

# SNP effects from ssGBLUP using BLUPF90 (postGSf90)

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BLUPF90 TEAM – 02/2023



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# Equivalence between GBLUP and SNP-BLUP

GBLUP

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{G}^{-1}\lambda_1 \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{W}'\mathbf{y} \end{bmatrix}$$

↓  
GEBV

$$\text{Var}(\mathbf{u}) = ?$$

$$\text{Var}(\mathbf{u}) = \mathbf{G}\sigma_u^2$$

SNP-BLUP (Ridge Regression)

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{Z} \\ \mathbf{Z}'\mathbf{X} & \mathbf{Z}'\mathbf{Z} + \mathbf{I}\lambda_2 \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{a}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{Z}'\mathbf{y} \end{bmatrix}$$

↓  
SNP effects

$$\mathbf{u} = \mathbf{Z}\mathbf{a}$$

$$\text{Var}(\mathbf{u}) = \mathbf{G}\sigma_u^2$$

# Are GBLUP and SNP-BLUP equivalent?

- Assumption of GBLUP:  $\text{Var}(\mathbf{u}) = \mathbf{G}\sigma_u^2$
- In SNP-BLUP:  $\mathbf{u} = \mathbf{Z}\mathbf{a}$

$$\mathbf{u} = \mathbf{Z}\mathbf{a}$$

$$\text{Var}(\mathbf{u}) = \text{Var}(\mathbf{Z}\mathbf{a})$$

$$\text{Var}(\mathbf{u}) = \mathbf{Z} \text{Var}(\mathbf{a}) \mathbf{Z}'$$

$$\text{Var}(\mathbf{u}) = \mathbf{Z}\mathbf{Z}'\sigma_a^2$$

$$\sigma_a^2 = \frac{\sigma_u^2}{2 \sum_{i=1}^{SNP} p_i(1 - p_i)}$$

$$\text{Var}(\mathbf{u}) = \mathbf{Z}\mathbf{Z}' \frac{\sigma_u^2}{2 \sum_{i=1}^{SNP} p_i(1 - p_i)}$$

$$\text{Var}(\mathbf{u}) = \boxed{\frac{\mathbf{Z}\mathbf{Z}'}{2 \sum_{i=1}^{SNP} p_i(1 - p_i)}} \sigma_u^2$$

Genomic  
relationship matrix  
VanRaden (2008)

$$\mathbf{G} = \frac{\mathbf{Z}\mathbf{Z}'}{2 \sum_{i=1}^{SNP} p_i(1 - p_i)}$$

$$\text{Var}(\mathbf{u}) = \mathbf{G}\sigma_u^2$$



GBLUP assumption!!!



# GBLUP and SNP-BLUP are equivalent!

If we can get  $\mathbf{u}$  ( $\mathbf{u} = \mathbf{Za}$ ) from SNP-BLUP, we can get  $\mathbf{a}$  from GBLUP!



*Review*

## Single-Step Genomic Evaluations from Theory to Practice: Using SNP Chips and Sequence Data in BLUPF90

Daniela Lourenco <sup>1,\*</sup>, Andres Legarra <sup>2</sup>, Shogo Tsuruta <sup>1</sup> , Yutaka Masuda <sup>1</sup>, Ignacio Aguilar <sup>3</sup>   
and Ignacy Misztal <sup>1</sup>

<https://www.mdpi.com/2073-4425/11/7/790>

# ssGBLUP and ssSNP-BLUP are also equivalent!

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{H}^{-1} \frac{\sigma_e^2}{\sigma_u^2} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{W}'\mathbf{y} \end{bmatrix}$$

## ssGBLUP

Misztal et al. (2009)  
 Legarra et al. (2009)  
 Aguilar et al. (2010)  
 Christensen & Lund (2010)

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{Z}\mathbf{M} & \mathbf{X}'_n\mathbf{Z}_n \\ \mathbf{M}'\mathbf{Z}'\mathbf{X} & \mathbf{M}'\mathbf{Z}'\mathbf{Z}\mathbf{M} + \mathbf{I} \frac{\sigma_e^2}{\sigma_a^2} & \mathbf{M}'_n\mathbf{Z}'_n\mathbf{Z}_n \\ \mathbf{Z}'_n\mathbf{X}_n & \mathbf{Z}'_n\mathbf{Z}_n\mathbf{M}_n & \mathbf{Z}'_n\mathbf{Z}_n + \mathbf{A}^{nn} \frac{\sigma_e^2}{\sigma_g^2} \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\boldsymbol{\alpha}} \\ \hat{\boldsymbol{\epsilon}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{M}'\mathbf{Z}'\mathbf{y} \\ \mathbf{Z}'_n\mathbf{y}_n \end{bmatrix}$$

## ssSNPBLUP or ssBR

Fernando et al. (2014)  
 Liu et al. (2014)  
 Mantysaari & Strandén (2016)



J. Dairy Sci. 101:10082–10088  
<https://doi.org/10.3168/jds.2018-14913>

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**Short communication: Genomic prediction using different single-step methods in the Finnish red dairy cattle population**

H. Gao,<sup>\*,†,‡</sup> M. Koivula,<sup>‡</sup> J. Jensen,<sup>\*</sup> I. Strandén,<sup>‡</sup> P. Madsen,<sup>\*</sup> T. Pitkänen,<sup>‡</sup> G. P. Aamand,<sup>‡</sup>  
 and E. A. Mantysaari<sup>‡</sup>

<sup>\*</sup>Center for Quantitative Genetics and Genomics, Department of Molecular Biology and Genetics, Aarhus University, DK-8830 Tjele, Denmark

<sup>†</sup>Nordic Cattle Genetic Evaluation, DK-8200 Aarhus, Denmark

<sup>‡</sup>Natural Resources Institute Finland (Luke), FIN-31600 Jokioinen, Finland

We confirmed that regular ssGBLUP and ssBR with an extra polygenic effect led to the same predictions.

# SNP effects in ssGBLUP

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{H}^{-1}\lambda_1 \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{W}'\mathbf{y} \end{bmatrix}$$

$$\hat{\mathbf{a}} = \alpha b \frac{1}{2\sum p_i(1-p_i)} \mathbf{Z}' \mathbf{G}^{-1} \hat{\mathbf{u}}$$

Matrix of SNP content
Genomic relationship matrix

$\alpha$  = blending parameter for  $\mathbf{G}$

$$\lambda = \frac{1}{n^2} \left( \sum_i \sum_j \mathbf{A}_{22ij} - \sum_i \sum_j \mathbf{G}_{ij} \right) \quad b = 1 - \frac{\lambda}{2}$$

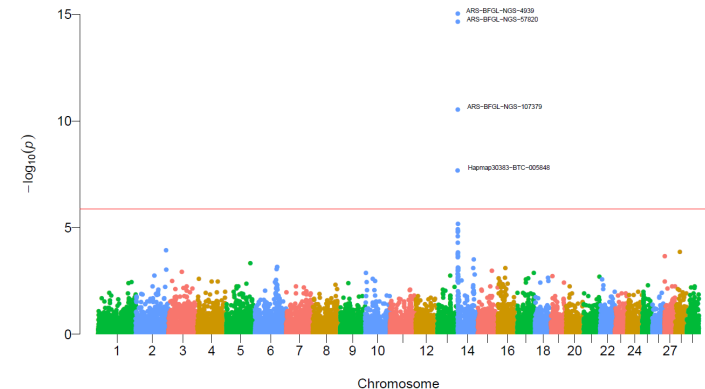
# What can we do with SNP effects?

