

BLUPF90 - a flexible mixed model program in Fortran 90

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INTRODUCTION

BLUPF90 is a mixed model program written in Fortran 90. This program was developed step by step in my graduate level course and focuses on simplicity and model flexibility. It supports general multiple trait models with missing values and different models/trait, and random regressions. Memory allocation is automatic. Sparse matrix operations are supported through sparse matrix module SPARSEM. Currently, all variables are stored in memory and only solutions are provided; solutions to models with up to a few millions of equations can be obtained. Extra functionality such as prediction error variance and REML variance components for problems of moderate size can be added without too much programming.

Computing details

The program is modular. All details of the model are localized in a structure called *model*. Storage of the left hand side (LHS) of the system of equations is in matrix structures in memory. Solutions are obtained either iteratively by SOR or PCG, or by sparse Cholesky factorization by FSPAK. All equations are ordered within traits. Using the sparse matrix storage and solution by iteration, the program needs about 30 bytes for each nonzero of the LHS, which is upper stored, and an extra 24 bytes per equation. With an average of 10 nonzero elements per row, which would correspond to 5 in upper-storage only, the memory requirements would be approximately 174 bytes/equations. Assuming some overheads, BLUPF90 can solve up to 2million equations with 512 Mbytes of memory. Dense systems of equations would reduce that limit.

Files

Parameter file

BLUPF90 is driven by a parameter file, with a general format as shown below. Keywords in capital need to be included exactly as they appear. Fields in italic are those replaced by the user.

```
# Each keyword can be preceded by comments, each starting with  
#
```

DATAFILE

```
name of data file
```

NUMBER_OF_TRAITS

```
number of traits
```

NUMBER_OF_EFFECTS

```
number of effects
```

OBSERVATION (S)

```
position of observations in data file (one per trait)
```

WEIGHT (S)

```
position of weight(s) in data file (one per trait); blank if  
all weights equal
```

```
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT
```

[EFFECT NESTED]

one line per effect:

position of effect (one per trait)

number of levels

*type of effect (one of **cross** for crossclassified or **cov** for covariable)*

position of effect where nested (one per trait, optional)

RANDOM_RESIDUAL VALUES

residual variance covariance matrix (full stored)

RANDOM_GROUP

number of one random effect or list of correlated effects (order as in EFFECTS above); correlated effects must be consecutive

RANDOM_TYPE

*type of random effect: one of **diagonal**, **add_animal**, **add_sire**, **add_an_upg**, **add_an_upginb** or **par_domin***

FILE

relationship file; blank line if file unnecessary

(CO)VARIANCES

variance covariance matrix for given correlated effects and traits (full stored)

The section starting with "RANDOM-GROUP" is repeated for each random effect or each group of random effects. Each keyword can be preceded by a comment starting with #, however, comments cannot separate (co)variance matrices. See APPENDIX for examples of parameter files. To avoid typing mistakes, one can

Different models per trait and missing values

The value 0 is used as a code for missing values for both data and parameter files. If an effect is missing for one trait, assign 0 to its position. For example, assume that trait 1 has a contemporary group on position 1 with 1000 levels and trait 2 has a contemporary group on position 7 with 2000 levels. This can be coded in the parameter file as:

```
1 0 1000 cross
```

```
0 7 2000 cross
```

and, when effects are specific to one trait, can be merged into one line

```
1 7 2000 cross
```

where the number of levels is greater of the two. A similar merge of two effects is in the example of Appendix B.

Data file

The data file is in free format containing real and integer values only. BLUPF90 expects all effects to be numbered from 1 consecutively. For renumbering, use another program. A renumbering program specific to BLUPF90 called RENUMF90 is available as a binary for Linux and Windows.

