using the module SPARSEM.

#### FSPAK90

FSPAK is a sparse matrix package written in F77 that performs operations on sparse matrices in format SPARSE\_IJA. Operations include solving a system of linear equations by factorization, calculating a (log)determinant or finding a sparse inverse of a matrix. A sparse inverse is such a matrix that contains inverse values only for those elements that were nonzero in the original matrix. For sparse matrices, FSPAK is very efficient computationally.

FSPAK90 is a F90 interface written to simplify the use of FSPAK.

#### A complete call to FSPAK90 is:

```
call fspak90(operation,ija,rs,sol,det,msglev,maxmem,rank)
```

#### where

operation=	"factorize"	- calculate sparse factorization
	"invert"	- calculate sparse inverse
	"solve"	- solve a system of equation
	"reset"	- reset the storage
	"det"	- calculate determinant
	"stat"	- print statistics
	"fact_mult"	- multiplication by Cholesky factor of the reordered
		matrix (if LL=IJA; sol=L*rs)
	"inv_fact_mult	" - solve the system formed by the Cholesky factor of the
		reordered matrix (sol: L*sol=rs)

ija = matrix in SPARSE\_IJA form
rs = real (r4) or (r8) vector of right hand side,
sol = real (r4) or (r8), identical to precision of rs, vector of solutions
det = real (r8) determinant or log-determinant
msglev= message level from 0 (minimum) to 3 (maximum); default=0
memory available in the system; default=infinite
rank=rank of matrix

All the arguments of fspak90 except "operation" and "ija" are optional except when they are needed in a specific "operation". Thus, rs and sol are needed for solving and det for "det" or "ldet".

Examples:

To solve:

call fspak90('solve',ija,rs,sol)
for both rs and sol either in single or double precision; all. Preceding steps are done automatically.

```
To solve using double precision right hand side and solutions:
      call fspak90('solve',ija,rs8=rs,sol8=sol)
To sparse invert:
      call fspak90('invert',ija)
To obtain the determinant d:
      call fspak90('det',ija,det=d)
To obtain the log determinant ld:
      call fspak90('ldet',ija,det=ld)
To obtain rank r with any operation:
      call fspak90(....,rank=r)
To force new factorization, when the input matrix has changed: call
      fspak90('factor',ija)
To deallocate the internal memory:
      call fspak90('reset')
To limit memory to a maximum od maxmem, e.g., 20,000k, with any operation call
      fspak90(....,maxmem=20000)
```

Note that only relevant arguments for each step need to be included in calling FSPAK90. Reordering is performed the first time when FSPAK90 is called. Subsequent factorization except after the option "reset" will reuse the ordering. Subsequent solves will reuse the factorization. Additionally:

```
To sample y from N(0,A) where x~N(0,1)
            call fspak90 ('fact_mult',A,rs8=x,sol8=y)
To sample y from N(0,A<sup>-1</sup>) where x~N(0,1)
            call fspak90 ('inv_fact_mult',A,rs8=x,sol8=y)
For details of the last operations, see Appendix S2
```

Additional subroutines and functions:

Function

```
y=mult(A,x)
```

y=mult(x,A)

Implements the matrix by vector multiplication for all matrix formats except dense\_symm, and for double precision x and y.

Subroutine

call multmatscal(A,x)

Implements A=A\*x for all matrix formats except dense\_symm, and for double precision x.

Hints on using SPARSEM

Initially all the matrices can be implemented in DENSEM format. After the program works well with an example, convert all data structures for potentially large matrices to sparse formats and verify that same results are obtained.

### Compiling

Matrix types and functions subroutine are defined in module sparsem. Subroutine fspak90 is in module sparseop. Program xx.f90 can be compiled as

f90 -Maa xx.f90 aa/sparsem.a

where aa is the directory containing the modules and the library, and M is the option to include module directory.