## 1) Predictions for animals not included in the evaluation

Indirect Predictions

Indirect Genomic Predictions

## 2) Genome-Wide Association Studies (GWAS)



# 1) Indirect Predictions

- Interim evaluations
  - Between official runs
- Not all genotyped animals are in the evaluations
  - Animals with incomplete pedigree increase bias and lower  $R^2$
- Commercial products
  - e.g., GeneMax -> genomic testing for non-registered animals



# 1) Indirect Predictions

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{H}^{-1}\lambda_1 \end{bmatrix} \begin{bmatrix} \hat{\boldsymbol{\beta}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{W}'\mathbf{y} \end{bmatrix} \quad \Rightarrow \quad \hat{\mathbf{a}} = \alpha b \frac{1}{2\sum p_i(1-p_i)} \mathbf{Z}'\mathbf{G}^{-1} \hat{\mathbf{u}}$$

Indirect Prediction:  $\mathbf{IP} = \mathbf{u}_m^* = \mathbf{Z}\hat{\mathbf{a}}$

# 1) Indirect Predictions

Indirect Prediction:  $\mathbf{u}_m^* = \mathbf{Z}\hat{\mathbf{a}}$

└─ Fine if comparing among animals with IP

- Not fine if comparing IP with GEBV from the main evaluation
  - Need to put IP in the pedigree scale

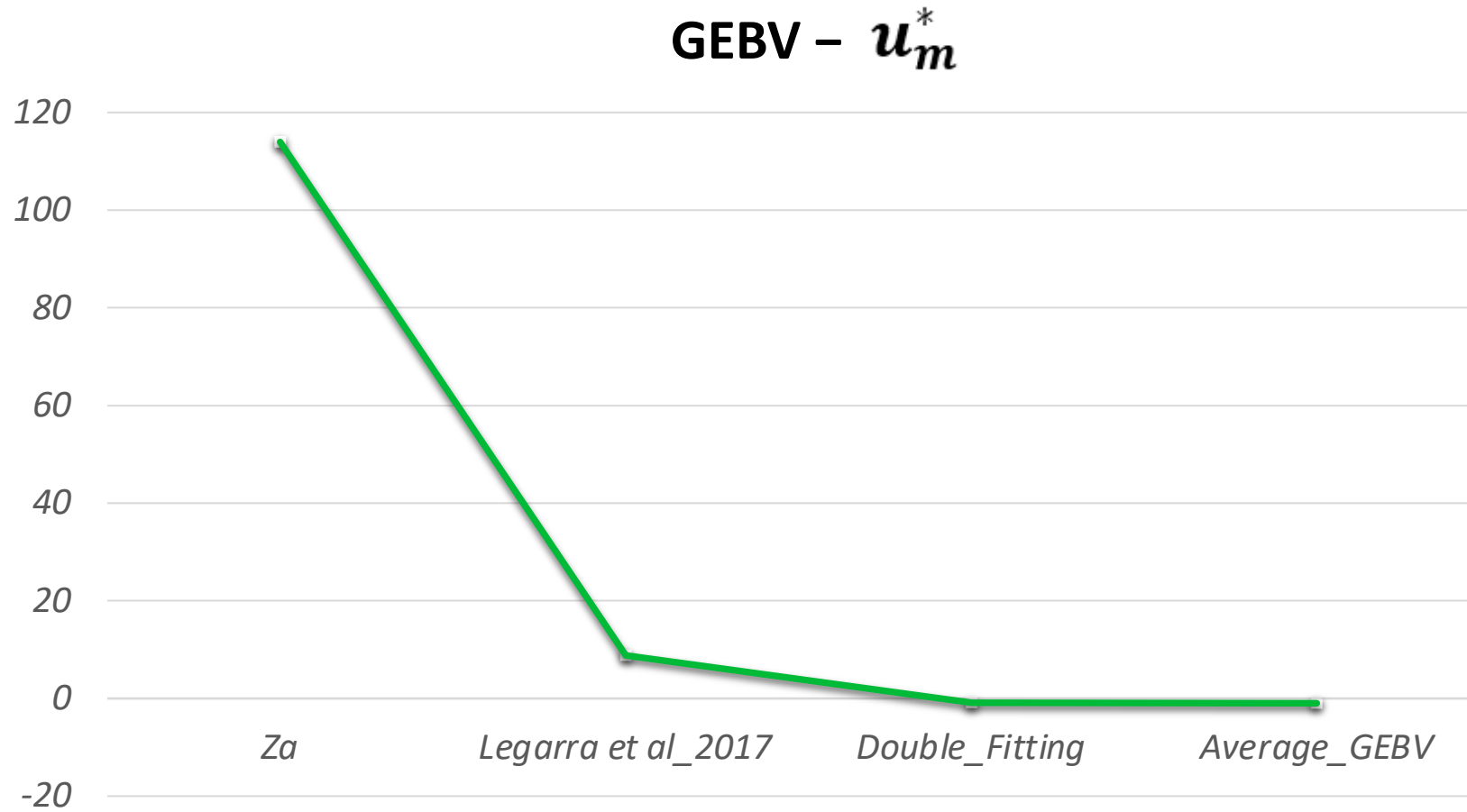
$$\mathbf{u}_m = \hat{\boldsymbol{\mu}} + \mathbf{u}_m^*$$

└─  $\hat{\boldsymbol{\mu}} = \alpha\lambda\mathbf{1}'\mathbf{G}^{-1}\hat{\mathbf{u}}$

$\alpha$  = blending parameter for  $\mathbf{G}$

$$\lambda = \frac{1}{n^2} \left( \sum_i \sum_j \mathbf{A}_{22ij} - \sum_i \sum_j \mathbf{G}_{ij} \right)$$

# 1) Indirect Predictions



# How to compute Indirect predictions

1) Pedigree + phenotypes + genotypes

2) **renumf90**

3) preGSf90 to save clean files

4) **blupf90+** (save the clean files)

- Good practice to save time: `OPTION saveGInverse + OPTION saveA22Inverse`

5) **postGSf90** (with clean files)

- BLUPF90 family software to compute SNP effects (+more)
- Same parameter file as `blupf90+`
- Good practice to save time: `OPTION readGInverse + OPTION readA22Inverse`

# Output from postGSf90

snp\_sol

<http://nce.ads.uga.edu/wiki/doku.php?id=readme.pregsf90>

contains solutions of SNP and weights

- 1: trait
- 2: effect
- 3: SNP
- 4: Chromosome
- 5: Position
- 6: SNP solution
- 7: weight

snp\_pred

- 1<sup>st</sup> line: model, tuning, blending information
- 2<sup>nd</sup> line: Trait/effect info
- AF in 10 columns
- $\mu_{\text{hat}}$ ,  $\text{var}_{\mu_{\text{hat}}}$
- SNP effects

# How to compute Indirect Predictions

## 6) pred90

- Have to provide a SNP file for the new genotyped animals to receive IP
  - same SNP as in the clean file

```
pred90 --snpfile newgen.txt --use_mu_hat
```

- The last statement adds the base, so that we have:  $\mathbf{u}_m = \hat{\boldsymbol{\mu}} + \mathbf{u}_m^*$

# Output from pred90

## SNP\_predictions

Animal ID      SNP call rate      Indirect Predictions

```
UGA50014      1.00      0.17414457
UGA50016      1.00      0.72332874E-01
UGA50042      1.00      1.0016705
UGA50058      1.00      0.17190497
UGA50060      1.00      0.98674759E-01
UGA50065      1.00     -0.60623702E-01
UGA50073      1.00     -0.17860851
UGA50077      1.00     -0.21597147
UGA50079      1.00     -0.69586390
UGA50084      1.00      1.0600574
UGA50085      1.00     -0.28602412
UGA50088      1.00     -0.12758011
```

pred90 can also compute accuracy of indirect predictions

```
OPTION snp_p_value  #in blupf90+
OPTION snp_var      #in postGSf90
--acc               #in pred90
```

Garcia et al. *Genetics Selection Evolution* (2022) 54:66  
<https://doi.org/10.1186/s12711-022-00752-4>



RESEARCH ARTICLE

Open Access

Theoretical accuracy for indirect predictions  
based on SNP effects from single-step GBLUP



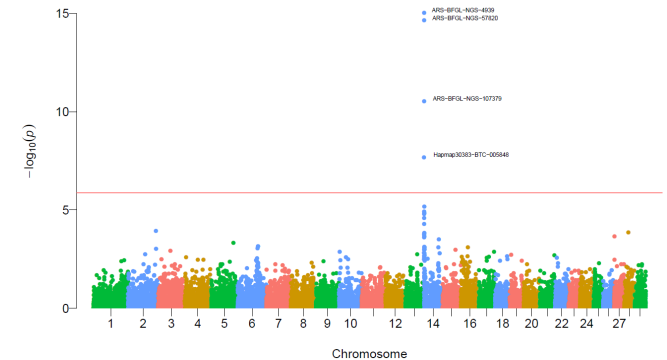
Andre Garcia<sup>1\*</sup>, Ignacio Aguilar<sup>2</sup>, Andres Legarra<sup>3</sup>, Shogo Tsuruta<sup>1</sup>, Ignacy Misztal<sup>1</sup> and Daniela Lourenco<sup>1</sup>