Random effects and Pedigree files

There are a few types additive effects, each with a different pedigree format.

a) additive sire (add_sire)

The pedigree file has the following format:

animal number, sire number, maternal grandsire number
where unknown sire and/or maternal grandsire numbers are replaced by 0.

b) additive animal (add_animal)

The pedigree file (add_animal) has the following format:
animal number, sire number, dam number
where unknown sire and/or dam numbers are replaced by 0.

c) additive animal with unknown parent groups (add_an_upg)

The pedigree file has the following format:
animal number, sire number, dam number, parent code
where sire and/or dam numbers can be replaced by unknown parent numbers, and
parent code = 3 - number of known parents, i.e., 1 (both parents known), 2 (one parent
known), and 3 (both parents unknown).

d) additive animal with unknown parent groups and inbreeding (add_an_upginb)

The pedigree file has the following format:
animal number, sire number, dam number, inb/upg code
where sire and/or dam numbers can be replaced by unknown parent numbers, and

$$\text{inb/upg code} = 4000 / [(1+m_s)(1-F_s) + (1+m_d)(1-F_d)]$$

where m_s (m_d) is 0 whenever sire (dam) is known, and 1 otherwise, and F_s (F_d) is the
coefficient of inbreeding of the sire (dam). For example, the inb/upg code for the
animal with both parents known is 2000.

e) parental dominance

The pedigree class file has the following format:
s-d s-sd s-dd ss-d ds-d ss-sd ss-dd ds-sd ds-dd code
where x-y is a combination number of animals x and y, s is sire, d is dam, sd is sire of
dam, etc. Code is a number of 0 to 255 and refers to the combination of missing
subclasses. If one line is:

$$p \ s_8 \ s_7 \ s_6 \ s_5 \ s_4 \ s_3 \ s_2 \ s_1 \ \text{code}$$

then $\text{code} = \sum(a_i 2^{**i})$, where $a_i=0$ if $s_i=1$ and 1 otherwise. For example, the code
for a line with all nonzero parental subclasses is 255. For a line with only zero
parental subclasses, If classes are ordered so that lines with zero parental subclasses,
 $\text{code}=0$. If lines are ordered so that p for parental classes with $\text{code}=0$ are ordered last,
they may be omitted and will added automatically. The parental dominance file can be
obtained from program RENDOMN.

BLUPF90 facilitates inclusion of other relationship matrices, e.g., for autocorrelation

Output file

The solutions are written to file called "solutions"

Comments and bugs

Many crashes and errors involving the word "hash" result from too few levels defined in the
parameter file.

BLUPF90 computes generalized solution by several methods and with a different precision. With different methods of solving, the values of solutions are likely to change, but estimable functions should be the same. With a different precision, solutions may be slightly different.

References

Misztal, I. 1997. SPARSEM - sparse matrix module in Fortran 90. Available on my home page (<http://nce.ads.uga.edu/~ignacy/f90> or at <ftp://num.ads.uga.edu>).

Misztal, I. 1994. Comparison of software packages in animal breeding. Proc. 5th World Congress Gen. Appl. Livest. Prod. Vol. 22:3-10. Available on my home page.

I. Misztal. 1990. JAA20 - a mixed model using with iteration on data. *ibid.*

Misztal, I. 1999. Complex models, more data: simpler programming. Proc. Inter. Workshop Comput. Cattle Breed. '99, March 18-20, Tuusula, Finland. *Interbull Bul.* 20:33-42.

L.R. Schaeffer. 1985. Course - Advances in estimating breeding values and population parameters. Technical University Berlin, Germany.

L. R. Schaeffer and J.C.M. Dekkers. 1994. Random regressions in animal models for test-day production in dairy cattle. Proc. World Cong. Genet. Appl. Livest. Prod., University of Guelph, Canada, 19:443-446.

Appendix A

Single trait “USDA-type” animal model. This example is from the documentation of program JAA20.

$$y_{ijkl} = hys_i + hs_{ij} + p_k + a_k + e_{ijkl}$$

where

y_{ijkl} - production yield
 hys_i - fixed herd year season
 hs_{ij} - random herd x sire interaction
 p_k - random permanent environment
 a_k - random animal

and

$$\text{var}(hs_{ij}) = .05, \text{var}(p_k) = .1, \text{var}(a_k) = .5, \text{var}(e_{ijkl}) = 1$$

Data file (ic)

Format: animal/hys/p/hs/y

```
1 1 1 1 10
2 1 2 1 11
3 2 3 2 15
4 2 4 3 13
5 3 5 4 14
6 3 6 3 12
```

Relationship file (is)