Beginning in May, 1999, SPARSEM is part of a programming package that includes BLUPF90, REMLF90, GIBSF90 etc. Compilation for several Unix environments is automated by makefiles. To find details, read Readme and Installation files in the package distributions. To create application with SPARSEM and possibly other modules, create a subdirectory in the main directory of the package, and adapt a makefile from the existing directory, e.g., blup.

#### Sample Programs

#### Dense matrix solution program

```
program test sparse structures use
sparsem; use kinds type (densem)::x
integer,parameter ::n=5
integer :: i,j
real (rh):: rs(n), sol(n), val
call init(x)
call zerom(x,n)
! set up a sample matrix do
i=1,n
 rs(i)=n+1-i
 val=10.0*i/i
 call addm(val,i,i,x)
 do j=i+1, n
   val=10.0*i/j
    call addm(val,i,j,x); call addm(val,j,i,x)
  enddo
enddo
```

```
print*,'rs: ',rs print*,'matrix' ; call printm(y) call
solve_iterm(y,rs,sol) !solve iteratively
print*,'sol: ',sol
end
```

Triangular dense matrix iterative-solution program

```
.....
type (dense_symm)::x
.....
(The rest of the program remains identical)
```

Sparse hash matrix iterative-solution program

```
type (sparse_hashm)::x
.....
```

Sparse IJA matrix iterative-solution program

Matrix in ija form cannot be set up directly but can be converted from hash form.

```
type (sparse_hashm)::x type
(sparse_ija)::y
...
y=x !conversion
call reset(x) ! Optional statement to release storage
print*,'rs: ',rs print*,'matrix' ; call printm(y) call
solve_iterm(y,rs,sol)
```

end

Sparse IJA matrix finite-solution and inversion program with FSPACK90

```
...
use sparsem use sparseop !fspak90 is in module sparseop .....
call fspak90('solve',y,rs,sol) ....
!now invert call
fspak90('invert',y)
call printm(y)
end
```

#### References

George, A. and Liu, J.W.H. (1981) Computer solution of large sparse positive definite systems. Prentice-Hall, Englewood Cliffs, N.J.

#### **Appendix S1**

```
Definitions of structure (type)
```

```
type densem
               !traditional dense square matrix
     integer :: n
     real(8) ,pointer::x(:,:)
end type densem
type dense symm
                     !upper stored symmetric dense matrix
     integer ::n
     real(8) ,pointer::x(:)
end type dense symm
type sparse hashm
   integer:: n,&
                        ! for compatibility mainly
             nel,& ! number of elements
                                                        filled,&
             ! number of filled elements
                                                    status !
             1 if ready to hash, 2 if in sorted
                         ! order
real (rh) , pointer :: x(:,:)
end type sparse hashm
type sparse_ija
                        ! number of equations
    integer :: n,&
                        ! number of nonzeroes
                nel
     integer, pointer::ia(:),ja(:) !will be ia(n+1), ja(m)
     real (8), pointer::a(:)
                                     !will be a(m)
end type
```

#### Accessing structures

Structures can be accessed within the application program using the "%" symbol. This is useful, e.g., when using Fortran 77 programs. The example below shows how to use a determinant program written in F77.

```
type (densem):: z
integer::i,j
real (rh)::value
call init(z)
call zerom(x,2)
```

```
! initialize z
do i=1,2
    do j=1,2
    value=i**j/10.
    call addm(value, i,j,z)
    enddo
enddo
print*, det(z%n,z%x)
end
function det(n,x)
!calculate determinant for a 2x2 matrix
integer n
real (r8):: x(n,n),det !
det= x(1,1)*x(2,2)/x(1,2)/x(2,1)
end
```

## Library

The following files are compiled into the library:

kind.f90	- definitions of precisions
sparse.f90	<ul> <li>type definitions + main subroutines,</li> </ul>
sparse2.f	- supporting subroutines (in f77),
fspak.f90	- f90 interface to fspak
fspak.f	- main fspak subroutine (in f77),
fspaksub.f	- supporting fspak subroutines (in f77),
sparssub.f	- low-level subroutines from the book of George and Liu (in f77),
second.f	<ul> <li>timing subroutine specific to each computer (in f77).</li> </ul>

Subroutines second() specific to other computers can be found in the FSPAK manual.