## 2) Genome-wide Association Studies



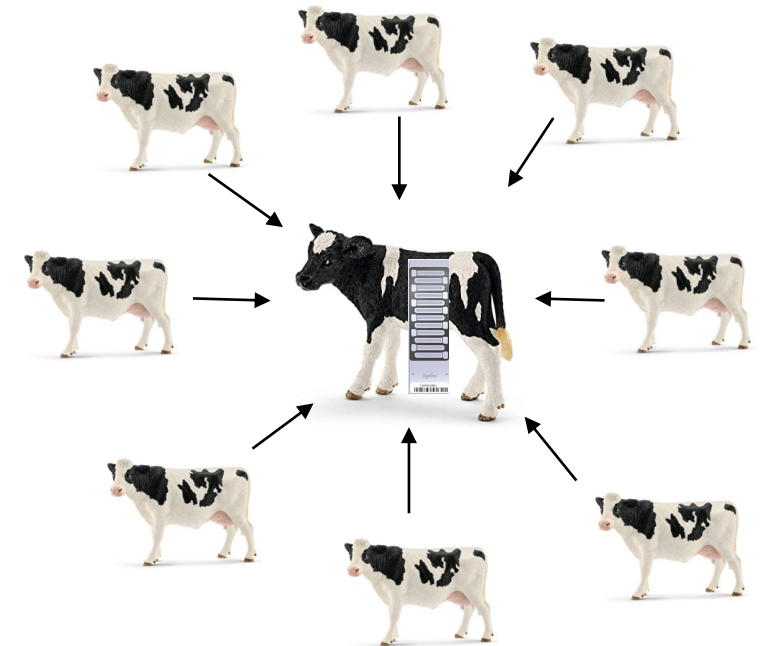
# Current standard for GWAS

- Single marker regression with **G** to compensate for relationships
  - $\mathbf{y} = \mathbf{X}\mathbf{b} + \mathbf{z}_i\mathbf{a}_i + \mathbf{u} + \mathbf{e}$ 
    - **z**: gene content {0,1,2}
    - **a**: SNP effect
- Estimate SNP effects
- Get p-values as  $pval_i = 2 \left( 1 - \Phi \left( \left| \frac{\hat{a}_i}{sd(\hat{a}_i)} \right| \right) \right)$
- Apply Bonferroni to correct for multiple testing
- **Assumption: Genotyped individuals have phenotypes**



# GWAS in livestock populations

- Most animals are non-genotyped
- Animals may not have phenotypes
- Some traits are sex-limited
  - milk, fat, protein
- Single marker regression
  - Only genotyped animals with phenotypes
  - Deregressed EBV
- Need a method that fits the livestock data
  - ssGWAS



# Single-step GWAS (historical)

SNP  
effects

GEBVs

$$\hat{\mathbf{a}} = \alpha b \frac{1}{2\sum p_i(1-p_i)} \mathbf{Z}'\mathbf{G}^{-1}\hat{\mathbf{u}}$$

VanRaden 2008  
Stranden and Garrick 2009  
Wang et al. 2012

a) Quadratic SNP variance (Falconer & Mackay, 1996)

$$d_i = \hat{a}_i^2 2p_i(1-p_i)$$

b) Nonlinear A SNP variance (VanRaden, 2008)

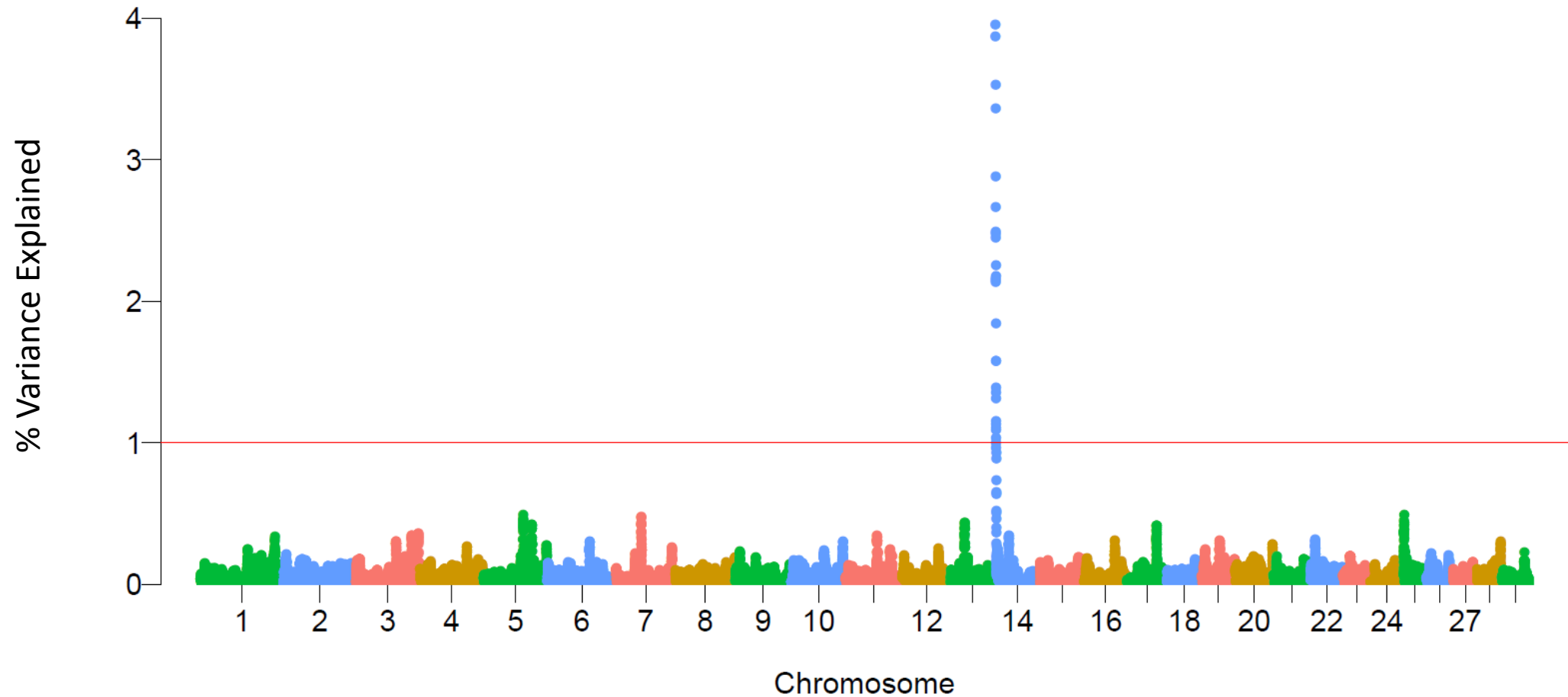
$$d_i = 1.125 \frac{|\hat{a}_i|}{sd(\hat{\mathbf{a}})} - 2$$