Format: animal/dam/sire/code

```
1 12 8 2
2 1 8 1
3 2 9 1
4 7 10 1
5 12 11 2
6 1 10 1
7 13 14 3
8 5 11 1
9 13 8 2
10 7 14 2
11 13 14 3
```

Parameter file

```
# Example of single-trait animal model with one fixed effect
DATAFILE
ic
NUMBER_OF_TRAITS
1
NUMBER_OF_EFFECTS
4
OBSERVATION(S)
5
WEIGHT(S)

EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT
[EFFECT NESTED]
2 3 cross
3 6 cross
```

```

4 4 cross
1 14 cross
RANDOM_RESIDUAL VALUES
1
RANDOM_GROUP
2
RANDOM_TYPE
diagonal
FILE

```

```

(CO)VARIANCES
.1
RANDOM_GROUP
3
RANDOM_TYPE
diagonal
FILE

```

```

(CO)VARIANCES
.05
RANDOM_GROUP
4
RANDOM_TYPE
add_an_upg
FILE
is
(CO)VARIANCES
.5

```

Execution

```

/home/ignacy/f90/examples blupf90
name of parameter file?exiap

```

BLUPF90 1.00

Parameter file: exiap

Data file: ic

Number of Traits 1
Number of Effects 4
Position of Observations 5
Position of Weight (1) 0
Value of Missing Trait/Observation 0

```

EFFECTS
# type                            position (2)                    levels
[positions for nested]
1 cross-classified                2                                3
2 cross-classified                3                                6
3 cross-classified                4                                4
4 cross-classified                1                               14

```

Residual (co)variance Matrix
1.000

Random Effect 2
 Type of Random Effect: diagonal
 trait effect (CO)VARIANCES
 1 2 0.100

Random Effect 3
 Type of Random Effect: diagonal
 trait effect (CO)VARIANCES
 1 3 0.050

Random Effect 4
 Type of Random Effect: additive animal
 Pedigree File: is

trait effect (CO)VARIANCES
 1 4 0.500

REMARKS

- (1) Weight position 0 means no weights utilized
- (2) Effect positions of 0 for some effects and traits mean that such effects are missing for specified traits

Data record length = 5
 original G
 0.10
 inverted G
 10.00
 original G
 0.05
 inverted G
 20.00
 original G
 0.50
 inverted G
 2.00
 solutions stored in file: "solutions"

/home/ignacy/f90/examples cat solutions

trait/effect	level	solution
1 1	1	11.8589
1 1	2	13.7539
1 1	3	14.7086
1 2	1	-0.0088
1 2	2	0.0088
1 2	3	-0.0159
1 2	4	0.0159
1 2	5	0.0321
1 2	6	-0.0321
1 3	1	0.0000
1 3	2	-0.0079
1 3	3	-0.0081
1 3	4	0.0161
1 4	1	-1.7627
1 4	2	-0.9553
1 4	3	1.4288
1 4	4	-0.9206
1 4	5	-1.0781
1 4	6	-2.3474

1	4	7	0.8511
1	4	8	-0.1521
1	4	9	3.8926
1	4	10	-2.7717
1	4	11	0.8528
1	4	12	-3.1911
1	4	13	7.9976
1	4	14	-6.3340

Appendix B

Example of multiple trait sire model (from L.R. Schaeffer notes of 1985).

Models

$$\begin{aligned}\text{Trait 1: } & y_{1i} = h_i + s_{1j} + e_{1ijk} \\ \text{Trait 2: } & y_{2i} = \mu + s_{2j} + e_{2jk}\end{aligned}$$

where

h - fixed herd
s - random sire

and

$$\text{var}(s) = A \begin{bmatrix} 10 & 10 \\ 10 & 20 \end{bmatrix}, \quad \text{var}(e) = I \begin{bmatrix} 8 & 6 \\ 6 & 17 \end{bmatrix}$$

Data file (lrsdat)

Format: h/ μ /s/ y_1 / y_2

```
1 0 1 3.4 0
2 0 2 1.3 0
1 1 3 .8 50.3
2 1 4 4.5 52.6
0 1 5 0 55.0
```

Pedigree file (lrsrel)

Format: bull/sire/MGS

```
1 3 0
2 0 5
3 0 0
4 0 0
5 0 0
```

Parameter file (lrsex)