## Appendix S2

```
Multiplication and solving using factors

Let A be a matrix. Factorization produced by FSPAK is L:

A=P'LL'P

where P is a reordering matrix chosen to minimize the size of L:

PP'=P'P=I

Operation "fact_mult" multiplies the factor by a vector:

y=P' L P x

Operation " inv_fact_mult" solves the system of equation:

P'L' Py=x

This is equivalent to:

y=P' (L'^{-1}) Px
```

Both operations were programmed by Juan Pablo Sanchez. The operations are useful for generation of large random samples from a multivariate normal distribution. They may be useful in Gibbs sampler algorithms when setting up and factorization of the system of equations in each round are feasible.

## **Module Prob**

Probability routines for use in threshold models and Gibbs sampling

Written by: Ignacy Misztal and Deukhwan Lee, University of Georgia e-mail: ignacy@uga.edu, 04/29/99-04/19/2001

Module Prob is a collection of random number generators / probabilities / truncated distributions useful for Gibbs sampling and for threshold models. The module uses features of Fortran 90 to simplify programming and high-level optimization to reduce running time, with simplicity being as important as efficiency. To understand the module fully, please read the documentation on SPARSEM and on BLUPF90.

Module prob uses high-quality generators from public domain package RANLIB for random number generators. Some low level code is from Luis Varona.

## Subroutines/functions

call set\_seed(n)

Sets seed for random number generator to integer n. If this subroutine is not called, the seed will be selected by the system.

#### x=gen\_uniform(a,b)

a,b - both real (r\*) or both integers or both missing. If a,b are missing, generates samples from uniform(0,1) distribution If a,b are real (r8), generates samples from uniform(a,b) distribution If a,b are integers, generates random integer between a and b

x=gen\_normal (mean, var)
mean - (r8) scalar or vector
var - (r8) scalar or square matrix
x - (r8) scalar or square matrix
Generates x=N(mean,Var) when mean and var are scalars, or x=MVN(mean,Var) when mean is a vector
and Var is a matrix. Arguments mean and var are optional. If they are missing, sampling is from N(0,1)

#### x=gen\_invwishart(inv\_q\_form,df)

inv\_q\_form - (r8) scalar or square matrix containing inverse of quadratic formdf - an integer containing degrees of freedomGenerates samples from inverted chi square or inverted Wishart distributions.

y=normal(x)
x - real(r8) scalar
y - real (r8) contains density(X) for N(0,1)

y=normal\_cdf(x)
x - real (r8) scalar
y - real (r8) cumulative distribution function for N(0,1)

y=normal\_invcdf(x)
x - real (r8) scalar in the range of <0,1>
y - real (r8) as in: x=normal\_cdf(y)

y=generate\_trunc\_normal(a,b,mean,var)
y - real (r8) scalar or vector
a,b - real (r8) lower and upper bound of random samples
mean - real(r8) scalar or vectors of mean, optional if scalar
var - real(r8) variance or covariance matrix, optional if scalar

If mean and var are missing, generates random samples from N(0,1) distribution truncated to interval <a,b>.

If mean and var are scalars, generates random samples from N(mean,var) distribution truncated to interval <a,b>.

If mean is a vector and var is a matrix, generates random samples from MVN(mean,var) distribution with first dimension truncated to interval <a,b>.

#### **Other functions/subroutines**

New functions/subroutines are added to Module prob periodically. Please see program prob.f90 for details.

#### Acknowledgments

We acknowledge Fernando Bussiman for reviewing the 2024 version of this manual and the many users who have reported "bugs" in the manual and programs.