# Single-step GWAS

Fat – US Holsteins

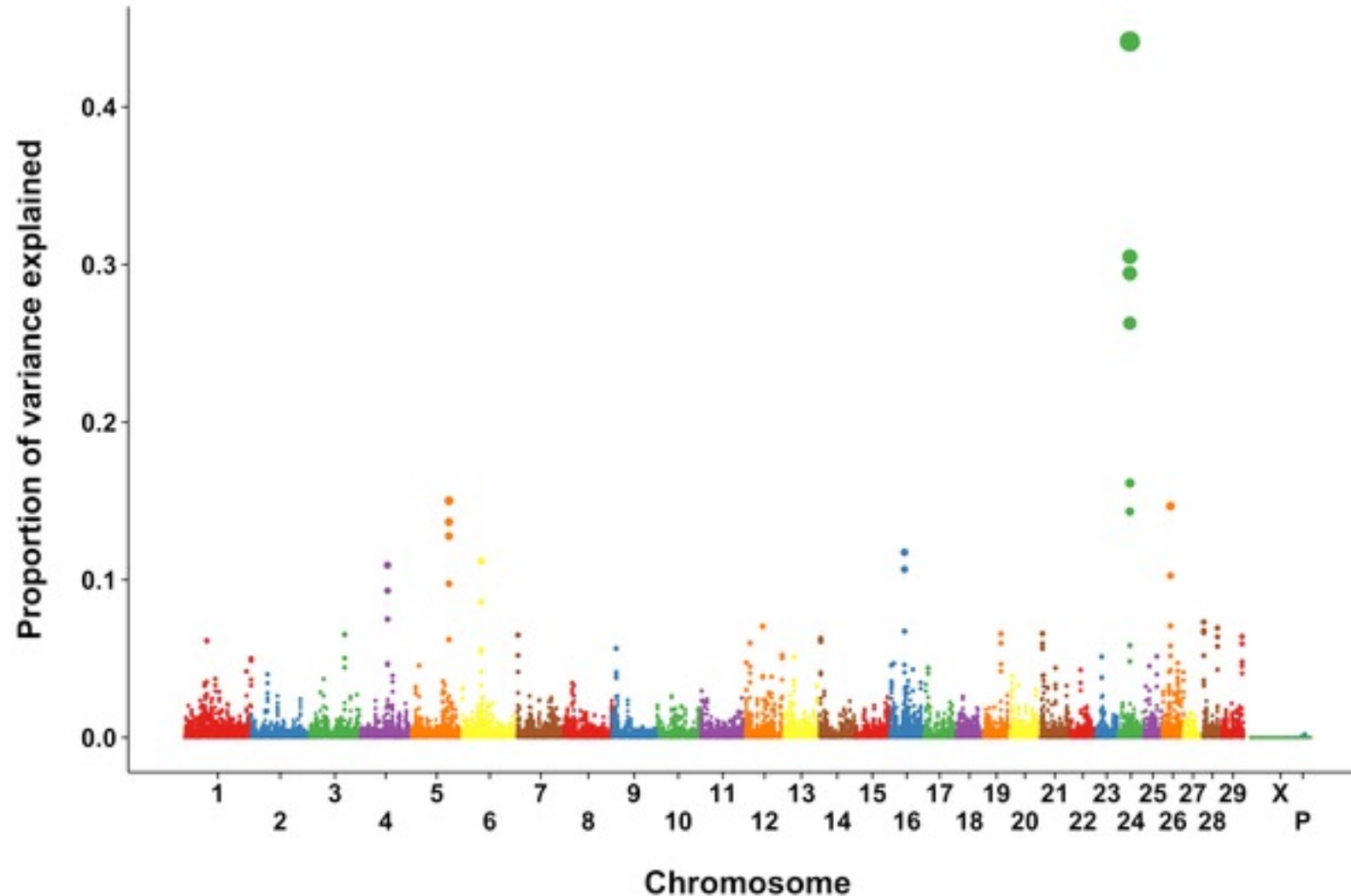
No P-value!!!

Manhattan plot of Variances



# Single-step GWAS

Figure 2. Proportion of SNP variance explained by 5-SNP moving windows for rectal temperature from a **single-step GBLUP** analysis



No P-value!!!

# Can we have p-values in ssGWAS?

Gualdrón Duarte et al. *BMC Bioinformatics* 2014, 15:246  
<http://www.biomedcentral.com/1471-2105/15/246>



## METHODOLOGY ARTICLE

## Open Access

### Rapid screening for phenotype-genotype associations by linear transformations of genomic evaluations

Jose L Gualdrón Duarte<sup>1</sup>, Rodolfo JC Cantet<sup>1</sup>, Ronald O Bates<sup>2</sup>, Catherine W Ernst<sup>2</sup>, Nancy E Raney<sup>2</sup> and Juan P Steibel<sup>2,3\*</sup>

### Genome-Wide Association Analyses Based on Broadly Different Specifications for Prior Distributions, Genomic Windows, and Estimation Methods

Chunyu Chen,<sup>1</sup> Juan P. Steibel, and Robert J. Tempelman  
Department of Animal Science, Michigan State University, East Lansing, Michigan 48824  
ORCID ID: 0000-0002-7833-6730 (R.J.T.)

Aguilar et al. *Genet Sel Evol* (2019) 51:28  
<https://doi.org/10.1186/s12711-019-0469-3>

## SHORT COMMUNICATION



## Open Access

### Frequentist p-values for large-scale-single step genome-wide association, with an application to birth weight in American Angus cattle

Ignacio Aguilar<sup>1</sup>, Andres Legarra<sup>2\*</sup>, Fernando Cardoso<sup>3,4</sup>, Yutaka Masuda<sup>5</sup>, Daniela Lourenco<sup>5</sup> and Ignacy Misztal<sup>5</sup>

## ANIMAL GENETICS Immunogenetics, Molecular Genetics and Functional Genomics

doi: 10.1111/age.12378

### Meta-analysis of genome-wide association from genomic prediction models

Y. L. Bernal Rubio<sup>\*†</sup>, J. L. Gualdrón Duarte<sup>\*</sup>, R. O. Bates<sup>\*</sup>, C. W. Ernst<sup>\*</sup>, D. Nonneman<sup>‡</sup>, G. A. Rohrer<sup>‡</sup>, A. King<sup>‡</sup>, S. D. Shackelford<sup>‡</sup>, T. L. Wheeler<sup>‡</sup>, R. J. C. Cantet<sup>†§</sup> and J. P. Steibel<sup>\*¶</sup>



J. Dairy Sci. 101:3140–3154  
<https://doi.org/10.3168/jds.2017-13364>  
© American Dairy Science Association®, 2018.

### Genome-wide association analyses based on a multiple-trait approach for modeling feed efficiency

Y. Lu,<sup>\*</sup> M. J. Vandehaar,<sup>\*</sup> D. M. Spurlock,<sup>†</sup> K. A. Weigel,<sup>‡</sup> L. E. Armentano,<sup>‡</sup> E. E. Connor,<sup>§</sup> M. Coffey,<sup>#</sup> R. F. Veerkamp,<sup>||</sup> Y. de Haas,<sup>||</sup> C. R. Staples,<sup>¶</sup> Z. Wang,<sup>\*\*</sup> M. D. Hanigan,<sup>††</sup> and R. J. Tempelman<sup>\*†</sup>

# P-values in ssGWAS

1) Factorize and Invert LHS of ssGBLUP with YAMS (Masuda et al., 2014)

2) Solve the MME for  $\begin{bmatrix} \hat{\beta} \\ \hat{u} \end{bmatrix}$  using the sparse Cholesky factor

3) Extract coefficients for genotyped animals ( $\mathbf{C}^{u_2 u_2}$ ) from  $\mathbf{LHS}^{-1}$

4) Obtain individual prediction error variance of SNP effects:

$$Var(\hat{a}_i) = \alpha b \frac{1}{2 \sum p_i (1 - p_i)} \mathbf{z}_i' \mathbf{G}^{-1} (\mathbf{G} \sigma_u^2 - \mathbf{C}^{u_2 u_2}) \mathbf{G}^{-1} \mathbf{z}_i \frac{1}{2 \sum p_i (1 - p_i)} \alpha b$$

(Gualdron-Duarte et al., 2014)

5) Backsolve GEBV to SNP effects ( $\hat{a}$ ):  $\hat{a} = \alpha b \frac{1}{2 \sum p_i q_i} \mathbf{Z}' \mathbf{G}^{-1} \hat{u}$

$$6) p\text{-value}_i = 2 \left( 1 - \Phi \left( \left| \frac{\hat{a}_i}{sd(\hat{a}_i)} \right| \right) \right)$$

$\Phi$  is the cumulative standard normal function

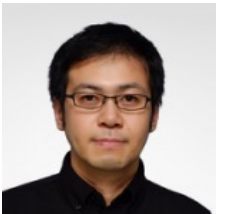
**blupf90+**



Ignacio  
Aguilar



Andres  
Legarra



Yutaka  
Masuda

**postGSf90**

# How to run ssGWAS with p-values in BLUPF90

- After renumf90 and preGSf90 to save clean files:
  - blupf90+ to estimate GEBV
    - OPTION SNP\_file `snp.dat_clean`
    - OPTION map\_file `mrkmap.txt_clean`
    - OPTION saveGInverse
    - OPTION saveA22Inverse
    - OPTION snp\_p\_value
  - postGSf90 to backsolve GEBV to SNP effect
    - OPTION SNP\_file `snp.dat_clean`
    - OPTION map\_file `mrkmap.txt_clean`
    - OPTION readGInverse
    - OPTION readA22Inverse
    - OPTION snp\_p\_value
    - OPTION windows\_variance X #if need variance explained by X SNP