Example of two trait sire model with unequal models

DATAFILE

lrsdat

NUMBER_OF_TRAITS

2

NUMBER_OF_EFFECTS

2

OBSERVATION(S)

4 5

WEIGHT(S)

EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT
[EFFECT NESTED]

1 2 2 cross

3 3 5 cross

RANDOM_RESIDUAL_VALUES

10 10

10 20

RANDOM_GROUP

2

RANDOM_TYPE

add_sire

FILE

lrsrel

(CO)VARIANCES

8 6
6 17

Execution

/home/ignacy/f90/examples blupf90
name of parameter file?lrsex

BLUPF90 1.00

Parameter file: lrsex

Data file: lrsdat

Number of Traits 2
Number of Effects 2
Position of Observations 4 5
Position of Weight (1) 0
Value of Missing Trait/Observation 0

EFFECTS

#	type	position (2)	levels
1	cross-classified	1 2	2
2	cross-classified	3 3	5

[positions for nested]

Residual (co)variance Matrix

10.000	10.000
10.000	20.000

Random Effect 1
Type of Random Effect: additive sire
Pedigree File: lrsrel

trait	effect	(CO)VARIANCES	
1	2	8.000	6.000
2	2	6.000	17.000

REMARKS

(1) Weight position 0 means no weights utilized
(2) Effect positions of 0 for some effects and traits means
that such effects are missing for specified traits

Data record length = 5

original G
8.00 6.00
6.00 17.00
inverted G
0.17 -0.06
-0.06 0.08

solutions stored in file: "solutions"

/home/ignacy/f90/examples cat solutions

trait/effect	level	solution
1 1	1	2.3877

2	1	1	52.4449
1	1	2	3.2180
2	1	2	0.0000
1	2	1	0.2243
2	2	1	-0.0210
1	2	2	-0.8217
2	2	2	-0.3866
1	2	3	-0.4969
2	2	3	-0.7512
1	2	4	0.6178
2	2	4	-0.0769
1	2	5	0.2217
2	2	5	1.0851

Appendix C

This test-day model example comes from the paper of Schaeffer and Dekkers (WCGALP94 18:443)

Model

$$y_{ijkl} = h_i + \beta_1 X_{1j} + \beta_2 X_{2j} + a_k + \gamma_{1k} X_{1j} + \gamma_{2k} X_{2j} + e_{ijkl}$$

where

y_{ijkl} - yield of test day

h_i - test day effect

X_{1j} - days in milk

X_{2j} - log(days in milk)

β_1, β_2 - fixed regressions

a_k - random animal

γ_{1k}, γ_{2k} - random regressions for each animal

and

$$\text{var}(e_{ijkl}) = 1; \text{var}(a_k, \gamma_{1k}, \gamma_{2k}) = [2.25 \ 4 \ -.7; 4 \ 1375 \ 12; -.7 \ 12 \ 94]^{-1}$$

Data file (lrsrrdat)

Format: h/a/ X_1 / X_2 /y

```
1 1 73 1.42985 26
1 2 34 2.19395 29
1 3 8 3.64087 37
2 1 123 0.908127 23
2 2 84 1.28949 18
2 3 58 1.65987 25
2 4 5 4.11087 44
3 1 178 0.538528 21
3 2 139 0.785838 8
3 3 113 0.992924 19
3 4 60 1.62597 29
4 2 184 0.505376 1
4 3 158 0.657717 15
4 4 105 1.06635 22
4 5 14 3.08125 35
5 3 218 0.335817 11
5 4 165 0.614366 14
5 5 74 1.41625 23
5 6 31 2.28632 28
6 3 268 0.129325 7
6 4 215 0.349674 8
6 5 124 0.90003 17
6 6 81 1.32586 22
```

Relationship file (lrsrrrel)

Format: animal/sire/dam

```
1 9 7
2 10 8
3 9 2
4 10 8
5 11 7
6 11 1
7 0 0
8 0 0
9 0 0
10 0 0
```

11 0 0

Parameter file (exlrsrr)

Example of single-trait random-regression model

DATAFILE

lrsrrdat

NUMBER_OF_TRAITS

1

NUMBER_OF_EFFECTS

6

OBSERVATION(S)

5

WEIGHT(S)

EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT
[EFFECT NESTED]

1 6 cross

3 1 cov

4 1 cov

2 11 cross

3 11 cov 2

4 11 cov 2

RANDOM_RESIDUAL VALUES

1

RANDOM_GROUP

4 5 6

RANDOM_TYPE

add_animal

FILE

lrsrrrel

(CO)VARIANCES

.447906	-0.001334	0.003506
-0.001334	0.000732	-0.000103
0.003506	-0.000103	.010678

Execution

/home/ignacy/f90/examples blupf90

name of parameter file?exlrsrr

BLUPF90 1.00

Parameter file: exlrsrr

Data file: lrsrrdat

Number of Traits	1
Number of Effects	6
Position of Observations	5
Position of Weight (1)	0
Value of Missing Trait/Observation	0

EFFECTS

#	type	position (2)	levels
[positions for nested]			
1	cross-classified	1	6
2	covariable	3	1
3	covariable	4	1
4	cross-classified	2	11

5	covariable	3	11	2
6	covariable	4	11	2

Residual (co)variance Matrix
1.000

correlated random effects 4 5 6
Type of Random Effect: additive animal
Pedigree File: lrsrrrel

trait	effect	(CO)VARIANCES		
1	4	0.448	-0.001	0.004
1	5	-0.001	0.001	0.000
1	6	0.004	0.000	0.011

REMARKS

- (1) Weight position 0 means no weights utilized
- (2) Effect positions of 0 for some effects and traits means that such effects are missing for specified traits

Data record length = 5

original G

0.45	0.00	0.00
0.00	0.00	0.00
0.00	0.00	0.01

inverted G

2.25	4.00	-0.70
4.00	1375.09	11.95
-0.70	11.95	94.00

solutions stored in file: "solutions"

/home/ignacy/f90/examples cat solutions

trait/effect level solution

1	1	1	19.9496
1	1	2	20.3729
1	1	3	20.6095
1	1	4	19.7278
1	1	5	18.6035
1	1	6	17.8500
1	2	1	-0.0498
1	3	1	5.2912
1	4	1	-0.4430
1	4	2	0.2704
1	4	3	-0.7288
1	4	4	1.1019
1	4	5	-0.1626
1	4	6	-0.4828
1	4	7	-0.0988
1	4	8	0.4574
1	4	9	-0.6288
1	4	10	0.4574
1	4	11	-0.1872
1	5	1	0.0369
1	5	2	-0.0661
1	5	3	0.0068
1	5	4	-0.0054
1	5	5	0.0069

1	5	6	0.0167
1	5	7	0.0133
1	5	8	-0.0238
1	5	9	0.0350
1	5	10	-0.0238
1	5	11	-0.0008
1	6	1	-0.0370
1	6	2	0.0325
1	6	3	-0.0479
1	6	4	0.0767
1	6	5	-0.0149
1	6	6	-0.0377
1	6	7	-0.0103
1	6	8	0.0364
1	6	9	-0.0480
1	6	10	0.0364
1	6	11	-0.0145

Appendix D

This model was used for studies on multibreed evaluation in beef cattle. It is provided as an example of a model with maternal effect and different models per trait.

Model (in concise form, with most indices omitted)

$$y_1 = cg_1 + bt + mbt + a + M + e$$

$$y_2 = cg_2 + bt + mbt + a + M + pe + e$$

$$y_3 = cg_3 + bt + mbt + a + e$$

where

- y_{1-3} - birth weight, weaning weight, and gain
- cg_{1-3} - contemporary groups separate for each trait
- br - breed type
- mbt - maternal breed type
- a - additive effect
- m - maternal effect
- pe - permanent environmental effect of the dam

Data file (data.out)

Format:

1. contemporary group for trait 1
2. contemporary group for trait 2
3. contemporary group for trait 3
4. animal breed type
5. maternal breed type
6. animal id
7. dam id
8. birth weight
9. weaning weight
10. gain

Relationship file (pedi.outok)

Format:

- animal
- sire or unknown parent group
- dam or unknown parent group
- "1 + number of missing parents"