# Output from postGSf90

chr<sub>sn</sub>\_pval

contains data to create plot by GNUPLOT

- 1: trait
- 2: effect
- 3:  $-\log_{10}(\text{p-value})$
- 4: SNP
- 5: Chromosome
- 6: Position in bp

Pft1e2.gnuplot

Pft1e2.R

chr<sub>sn</sub>

contains data to create plot by GNUPLOT

- 1: trait
- 2: effect
- 3: values of SNP effects to use in Manhattan plots  $\rightarrow [\text{abs}(\text{SNP}_i)/\text{var}(\text{SNP})]$
- 4: SNP
- 5: Chromosome
- 6: Position

Sft1e2.gnuplot

Sft1e2.R

# Output from postGSf90

```
chrnpvar
```

contains data to create plot by GNUPLOT

- 1: trait
- 2: effect
- 3: variance explained by  $n$  adjacents SNP
- 4: SNP
- 5: Chromosome
- 6: Position

Vft1e2.gnuplot

Vft1e2.R

# Output from postGSf90

snp\_sol

contains solutions of SNP and weights

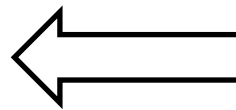
- 1: trait
- 2: effect
- 3: SNP
- 4: Chromosome
- 5: Position
- 6: SNP solution
- 7: weight

if `OPTION windows_variance` is used

- 8: variance explained by  $n$  adjacents SNP.

if `OPTION snp_p_value` is used

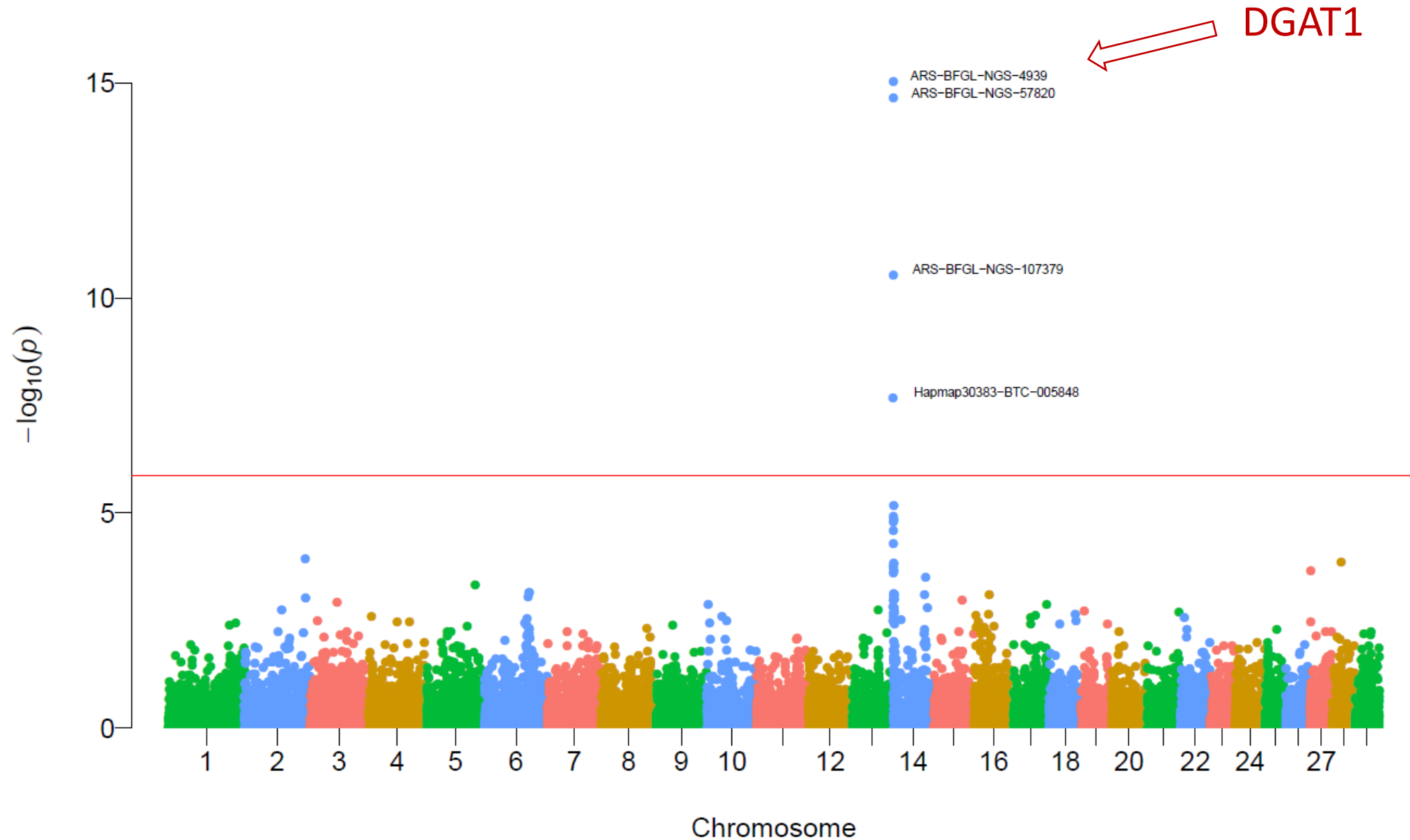
- 9: variance of the SNP solution (used to compute the p-value)



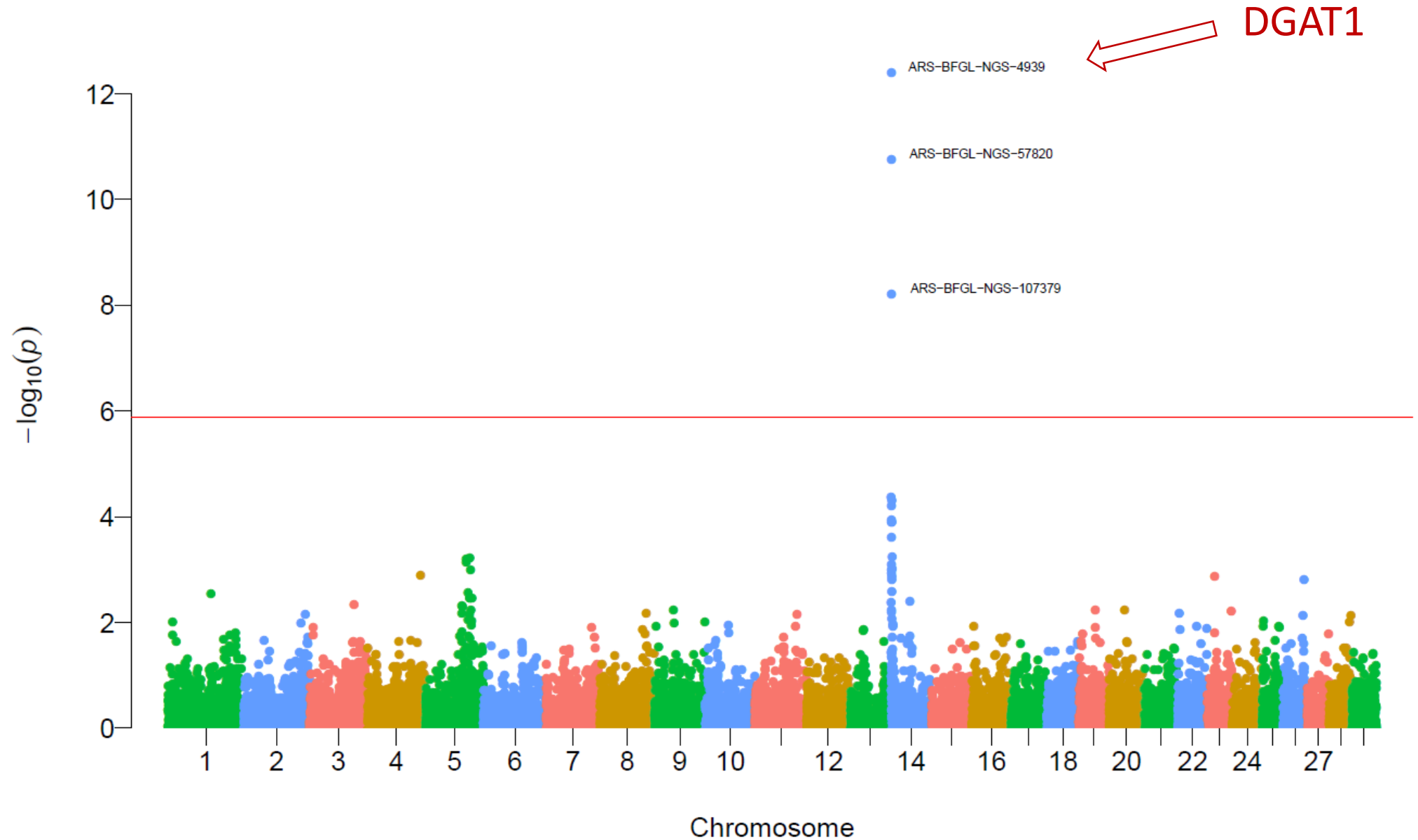
# P-values in ssGWAS for US Holsteins

- US HOL 2009 data: milk, fat, protein
- Single-trait models
  - 10k genotyped bulls
  - 752k records for 100k daughters
  - 303k animals in ped