Parameter file (exlrsrr)

DATAFILE

data.out

NUMBER_OF_TRAITS

3

NUMBER_OF_EFFECTS

6

OBSERVATION(S)

8 9 10

WEIGHT(S)

EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT

[EFFECT

NESTED]

1 2 3 133085 cross

4 4 4 181 cross

5 5 0 165 cross

6 6 6 1724112 cross

7 7 0 1724112 cross

0 7 0 1724112 cross

RANDOM_RESIDUAL VALUES

26.3 0.0 0.0

0.0 1312.9 0.0

0.0 0.0 1246.3

RANDOM_GROUP

4 5

RANDOM_TYPE

add_an_upg

FILE

pedi.outok

(CO)VARIANCES

22.9 36.3 18.6 -4.6 0.0 0.0

36.6 500.2 110.8 0.0 -91.6 0.0

18.6 110.8 313.0 0.0 0.0 0.0

-4.6 0.0 0.0 10.1 0.0 0.0

0.0 -91.6 0.0 0.0 419.1 0.0

0.0 0.0 0.0 0.0 0.0 0.0

RANDOM_GROUP

2

RANDOM_TYPE

diagonal

FILE

(CO)VARIANCES

0.263 0.0 0.0

0.0 13.129 0.0

0.0 0.0 12.463

RANDOM_GROUP

3

RANDOM_TYPE

diagonal

FILE

(CO)VARIANCES

0.263 0.0 0.0

0.0 13.129 0.0

0.0 0.0 0.0

RANDOM_GROUP

6

RANDOM_TYPE

diagonal

FILE

(CO)VARIANCES

0.0	0.0	0.0
0.0	45.5	0.0
0.0	0.0	0.0

Appendix E

A single-trait random regression model for test-day milk is using cubic Legendre polynomials.

Model

$$y_{ijkl} = \text{hym}_{ij} + \sum_{m=1}^4 \alpha_m(l) h_{im} + \sum_{m=1}^4 \alpha_m(l) u_{km} + \sum_{m=1}^4 \alpha_m(l) p_{im} + e_{ijkl}$$

where

y_{ijkl} - test day milk

hym_{ij} - herd-year-test for herd i and year-test j

h_i - effects of herd i

$\alpha_m(l)$ - value of m -th Legendre polynomial at point corresponding to $\text{DIM}=l$

u - additive effects

p_e - permanent environmental effects

Data file (datarr)

Format:

1. herd
2. herd-year-test
- 3-6. values of Legendre polynomials
7. weight for residuals: $100/\text{var}(e_{ijkl})$
8. test day
9. animal

Relationship file (pedirr)

Format:

animal
sire
dam

Parameter file (exrr3)

DATAFILE

datarr

NUMBER_OF_TRAITS

1

NUMBER_OF_EFFECTS

13

OBSERVATION(S)

8

WEIGHT(S)

7

EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT

2 3726 cross #herd-year-test

3 84 cov 1 #herd

4 84 cov 1

5 84 cov 1

6 84 cov 1

3 21874 cov 9 #additive

4 21874 cov 9

5 21874 cov 9

6 21874 cov 9
3 21874 cov 9 #pe
4 21874 cov 9
5 21874 cov 9
6 21874 cov 9

RANDOM_RESIDUAL VALUES

100

RANDOM_GROUP

6 7 8 9

RANDOM_TYPE

add_animal

FILE

pedirr

(CO)VARIANCES

(4 x 4 matrix)

RANDOM_GROUP

10 11 12 13

RANDOM_TYPE

diagonal

FILE

(CO)VARIANCES

(4 x 4 matrix)

Appendix F

A terminal cross model by Fernando et al. and Lo et al.

breed A: ya=cga + ua + ea
breed B: yb=cgb+ ub +eb
cross: yab=cgab+ uaab + ubab +eab

Data file (data_cross)

1. cg A (85 levels)
2. cg B (110 levels)
3. cg crossbred (87 levels)
4. animal - breed A (2400 animals) or parent from breed A
5. animal - breed B (3000 animals) or parent from breed B
7. ya
8. yb
9. yc