# P-values in ssGWAS - Milk

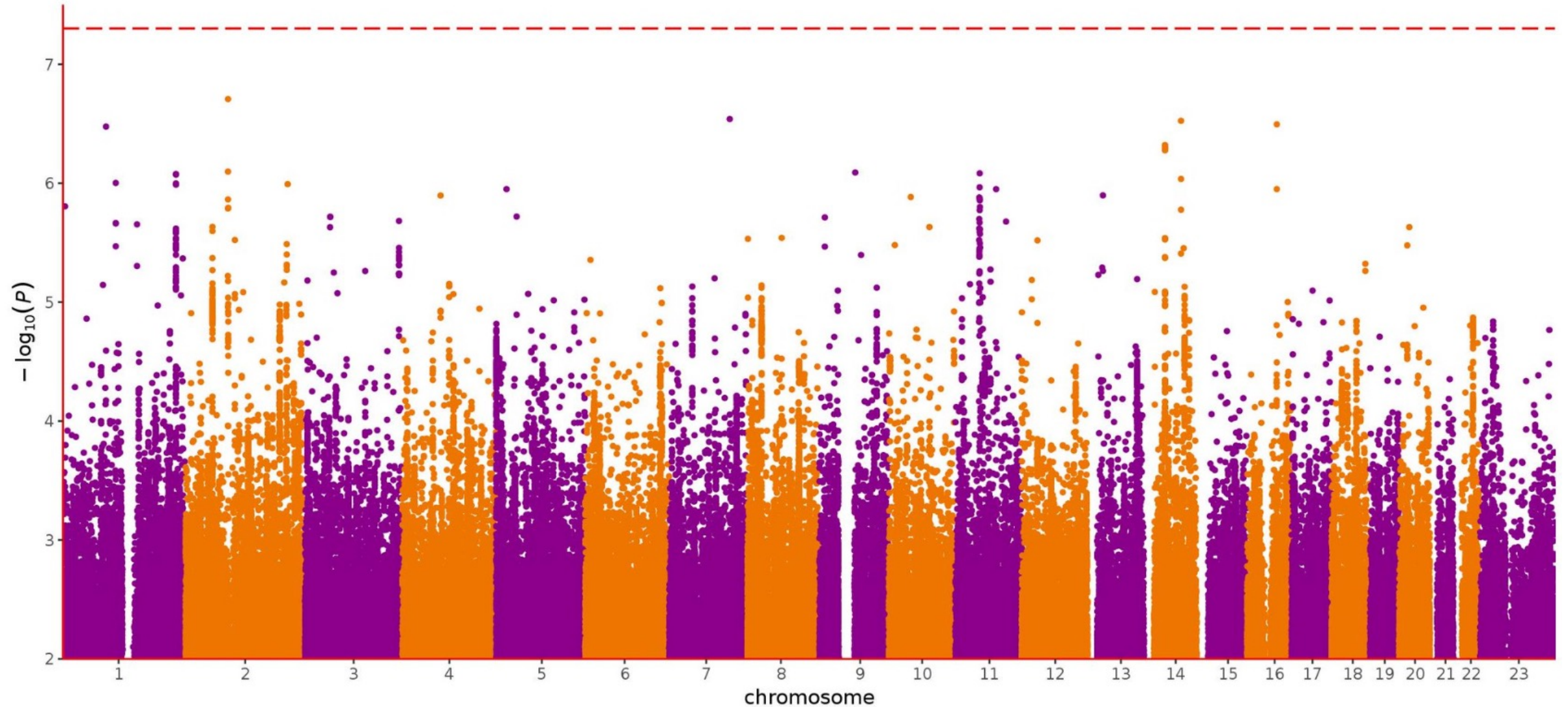


# P-values in ssGWAS - Fat



# Non-significant hits

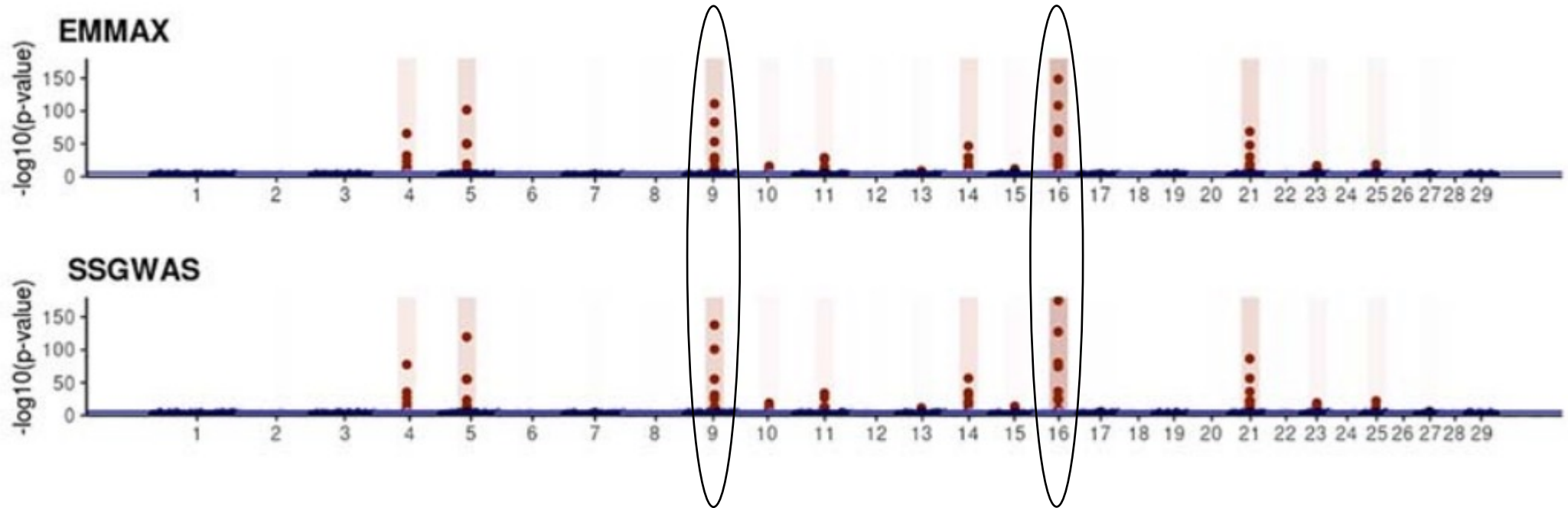
Work/job satisfaction  
N=82190



# ssGWAS vs. EMMAX

- Simulated population (1 QTN per CHR)

14k genotyped sires  
Deregressed EBV  
(10 daughters)



14k genotyped sires  
500k Pedigree  
250k phenotypes

Association	EMMAX (Khang et al., 2010)	ssGWAS (Aguilar et al., 2019)
True Positive	55.2 <sup>a</sup> (3.7)	61.6 <sup>a</sup> (8.7)
False Positive	0.0	0.0



# postGSf90 options

<http://nce.ads.uga.edu/wiki/doku.php?id=readme.pregsf90>

```
OPTION Manhattan_plot
```

Uses GNUPLOT to plot the Manhattan plot (SNP effects) for each trait and correlated effect.

```
OPTION Manhattan_plot_R
```

Uses R to plot the Manhattan plot (SNP effects) for each trait and correlated effect.

pdf images are created: *manplot\_St1e2.pdf*, but other formats can be specified.

Note: *t1e2* corresponds to trait 1, effect 2.

```
OPTION Manhattan_plot_R_format <format>
```

Control the format type to create images in R

`format` values accepted:

- pdf (default)
- png
- tif

```
OPTION plotsnp <n>
```

Control the values of SNP effects to use in Manhattan plots

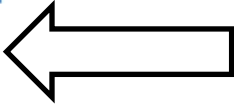
- 1: plot regular SNP effects: `abs(val)`
- 2: plot standardized SNP effects: `abs(val/sd)` (default)

# Output from postGSf90

snp\_sol

contains solutions of SNP and weights

- 1: trait
- 2: effect
- 3: SNP
- 4: Chromosome
- 5: Position
- 6: SNP solution
- 7: weight



if `OPTION windows_variance` is used

- 8: variance explained by  $n$  adjacents SNP.

if `OPTION snp_p_value` is used

- 9: variance of the SNP solution (used to compute the p-value)

# Weighted single-step GBLUP - WssGBLUP

# Weights for SNP in ssGBLUP

- ssGBLUP
  - Same weights for SNP

$$G = \frac{ZZ'}{2 \sum p_i(1-p_i)}$$

- WssGBLUP
  - Different weights for SNP

$$G = \frac{ZDZ'}{2 \sum p_i(1-p_i)}$$

- Weights may increase accuracy of GEBV
- If SNPs explain high %variance

# SNP effect and weights in ssGBLUP

$$\begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{W} \\ \mathbf{W}'\mathbf{X} & \mathbf{W}'\mathbf{W} + \mathbf{H}^{-1}\lambda \end{bmatrix} \begin{bmatrix} \hat{\mathbf{b}} \\ \hat{\mathbf{u}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{Z}'\mathbf{y} \end{bmatrix}$$

$$\hat{\mathbf{a}} = \frac{1}{2\sum p_i(1-p_i)} \mathbf{D} \mathbf{Z}' \mathbf{G}^{-1} \hat{\mathbf{u}}$$

Matrix of SNP weights

Matrix of SNP content

Genomic relationship matrix

a) Quadratic SNP weights (or variance) (Falconer & Mackay, 1996)

$$d_i = \hat{a}_i^2 2p_i(1-p_i) \quad \text{Default}$$

b) Nonlinear A SNP weights (or variance) (VanRaden, 2008)

$$d_i = 1.125 \frac{|\hat{a}_i|}{sd(\hat{\mathbf{a}})}^{-2}$$

# SNP weighting in ssGBLUP: WssGBLUP

- Wang et al. (2012):

1) Set  $\mathbf{D}_t = \mathbf{I}$  and  $\mathbf{G}_t = \frac{\mathbf{Z}\mathbf{D}\mathbf{Z}'}{2 \sum p_i(1-p_i)}$

2) Compute GEBV using ssGBLUP approach

3) Compute SNP effects as  $\hat{\mathbf{a}} = \lambda \mathbf{D} \mathbf{Z}' \mathbf{G}^{-1} \widehat{\mathbf{GEBV}}$

Diagonal matrix of weights

4) Calculate SNP weight

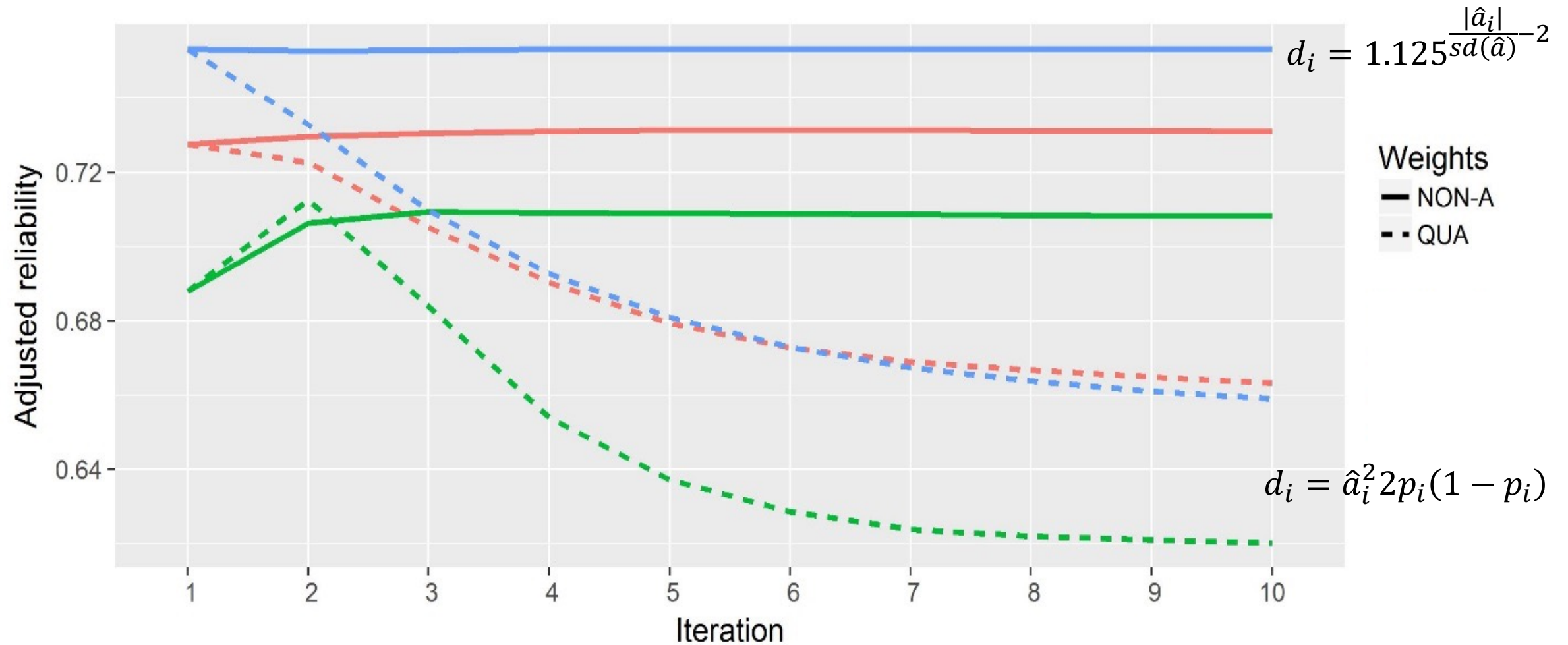
5) Normalize  $\mathbf{D}_{(t+1)}$

6)  $\mathbf{G}_{(t+1)} = \frac{\mathbf{Z}\mathbf{D}_{(t+1)}\mathbf{Z}'}{2 \sum p_i(1-p_i)}$

*“Iterative method  
needs  
convergence”*



# Convergence for nonlinear A and quadratic weight



# OPTION which\_weight nonlinearA

```
OPTION which_weight nonlinearA
```

$$d_i = 1.125 \frac{|\hat{a}_i|}{sd(\hat{a})}^{-2}$$

This option assumes the default constant (CT) is 1.125. To change the constant value to reflect a distribution closer to normal, use a CT value closer to 1:

```
OPTION which_weight nonlinearA 1.05
```