Pedigree files: pedig_A for breed A and pedig_B for breed B

Parameter file

```
# Example of a terminal-cross model
DATAFILE
data-cross
NUMBER_OF_TRAITS
3
NUMBER_OF_EFFECTS
3
OBSERVATION(S)
6 7 8
WEIGHT(S)

EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT
NESTED]
1 2 3 110 cross
4 0 4 2400 cross cross
0 5 5 3000 cross
RANDOM_RESIDUAL_VALUES
100 0 0
0 100 0
0 0 100
RANDOM_GROUP
2
RANDOM_TYPE
add_animal
FILE
pedig_A
(CO)VARIANCES
40 0 30
0 0 0
30 0 50
RANDOM_GROUP
3
RANDOM_TYPE
add_animal
FILE
pedig_B
(CO)VARIANCES
0 0 0
0 50 30
0 30 40
40 30
```

Appendix G

Example of a competitive model (a la Muir and Schinkel)

$$y = cg + a + c_1 + c_2 + \dots + c_5 + e$$

c_i is the effect of the i -th competitor; assumed pen size of up to 6.

Datafile (data_comp)

1. y
2. cg (max 120)
3. animal (max 3000)
4. competitor 1
5. c 2
- ...
8. c 5

if pen size is less than 10, unused fields set to 0.

Parameter file

```
# Example of a competitive model
```

```
DATAFILE
```

```
data_comp
```

```
NUMBER_OF_TRAITS
```

```
1
```

```
NUMBER_OF_EFFECTS
```

```
1
```

```
OBSERVATION(S)
```

```
1
```

```
WEIGHT(S)
```

```
EFFECTS: POSITIONS_IN_DATAFILE NUMBER_OF_LEVELS TYPE_OF_EFFECT [EFFECT  
NESTED]
```

```
2 120 cross
```

```
3 3000 cross
```

```
4 0 cross
```

```
5 0 cross
```

```
6 0 cross
```

```
7 0 cross
```

```
8 3000 cross
```

```
RANDOM_RESIDUAL VALUES
```

```
50
```

```
RANDOM_GROUP
```

```
2 3
```

```
RANDOM_TYPE
```

```
add_animal
```

```
FILE
```

```
pedig
```

```
VARIANCES
```

```
40 -10
```

```
-10 10
```

Appendix H

Design of the program

The model is completely described in the module MODEL.

```

module model
implicit none

!      Types of effects
integer,parameter::effcross=0,& !effects can be cross-classified
                    effcov=1    !or covariables

!      Types of random effects
integer, parameter :: g_fixed=1,&      ! fixed effect
                    g_diag=2, &      ! diagonal
                    g_A=3, &        ! additive animal
                    g_A_UPG=4, &    ! additive animal with unknown
                                !      parent groups
                    & g_A_UPG_INB=5, & ! additive animal with unknown
                                !      parent groups and inbreeding
                    & g_As=6,&      ! additive sire
                    g_PD =7, &      ! parental dominance
                    g_last=8       ! last type

character (40)      ::  parfile, &    !name of parameter file
                    datafile        !name of data set

integer :: ntrait,&          !number of traits
          neff,&            !number of effects
          miss=0           !value of missing trait/effect

integer,allocatable :: pos_y(:)      !positions of observations
integer ::          pos_weight      ! position of weight of records; zero if none

integer,allocatable :: pos_eff(:,:),& !positions of effects for each trait
                    nlev(:),&      !number of levels
                    effecttype(:),& !type of effects
                    nestedcov(:,:),& !position of nesting effect for each trait
                                ! if the effect is nested covariable
                    & randomtype(:),& ! status of each effect, as above
                    randomnumb(:)  ! number of consecutive correlated effects

character (40),allocatable:: randomfile(:) ! name of file associated with given
                                           ! effect

real, allocatable :: r(:,:),&      !residual (co)variance matrix
                    rinv(:,:),&   ! and its inverse
                    g(:,:,:)      ! The random (co)variance matrix for each trait
end module model