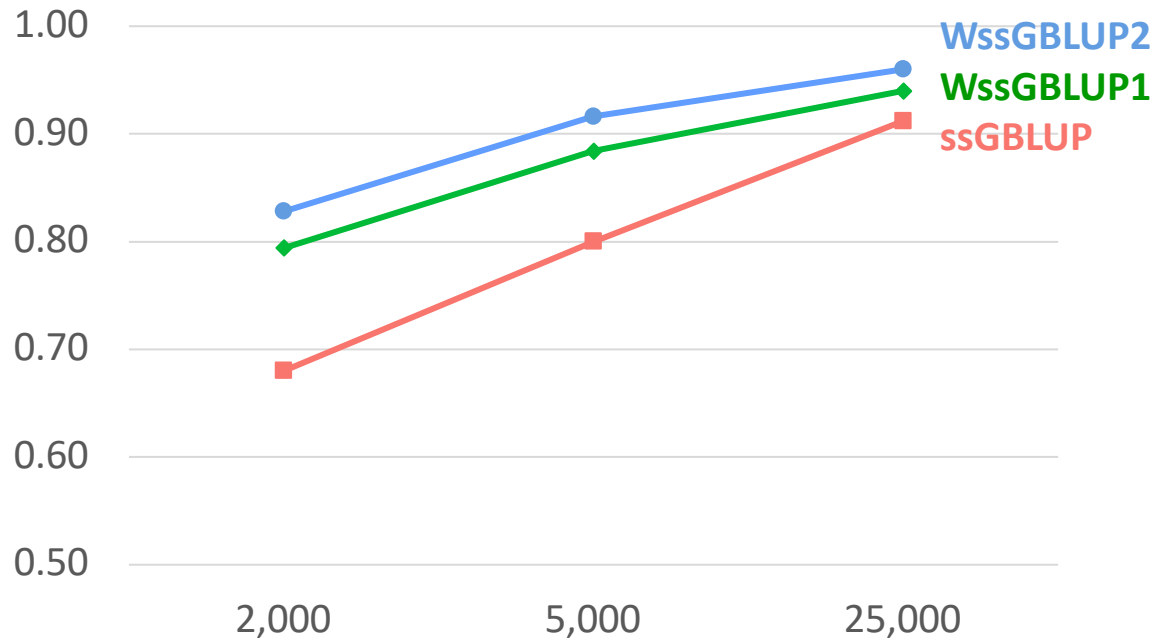
By default, the maximum change in SNP variance is limited to 5, which is calculated as  $CT^{(5-2)}$  and returns a value of 1.4238 with  $CT=1.125$ . If this limit is to be changed to 10, the following option can be used, where the value provided (x) is the result of the expression  $CT^{(x-2)}$ . As an example, if CT is 1.05 and x is 10, the value provided to the option should be 1.4775:

```
OPTION SNP_variance_limit 1.4775
```

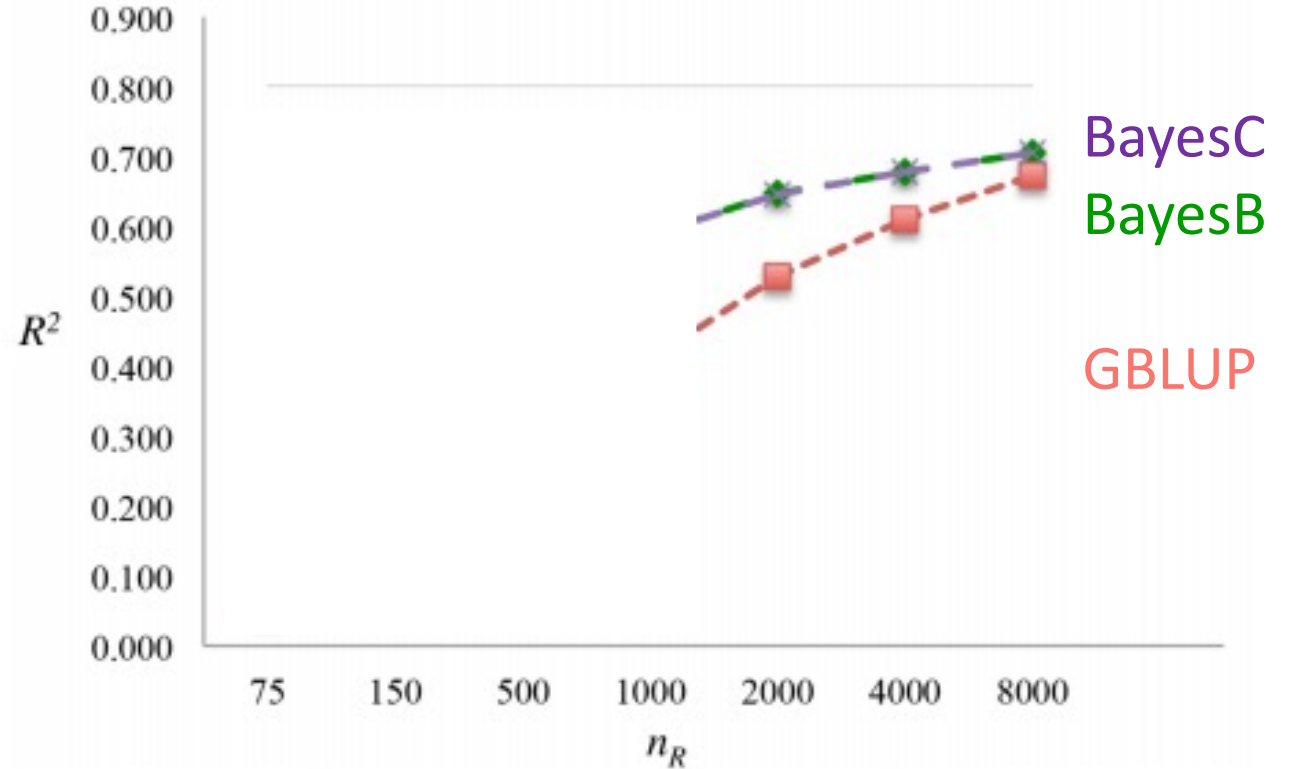


# WssGBLUP for large populations

10 QTN



Lourenco et al. (2017)



Karaman et al. (2016)

# How to run WssGBLUP in BLUPF90

- After renumf90 and preGSf90 to save clean files:
  - blupf90+ to estimate GEBV
    - `OPTION SNP_file snp.dat_clean`
    - `OPTION map_file mrkmap.txt_clean`
    - `OPTION saveGINverse`
    - `OPTION saveA22Inverse`
    - `OPTION weightedG w.txt` #vector of weights
  - postGSf90 to backsolve GEBV to SNP effect
    - `OPTION SNP_file snp.dat_clean`
    - `OPTION map_file mrkmap.txt_clean`
    - `OPTION readGINverse`
    - `OPTION readA22Inverse`
    - `OPTION which_weight nonlinearA`
    - `OPTION weightedG w.txt` #vector of weights
    - `OPTION windows_variance 1`

# How to run WssGBLUP for 3 iterations in BLUPF90

```
awk 'BEGIN { for (i==1;i<45000;i++) print 1}' > w.txt    # number of lines = number of SNP
```

```
for j in {1..3}
```

```
do
```

```
echo blup.par | blupf90+ | tee blup.log1_$j
cp solutions solutions1_$j
echo post.par | postGSf90 | tee post.log1_$j
cp snp_sol snp_sol1_$j
cp w.txt w.txt_$j
awk '{ if ($1==1) print $7}' snp_sol > w.txt
mkdir plot1_$j
cp chr.snp plot1_$j/chr.snp
cp chr.snpvar plot1_$j/chr.snpvar
rm chr.snp chr.snpvar snp_sol solutions
```

```
done
```

```
rm Gi A22i
```

# How to run WssGBLUP for 3 iterations and multi-trait models in BLUPF90

- Although the model can be multi-trait, there is only one **G**
  - Only one set of weights can be used
- To estimate correct weights for each trait in a multi-trait model:
  - Add an option in postGSf90

```
OPTION postgs_trt_eff x1 x2
```

- x1 is the trait you are interested (number of the trait)
  - x2 is the effect (number of effect in this case)
- Run once for each trait or effect of interest using weights for the specific trait or effect

## BLUPF90 Family of Programs

Now with support for genomic selection

*Ignacy Misztal and collaborators, University of Georgia*

BLUPF90 family of programs is a collection of software in Fortran 90/95 for mixed model computations in animal breeding. The goal of the software is to be as simple as with a matrix package and as efficient as in a programming language. For general description, see a [paper](#) from the CCB'99 workshop or see a [paper](#) on BGF90 at 7th WCGALP.

For variance component estimation, the family offers choices for simple and complicated models; see paper ["Reliable computing in estimation of variance components"](#). From 2009 the programs are successively modified for genomic selection using a [single-step](#) approach (or ssGBLUP) by Ignacio Aguilar and Shogo Tsuruta.

For support, join [blupf90](#) group at yahoo.com.

### Troubleshooting

⚠ If the software crashes with segmentation fault, please change settings in your operating system. See [FAQ:Segmentation fault](#) for details. Also, The [FAQ pages](#) provide useful suggestions and solutions.

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