```

The core of the program is presented below.

```

program BLUPF90
use model;use sparsem; use sparseop
implicit none
real,allocatable :: y(:),&          ! observation value
                    indata(:)      ! one line of input data

real ::          weight_y          ! weight for records

type (sparse_hashm)::xx            ! X'X in sparse hash form
type (sparse_ija):: xx_ija        ! X'X in IJA form, for use with FSPAK only
real, allocatable:: xy(:),sol(:)  !X'Y and solutions

real,allocatable :: weight_cov(:,:)&
integer,allocatable:: address(:,:)& ! start and address of each effect
integer :: neq,io,&                ! number of equations and io-status
          data_len,&              ! length of data record to read
          i,j,k,l                 ! extra variables
real:: val, dat_eff

!
call read_parameters
call print_parameters
neq=ntrait*sum(nlev)

```

```

data_len=max(pos_weight,maxval(pos_y),maxval(pos_eff))
print*, 'Data record length = ', data_len
allocate (xy(neq), sol(neq), address(neff, ntrait), &
          weight_cov(neff, ntrait), y(ntrait), indata(data_len))
call zerom(xx, neq); xy=0
!
call setup_g           ! invert R matrices

open(50, file=datafile) !data file

! Contributions from records
do
  read(50, *, iostat=io) indata
  if (io.ne.0) exit
  call decode_record
  call find_addresses
  call find_rinv
  do i=1, neff
    do j=1, neff
      do k=1, ntrait
        do l=1, ntrait
          val=weight_cov(i, k)*weight_cov(j, l)*weight_y*rinv(k, l)
          call addm(val, address(i, k), address(j, l), xx)
        enddo
      enddo
    enddo
    do k=1, ntrait
      do l=1, ntrait
        xy(address(i, k))=xy(address(i, k))+rinv(k, l)*y(l)*weight_cov(i, k) &
          *weight_y
      enddo
    enddo
  enddo
enddo
!
! Random effects' contributions
do i=1, neff
  select case (randomtype(i))
  case (g_fixed)
    continue           ! fixed effect, do nothing
  case (g_diag)
    call add_g_diag(i)
  case (g_A, g_As, g_A_UPG, g_A_UPG_INB)
    call add_g_add(randomtype(i), i)
  case (g_PD)
    call add_g_domin(i)
  case default
    print*, 'unimplemented random type', randomtype(i)
  endselect
enddo

if (neq < 15) then
  print*, 'left hand side'
  call printm(xx)
  print '( ' ' right hand side: ' ', 100f8.1)', xy
endif

call solve_iterm(xx, xy, sol)

! Comment the line above and uncomments the lines below only if
! solutions by FSPAK are desired
!xx_ija=xx;
!call fspak90('solve', xx_ija, xy, sol)

if (neq < 15) print '( ' ' solution: ' ', 100f7.3)', sol

call store_solutions

```

Warning

When the program is modified to solve for different left hand sides repeatedly by FSPAK, e.g., in variance component procedures, always factorize before solving:

```
call fspak90('factorize', xx_ija)
```



```
call fspak90('solve',xx_ija,xy,sol)
```

The solving step assumes that the first factorization is intact, and subsequent solves involve the initial factorization.

Appendix I

Extensions to the parameter file

BLUPF90 can be modified so that the parameter file can contain additional lines with the following format:

```
OPTION name str1 str2 ....
```

This line(s) can be read by subroutine

```
call getoption(name,n,x,xc)
```

where str1, str2 are strings separated by spaces. If the line with a given name cannot be located, n=-1. Otherwise, the subroutine assigns: xc(1)=str1, xc(2)=str2,...and attempts to decode strings into real values: x1=value(str1),....; n contains the number of strings. x and xc are optional and their dimensions may be smaller than n in which case some strings/values are not stored. Upon exit, unit 40 points to the next line in the parameter file to the one located.

Example

Suppose that BLUPF90 was modified to add an autoregressive effect. Details for that effect are specified in the following parameter line:

```
OPTION autoregressive effect 2 rho .82 variance 500.0
```

Then, assuming declarations:

```
integer :: n, x(20)
```

```
character (10) :: xc(20)
```

the call

```
call getoption('autoregressive',n,x,xc)
```

will result in n=6, xc(1)='effect', xc(2)='2', xc(3)='rho',..., and x(1)=0, x(2)=2.0, x(3)=0, x(4)=.82,...., x(6)=500.0.